



### Assimilating Observations with Spatially and Temporally Correlated Errors in a Global Atmospheric Model

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# Outline

Dealing with correlated observation error in ensemble filters.

- 1. Idealized correlated error.
- 2. Difference observations.
- 3. Explicitly modeling instrument error.
- 4. Comparing the two methods.
- 5. Conclusions and recommendations.





# Most Observations Have Correlated Obs. Errors

Examples:

- Satellite radiances: instrument bias and aging.
- In situ soil moisture: instrument plus siting representativeness.
- Rainfall: gauge deficiencies plus siting.





Example: Correlated Error AR1 with Variance 1. Single Step Cov 0.999. Fixed for all cases.







Example: Correlated Error AR1 with Variance 1. Single Step Cov 0.999. Fixed for all cases. Vary uncorrelated error variance, 0.01



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Example: Correlated Error AR1 with Variance 1. Single Step Cov 0.999. Fixed for all cases. Vary uncorrelated error variance, 0.1



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Example: Correlated Error AR1 with Variance 1. Single Step Cov 0.999. Fixed for all cases. Vary uncorrelated error variance, 1.0





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Example: Correlated Error AR1 with Variance 1. Single Step Cov 0.999. Fixed for all cases. Vary uncorrelated error variance, 10.0







### Possible approaches to dealing with correlated obs error

- Ignore it (common),
- > Add parameters to forward operator, estimate them,
- Model it explicitly (various ways),
- Time difference observations.





## **1D Linear Exponential Growth Model**

True trajectory is always 0. Evolution is  $x_{t+1} = 1.1x_t$ Perturbations grow exponentially in time.





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## **Assimilating Correlated Observations**





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## **1D Exponential Growth Model Results**

#### Exact Smoother Result. Can't do better than this.



CAR

## **1D Exponential Growth Model Results**

#### EAKF Poor Unless Uncorrelated Error Dominates

growth= 0.100000 mbias= 0.000000 phi= 0.999000 sigma= 0.044710 bias= 0.000000





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## **Two Types of Difference Observations**





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## **1D Exponential Growth Model Results**

#### Exact Unlinked Difference Obs Much worse.

growth= 0.100000 mbias= 0.000000 phi= 0.999000 sigma= 0.044710 bias= 0.000000



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## **1D Exponential Growth Model Results**

#### EAKF is nearly exact for Unlinked Difference Obs.

growth= 0.100000 mbias= 0.000000 phi= 0.999000 sigma= 0.044710 bias= 0.000000



CAR

Data Assimilation Research Festbed







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## **1D Exponential Growth Model Results**

#### Exact linked Difference Obs Nearly Identical to Analytic.





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## **1D Exponential Growth Model Results**

#### EAKF Linked Diff. Obs. Good when correlated error dominates.

growth= 0.100000 mbias= 0.000000 phi= 0.999000 sigma= 0.044710 bias= 0.000000





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## **1D Exponential Growth Model Results**

#### Comparison to Just Using Raw Observations

growth= 0.100000 mbias= 0.000000 phi= 0.999000 sigma= 0.044710 bias= 0.000000



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Error

CAR

Data Assimilation Research Testbed

### Lorenz 63 Model



### Lorenz 63 Model





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# L63 Results, Linked Difference Obs

#### 3 Instruments



5 ensemble members. Adaptive inflation. Observations every 6 model timesteps.





# L63 Results, Linked Difference Obs

#### 3 Instruments





5 ensemble members. Adaptive inflation. Observations every 6 model timesteps.



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## L63 Summary

- Difference obs better unless uncorrelated error variance dominates.
- Improvement greater for single instrument.
- Ensembles often under-dispersive (what a surprise!).





### Lorenz 96 Model, 40-variables



Observing System 1 40 Instruments. Each has own correlated error.





#### Lorenz 96 Model, 40-variables



# L96 Results, Linked Difference Obs

#### 40 Instruments



10 ensemble members. Adaptive inflation, 0.2 halfwidth localization. Observations every model timestep.





# L96 Results, Linked Difference Obs

#### 40 Instruments





10 ensemble members. Adaptive inflation, 0.2 halfwidth localization. Observations every model timestep.



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## L96 Results, Linked Difference Obs

- Difference obs better unless uncorrelated error variance dominates.
- Improvement much greater for single instrument.
- Ensembles often over-dispersive.
- > Dealing with time correlation harder than space correlation.



































































30x60 horizontal grid, 5 levels.

Surface pressure, temperature, wind components. 28,800 variables.





## Low-Order Dry Dynamical Core: Observations



Assimilate once per day. 0.2 radian localization. Observe each surface pressure grid point. Uncorrelated obs error variance 100 Pa.





## Low-Order Dry Dynamical Core: Observations



Uncorrelated obs error variance 100 Pa.

Correlated obs error along 'simulated polar orbiter track'. Vary ratio of correlated to uncorrelated obs error variance.



## Low-Order Dry Dynamical Core: PS Results



Linked difference better for large correlated error. Standard better for small correlated error.





## Low-Order Dry Dynamical Core: T Results



Linked difference better for large correlated error. Standard better for small correlated error.





### PS RMSE Structure: Large Uncorrelated Error, Ratio 4

Surface Pressure RMSE (Pascals)







#### PS RMSE Structure: Moderate Uncorrelated Error, Ratio 1

Surface Pressure RMSE (Pascals)







### PS RMSE Structure: Small Uncorrelated Error, Ratio 1/4

Surface Pressure RMSE (Pascals)







### T RMSE Structure: Small Uncorrelated Error, Ratio 1/4

Level 3 Temperature RMSE (K)



# Base errors largest in tropics.







## Low-Order Dry Dynamical Core Summary

- Linked difference obs better for large correlated error.
- Linked difference not sensitive to correlated error size.
- Adaptive inflation struggles with large correlated error.
- Could use base approach for uncorrelated obs, difference for correlated error obs.
- For example, base for sondes, difference for radiances.
- Difference obs allows assimilating before knowing correlated error characteristics.





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## **Modeling Correlated Observation Error**

Error in examples is AR1:

(other types may need other methods).

Given correlated error now, can predict it at later time.

Have ensemble of model state.

Also ensemble of correlated error for each instrument.





## **Modeling Correlated Observation Error**

Forecast: Advance model & correlated error ensembles.
 Forward operator (for each ensemble member):
 Apply standard forward operator to state, H(x),
 Add correlated error.

- 3. Observation Increments: Compute normally.
- 4. State variable update:

Use regression (ensemble Kalman gain) to update:

Model state variables,

Correlated observation variables.





#### 320 Member deterministic ensemble filter (EAKF) State





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#### 320 Member deterministic ensemble filter (EAKF) State



All results for 5000 steps after 1000 step spin-up.



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#### 320 Member deterministic ensemble filter (EAKF) State



All results for 5000 steps after 1000 step spin-up.





#### 320 Member deterministic ensemble filter (EAKF) State



Exact asymptotic solution can be computed. Indistinguishable from 320 member ensemble.





#### 320 Member deterministic ensemble filter (EAKF) Obs. Error



Exact asymptotic solution can be computed. Indistinguishable from 320 member ensemble.





#### Fails for small ensembles with large correlated error. 320 Member EAKF 20 Member EAKF



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#### Fails for small ensembles with large correlated error. 10 Member EAKF 20 Member EAKF



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## **Ensemble Filters Scale Poorly for Random Fields**

Ensemble size > 1 is exact with no correlated obs error. Random walk evolution of correlated error is a problem. Can reduce this by reducing 'randomness' of ensemble.

AR1 series for observation error is:  $e_t = \phi e_{t-1} + Normal(0, \sigma_c^2)$ 

Given a posterior ensemble estimate of *e* at previous time: Expected prior mean at next time is:  $E(e_p) = \phi E(e_u)$ Expected prior variance is:  $E[var(e_p)] = \phi^2 E[var(e_u)] + \sigma_c^2$ 

'Deterministic' forecast for observation error:

'Adjust' ensemble to have exactly these statistics.





Deterministic works with smaller ensembles. Used hereafter.



Try multiplicative inflation of state.

10 Member inflated

**Global Posterior** 



# Multiplicative inflation for obs error ensemble is bad.





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#### Multiplicative inflation for state improves performance.

#### 10 Member

#### 10 Member inflated



## Lorenz 96 Model, 40-variables



Observing System 1: 40 Instruments. Each has own correlated error.




### Lorenz 96 Model, 40-instruments



20 member EAKF.

Optimal inflation.

Localization halfwidth 0.2



Modeling obs error helps. Spread is deficient.



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#### Lorenz 96 Model, 40-variables



### Lorenz 96 Model, 1-instrument



20 member EAKF.

Optimal inflation.

Localization halfwidth 0.2



Modeling obs error helps. Spread is better than many instrument case.





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#### Lorenz 96 Model, 40-instruments

Time difference assimilation best for large correlated error. Terrible for small correlated error.



20 member EAKF. Optimal inflation. Localization halfwidth 0.2





#### Lorenz 96 Model, 1-instrument

Time difference assimilation best for large correlated error. Not bad for small correlated error.



20 member EAKF. Optimal inflation. Localization halfwidth 0.2





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### Conclusions

- Modeling correlated obs error 'optimal' for large ensemble.
- Sampling error is a problem for small ensembles.
- Multiplicative state inflation can reduce this problem.
- Additive inflation for obs error may help?
- Time difference obs effective for large correlated error.

General things to keep in mind:

- Details of filtering problem determine best methods.
- Making models/filters more deterministic generally helps.





## Learn more about DART at:



# www.image.ucar.edu/DAReS/DART

Anderson, J., Hoar, T., Raeder, K., Liu, H., Collins, N., Torn, R., Arellano, A., 2009: *The Data Assimilation Research Testbed: A community facility.* BAMS, **90**, 1283—1296, doi: 10.1175/2009BAMS2618.1



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