

Measurements of Turbulence Profiles with Scanning Doppler Lidar for Wind Energy Applications

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Acknowledgments

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Complements of Steve Hannon

Beam Is Scanned to Provide
2-3D Spatial Coverage

Return Light is Doppler
Shifted by Moving Aerosols

2 μm wavelength system:
60 m (400 nsec) Pulse
transmitted @ 500Hz

1.6 μm wavelength system
~40 m (270 nsec) Pulse
transmitted @ 750Hz

IT'S EYE SAFE!

'Pencil' Beam
Width 10-30 cm

Portion of Scattered
Light Collected
By Telescope

Relative Wind Induces a Doppler
Frequency Shift in the Backscattered
Light; This Frequency Shift Is
Detected by the Sensor



- Doppler Lidar = Infrared Doppler Radar
- Infrared: Instead of Raindrops, Lidar Uses Natural Particulates
- Doppler: Velocity/Wind Sensing (Strength)
- Radar: Accurate Position Information



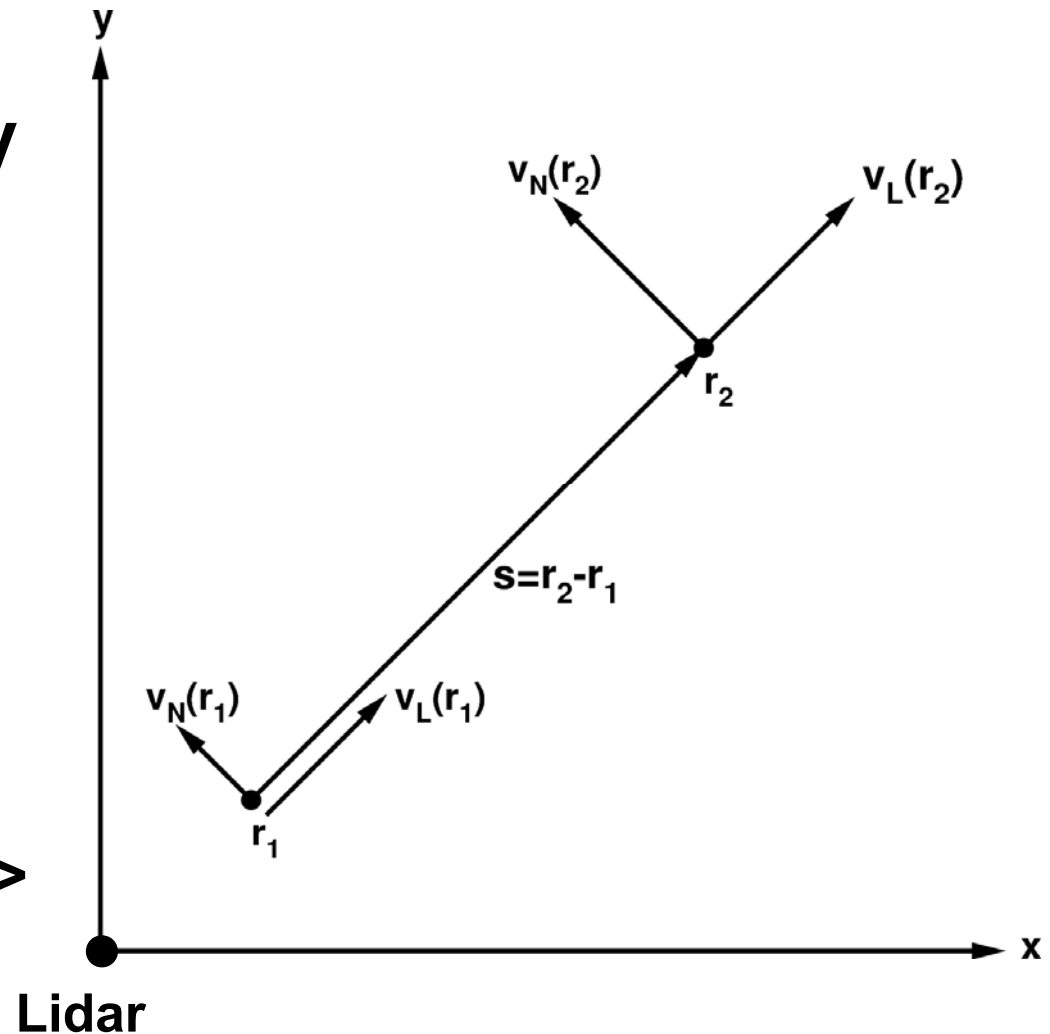
Point Statistics of Turbulence

- Longitudinal velocity (radial)
- Transverse velocity
- Longitudinal structure function

$$D_{LL}(s) = \langle [v_L(r_2) - v_L(r_1)]^2 \rangle$$

- Transverse structure function

$$D_{NN}(s) = \langle [v_N(r_2) - v_N(r_1)]^2 \rangle$$



Horizontal Isotropic Turbulence

- **Universal description - longitudinal**

$$D_{LL}(s) = 2 \sigma_u^2 \Lambda(s/L_{0u})$$

- σ_u – longitudinal standard deviation
- L_{0u} – longitudinal outer scale
- $\Lambda(x)$ – universal function (von Kármán)
- $s \ll L_{0u}$

$$D_{LL}(s) = C_K \varepsilon_u^{2/3} s^{2/3} \quad C_K \sim 2.0$$

- ε_u = energy dissipation rate

Horizontal Isotropic Turbulence

- **Universal description - transverse**

$$D_{NN}(s) = 2 \sigma_v^2 \Lambda(s/L_{0v})$$

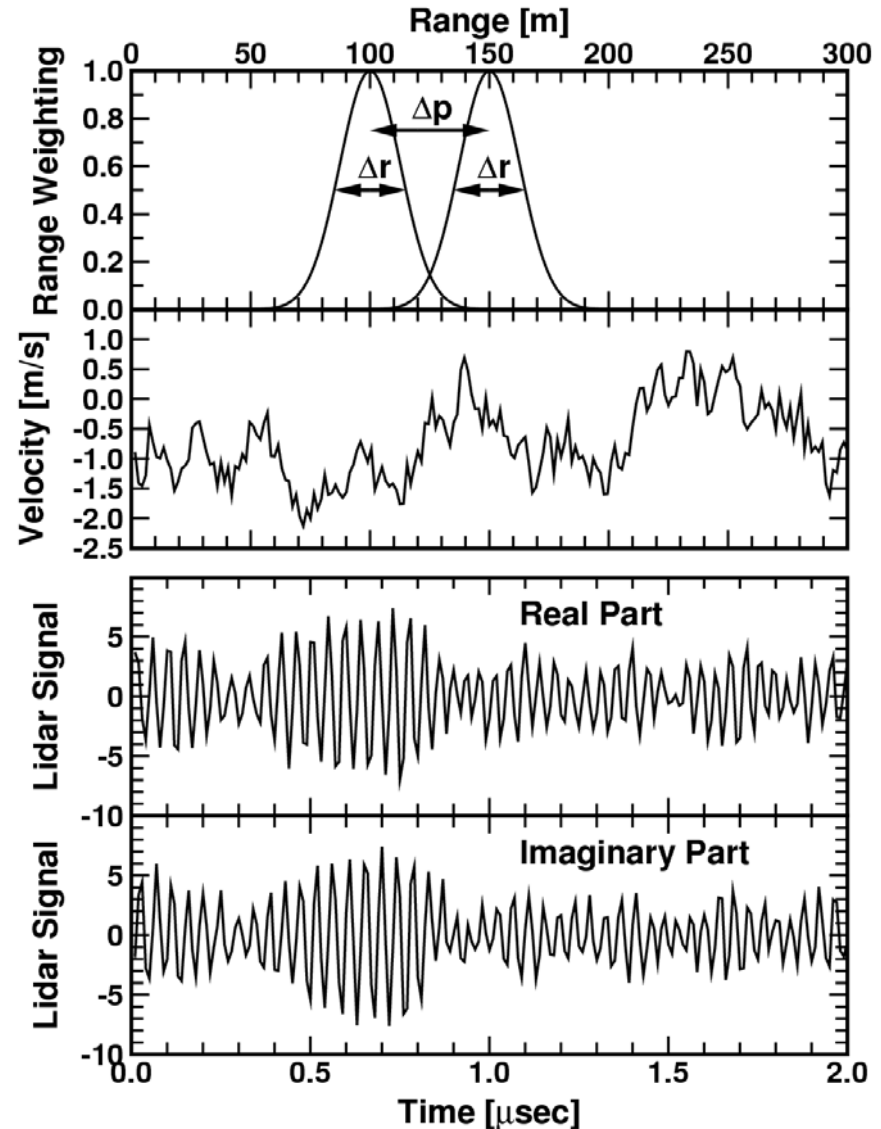
- σ_v – transverse standard deviation
- L_{0v} – transverse outer scale
- $\Lambda(x)$ – universal function (von Karman)
- $s \ll L_{0v}$

$$D_{NN}(s) = C_J \varepsilon_v^{2/3} s^{2/3} \quad C_J \sim 2.67$$

- ε_v = energy dissipation rate

Doppler LIDAR Range Weighting

- Time of data maps to range ($1 \mu\text{s} = 150 \text{ m}$)
- Pulsed lidar velocity measurements filter the random radial velocity $v_r(z)$
- Pulse width Δr
- Range gate length defined by processing interval Δp
- Range weighting $W(r)$



LIDAR Data and Range Weighting

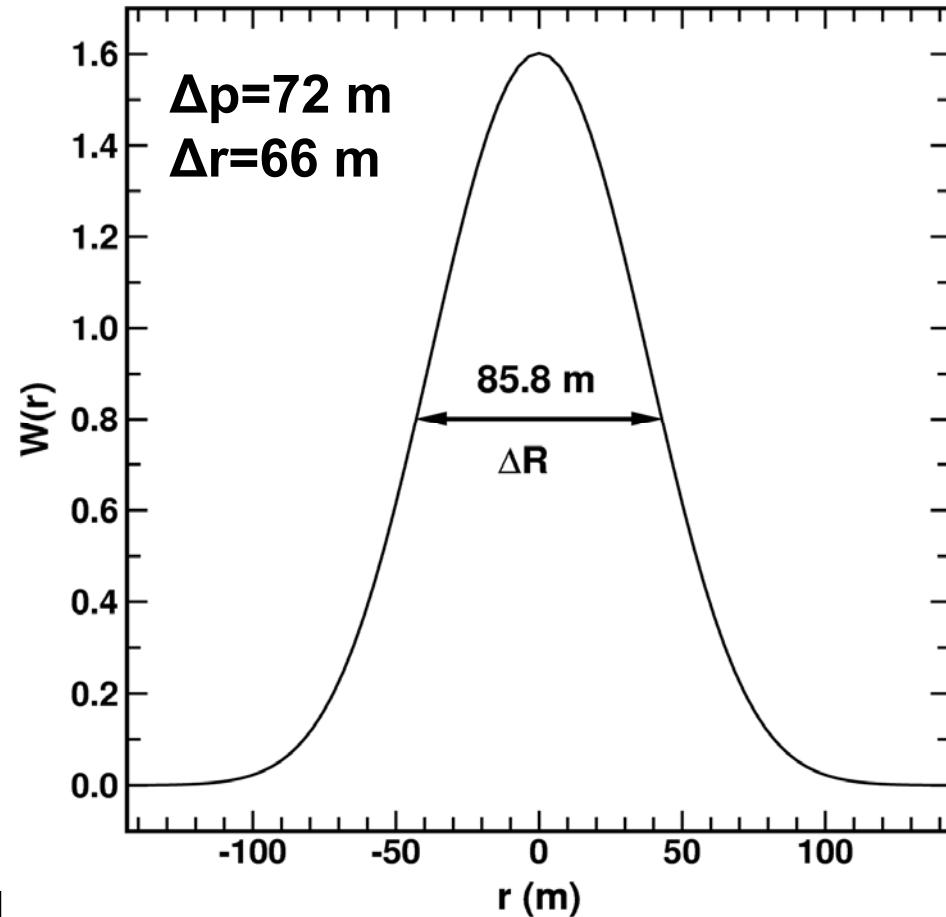
- LIDAR radial velocity estimates at range R

$$v(R) = v_{\text{wgt}}(R) + e(R)$$

- $v_{\text{wgt}}(R)$ - pulse weighted velocity
- $e(R)$ estimation error

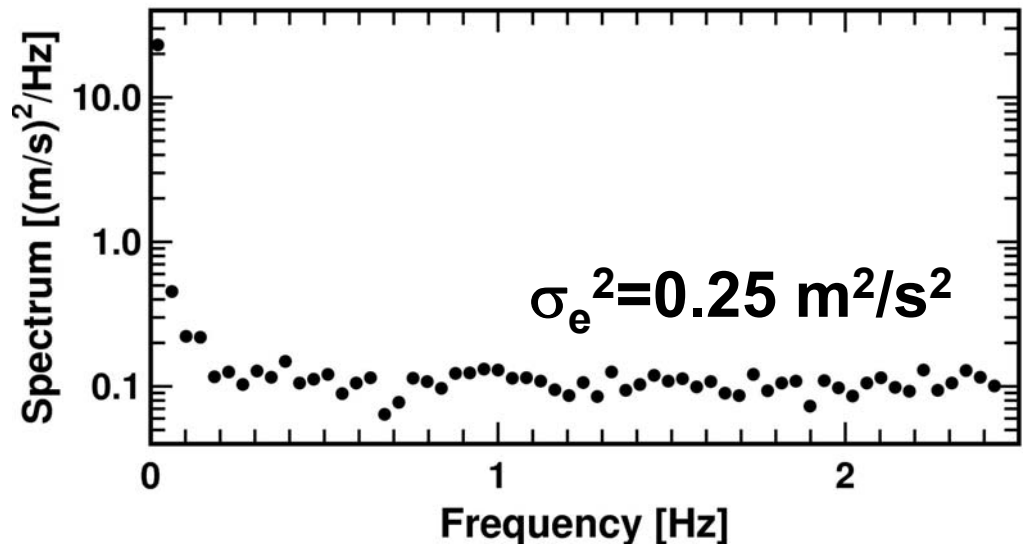
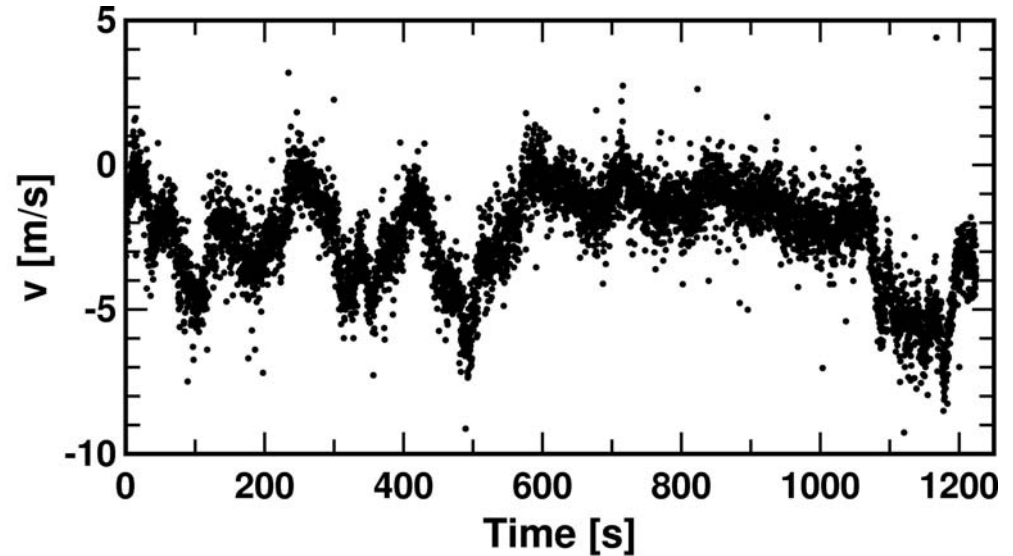
$$v_{\text{wgt}}(R) = \int v_r(z) W(R-z) dz$$

- $v_r(z)$ - random radial velocity
- $W(r)$ - range weighting



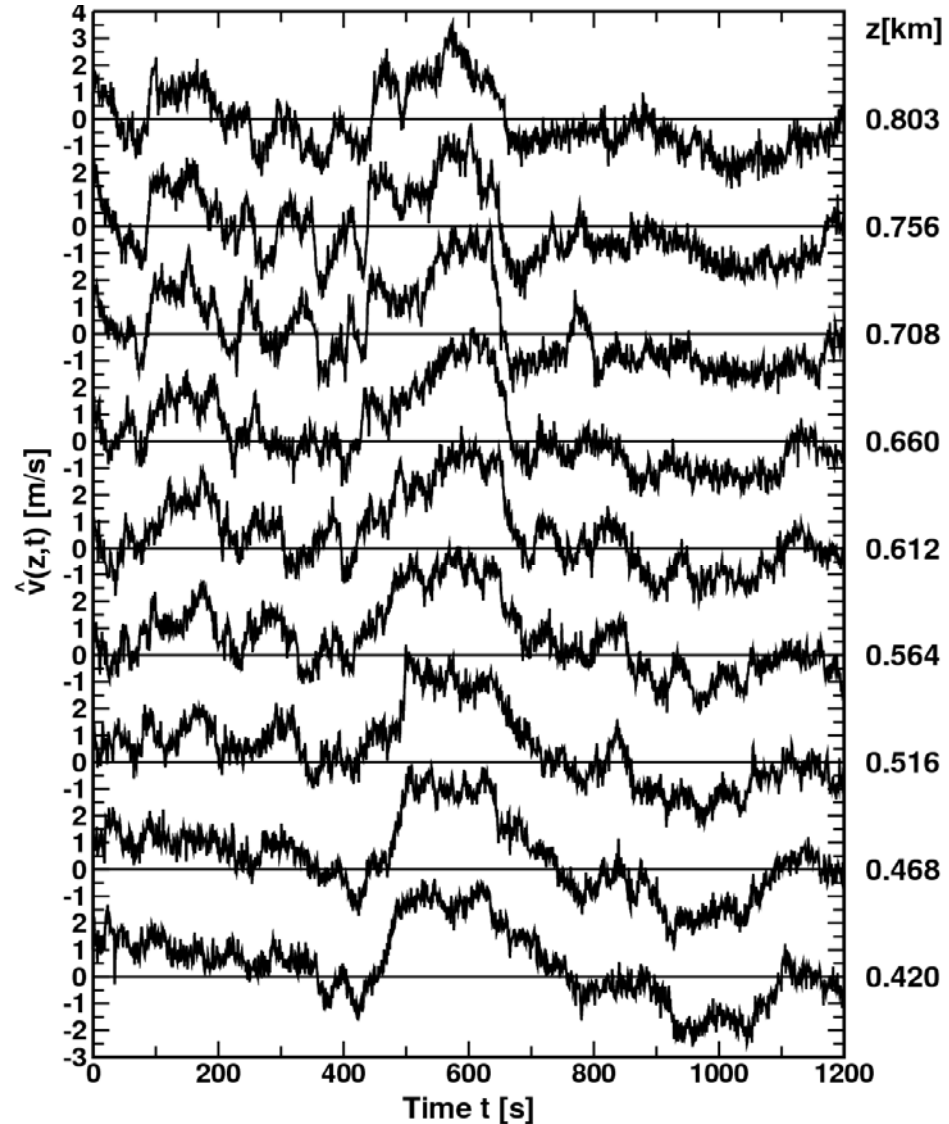
Estimates of Random Error

- Radial velocity error variance σ_e^2 can be determined from data
- Spectral noise floor is proportional to σ_e^2



Non-Scanning Lidar Data

- Vertically pointed beam
- Time series of velocity for various altitudes z
- High spatial and temporal resolution
- Resolves turbulence



Lidar Structure Function (Radial)

- **Corrected longitudinal structure function**

$$D_{\text{wgt}}(\mathbf{s}) = D_{\text{raw}}(\mathbf{s}) - 2 \sigma_e^2(\mathbf{s})$$

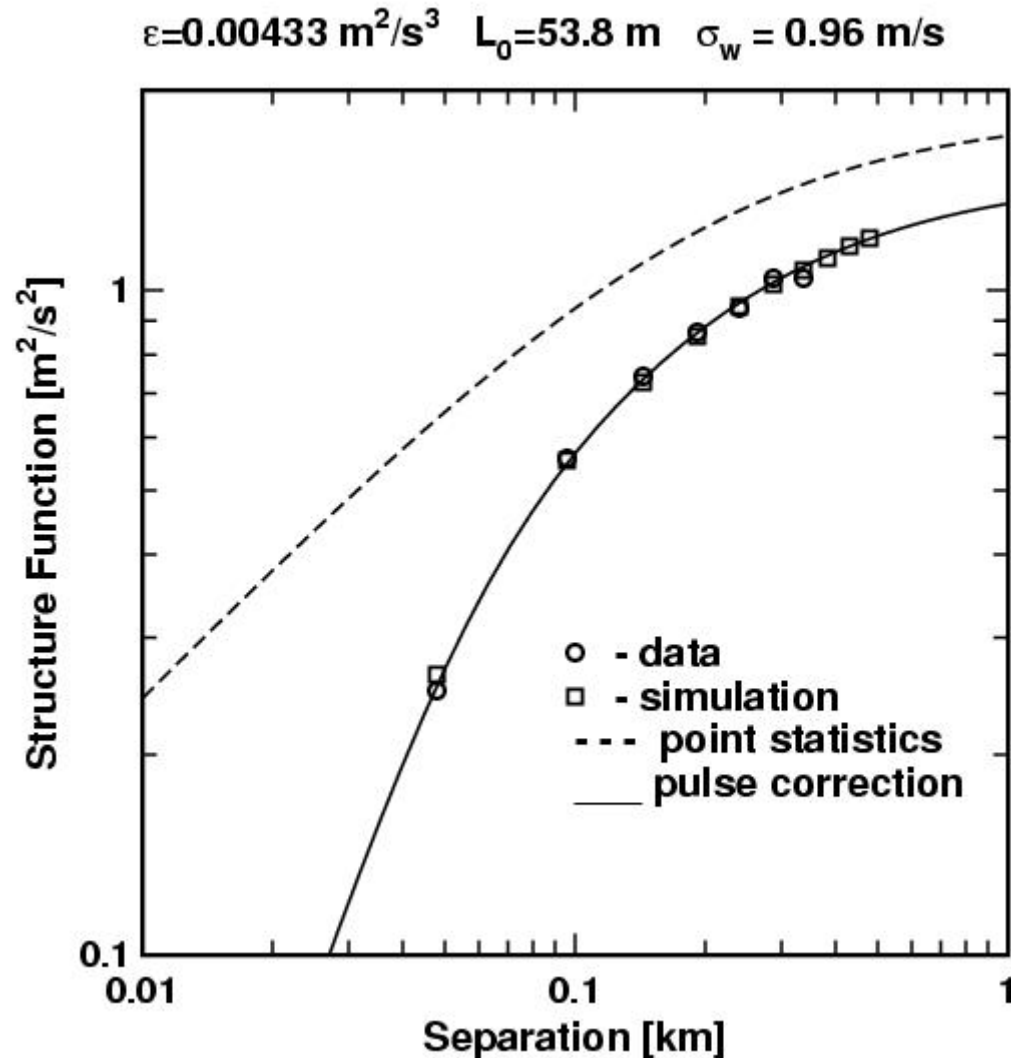
- $D_{\text{raw}}(\mathbf{s})$ – raw structure function
- $\sigma_e^2(\mathbf{s})$ – correction for estimation error
- **Theoretical relation ($\Delta h \ll \Delta p$)**

$$D_{\text{wgt}}(\mathbf{s}) = 2 \sigma_u^2 G(\mathbf{s}, L_{0u}, \Delta p, \Delta r)$$

- **Best-fit to data produces estimates of $\sigma_u, L_{0u}, \epsilon_u$**

Turbulence Statistics

- Calculate corrected structure function
- Determine best-fit to theoretical model
- Best-fit parameters are estimates of turbulence statistics

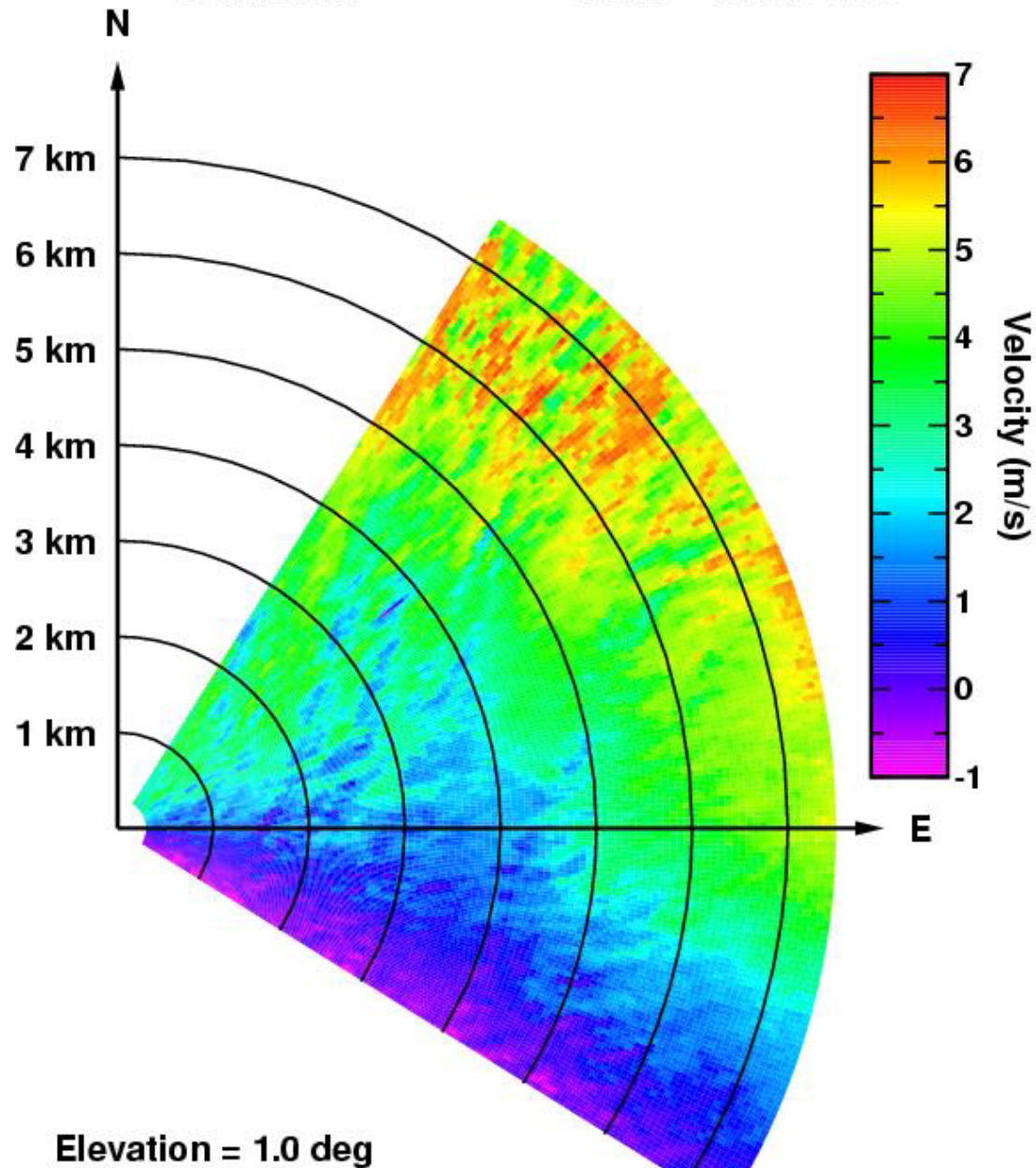


Scanning Lidar Data

- **High-resolution profiles of wind speed and turbulence statistics**
- **Highest statistical accuracy**
- **Rapid update rates compared with tower derived statistics**
- **Can provide profiles at multiple locations**
- **Ideal for some wind energy applications**

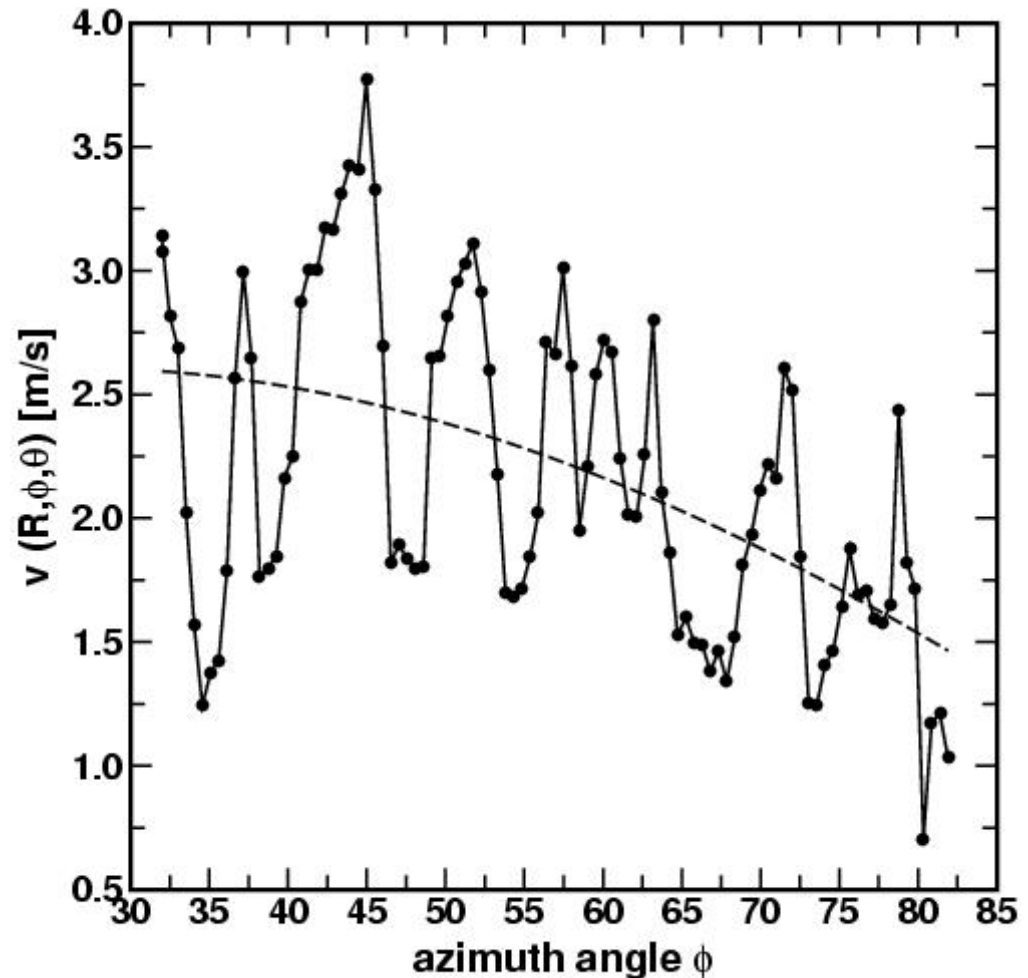
LIDAR Velocity Map for 1°

- Radial velocity
- 100 range-gates along beam
- 180 beams ($\Delta\phi=0.5$ degree)
- 18 seconds per scan
- $\Delta h=R \Delta\phi \ll \Delta\rho$ for $R<2\text{km}$



Wind Speed and Direction

- **Best-fit lidar radial velocity for best-fit wind speed and direction**
- **Fluctuations are turbulence**
- **Longitudinal fluctuations along the lidar beam**
- **Transverse fluctuation in azimuth direction**



Lidar Structure Function (Azimuth)

- **Corrected azimuth structure function**

$$D_{\text{wgt}}(\mathbf{s}) = D_{\text{raw}}(\mathbf{s}) - 2 \sigma_e^2(\mathbf{s})$$

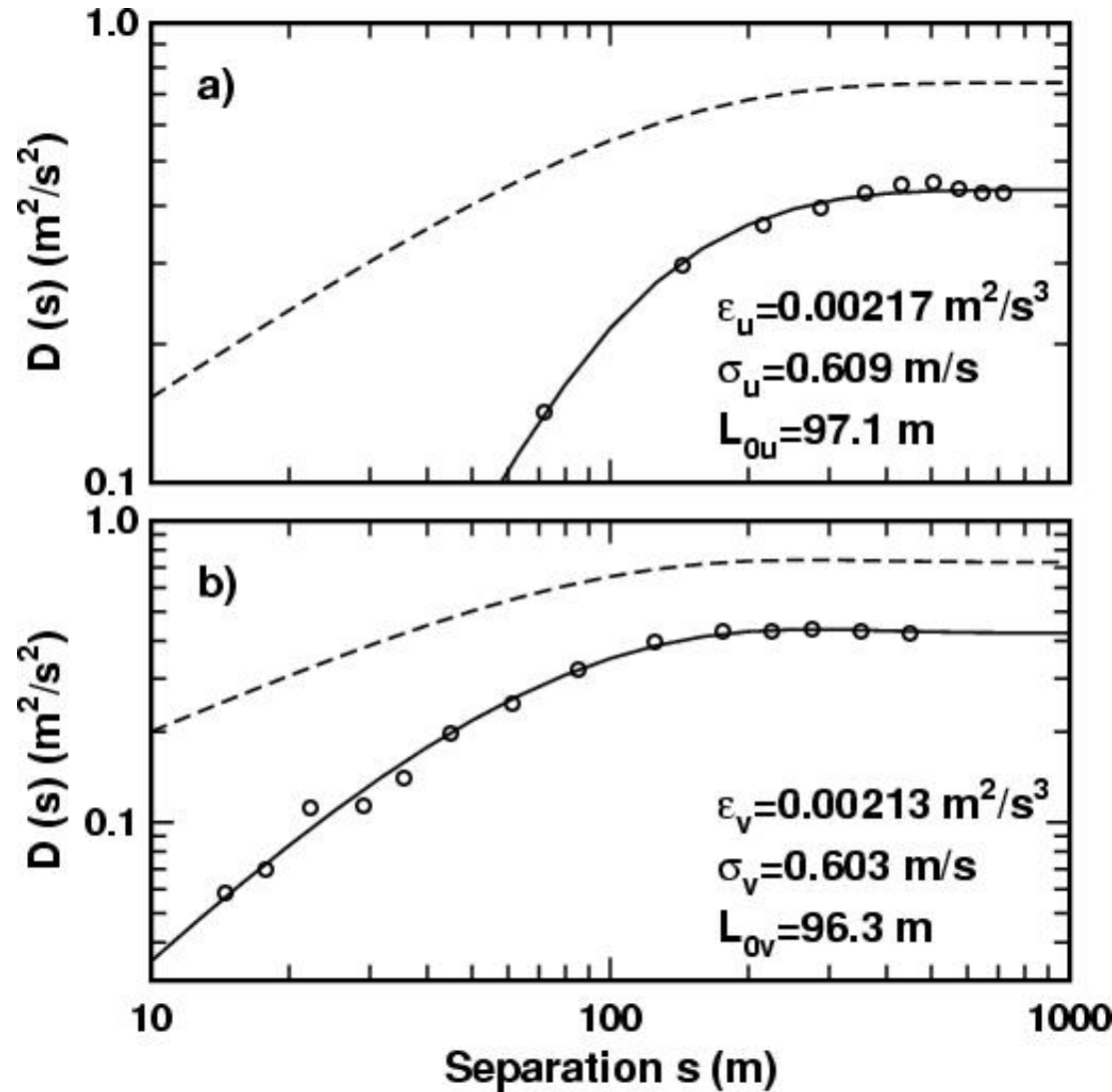
- $D_{\text{raw}}(\mathbf{s})$ – raw structure function
- $\sigma_e^2(\mathbf{s})$ – correction for estimation error
- **Theoretical relation ($\Delta h \ll \Delta p$)**

$$D_{\text{wgt}}(\mathbf{s}) = 2 \sigma_v^2 G_\varphi(\mathbf{s}, L_{0v}, \Delta p, \Delta r)$$

- **Best-fit to data produces estimates of $\sigma_v, L_{0v}, \varepsilon_v$**

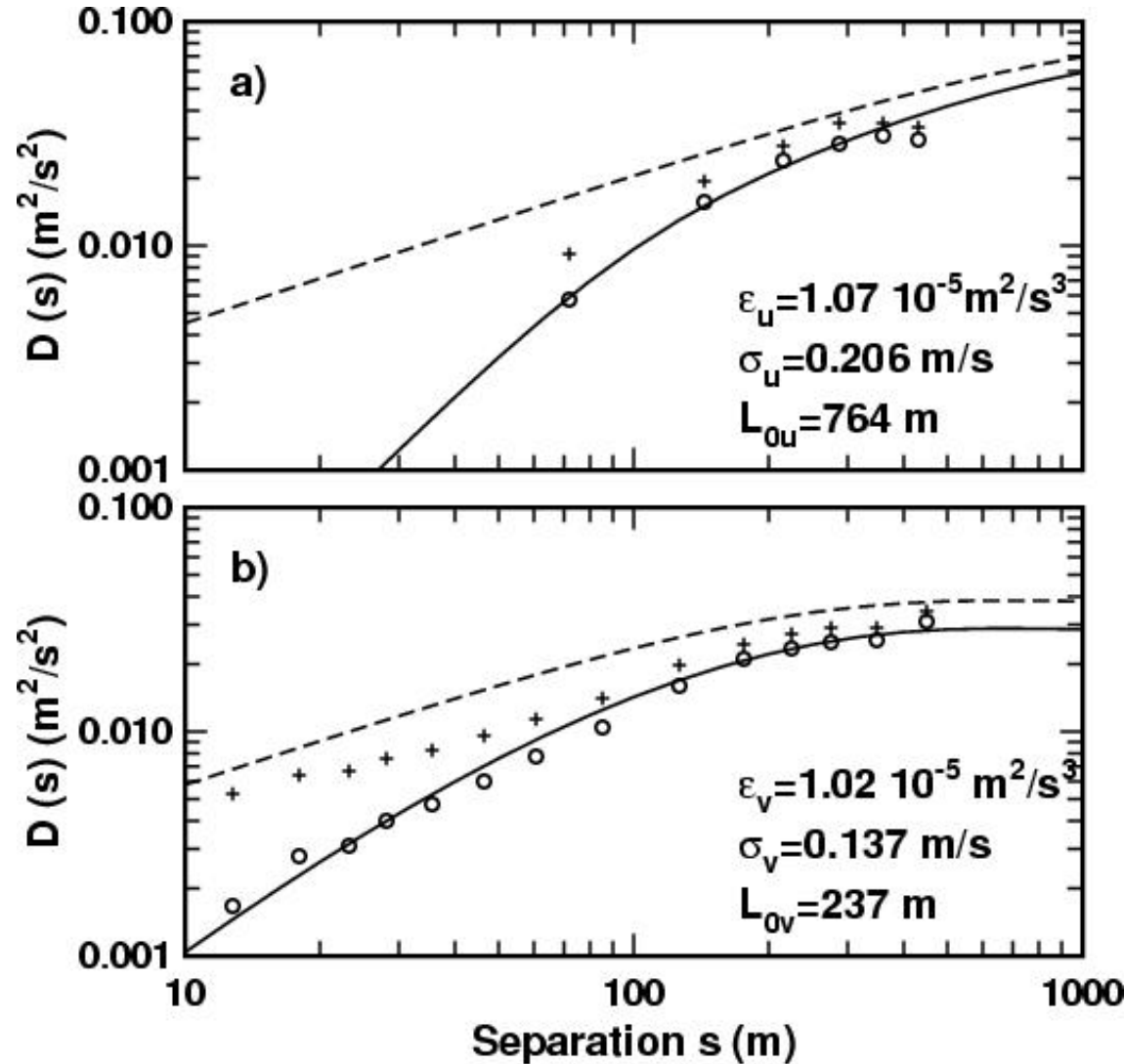
Turbulence Estimates Zero Elevation

- **Structure function of radial velocity in range a)**
- **Best fit produces estimates of σ_u , ε_u , L_{0u}**
- **Structure function in azimuth b)**
- **Best fit produces estimates of σ_v , ε_v , L_{0v}**

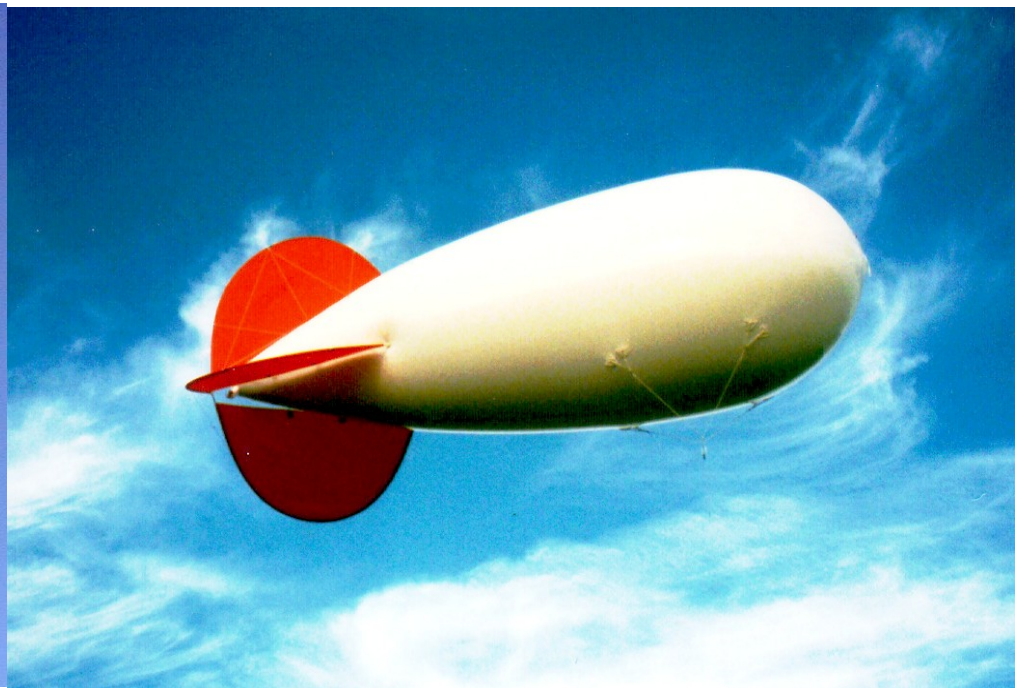


Turbulence Estimates H=80 m

- Best fit for noise corrected structure function (o)
- Raw structure functions (+)
- Radial velocity a) has small elevation angles ($\leq 4^\circ$)
- Structure function in azimuth b)
- Good agreement in ε_u and ε_v (isotropy)



CIRES Tethered Lifting System (TLS): Hi-Tech Kites or Aerodynamic Blimps



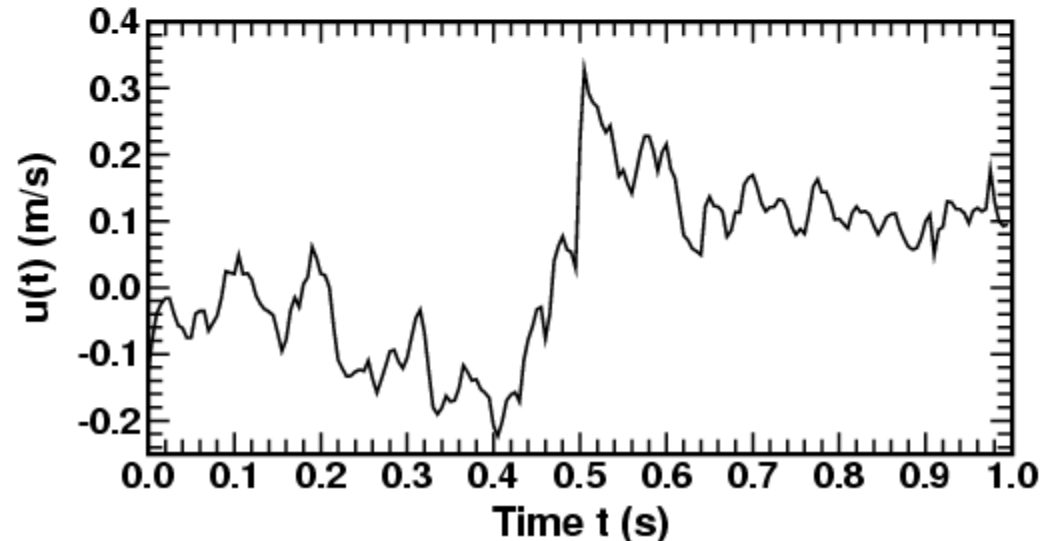
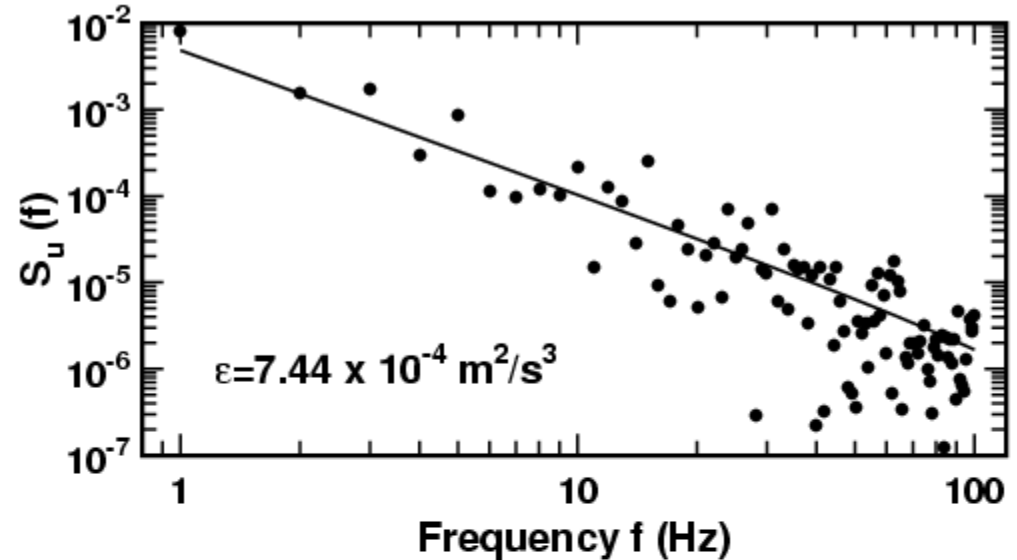
High Resolution Profiles from TLS Data

- TLS instrumentation used as “truth” for turbulence profiles
- Hot-wire sensor for small scale velocity
- Cold-wire sensor for small scale temperature



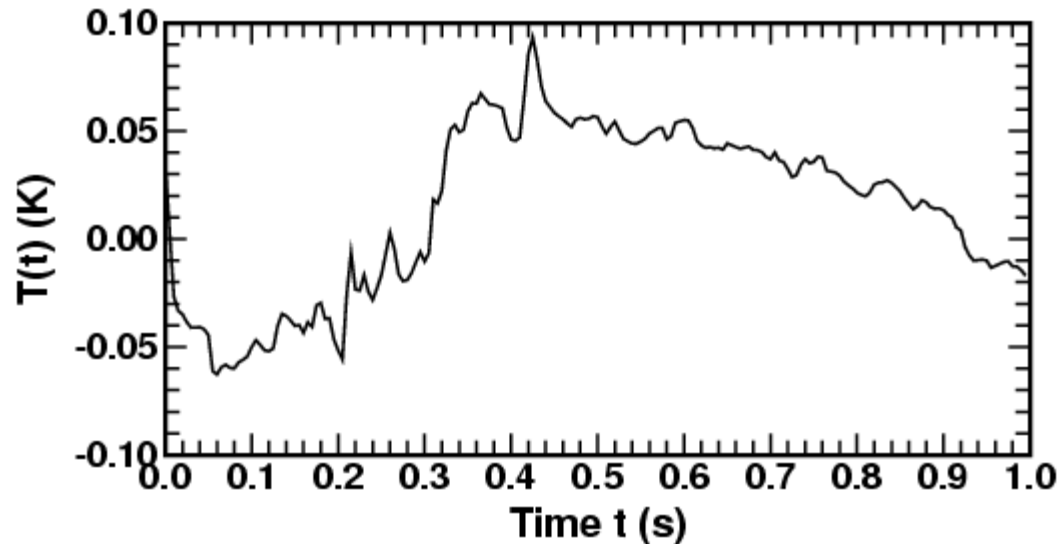
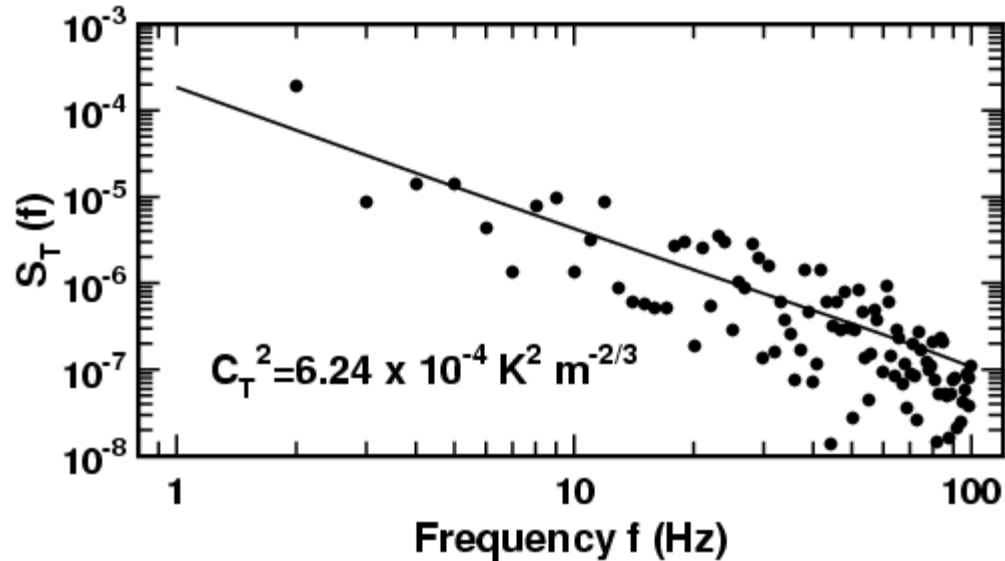
Velocity Turbulence

- Along-stream velocity $u(t)$
- Spectrum $S_u(f)$
- Taylor's frozen hypothesis
- Energy dissipation rate ε

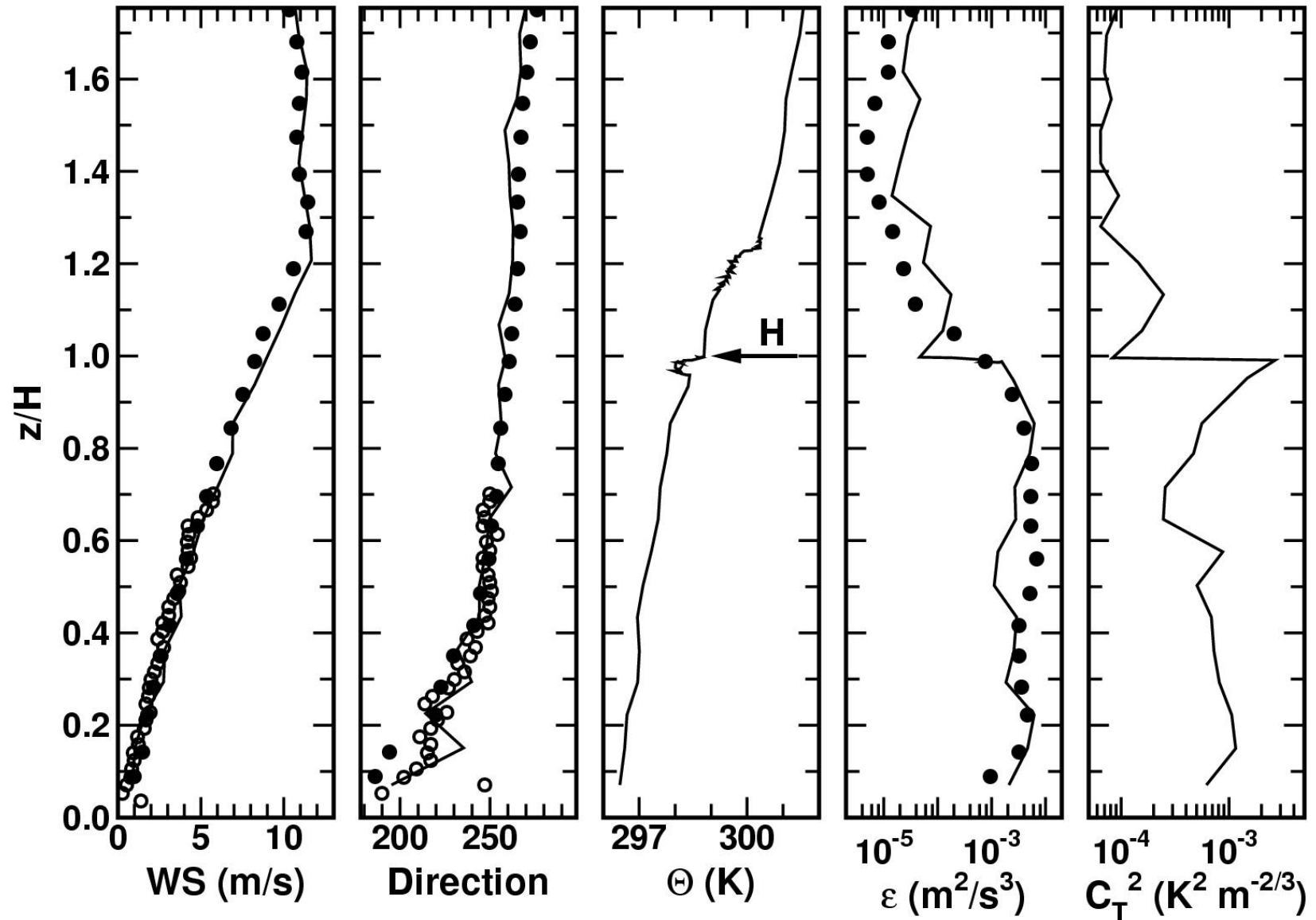


Temperature Turbulence

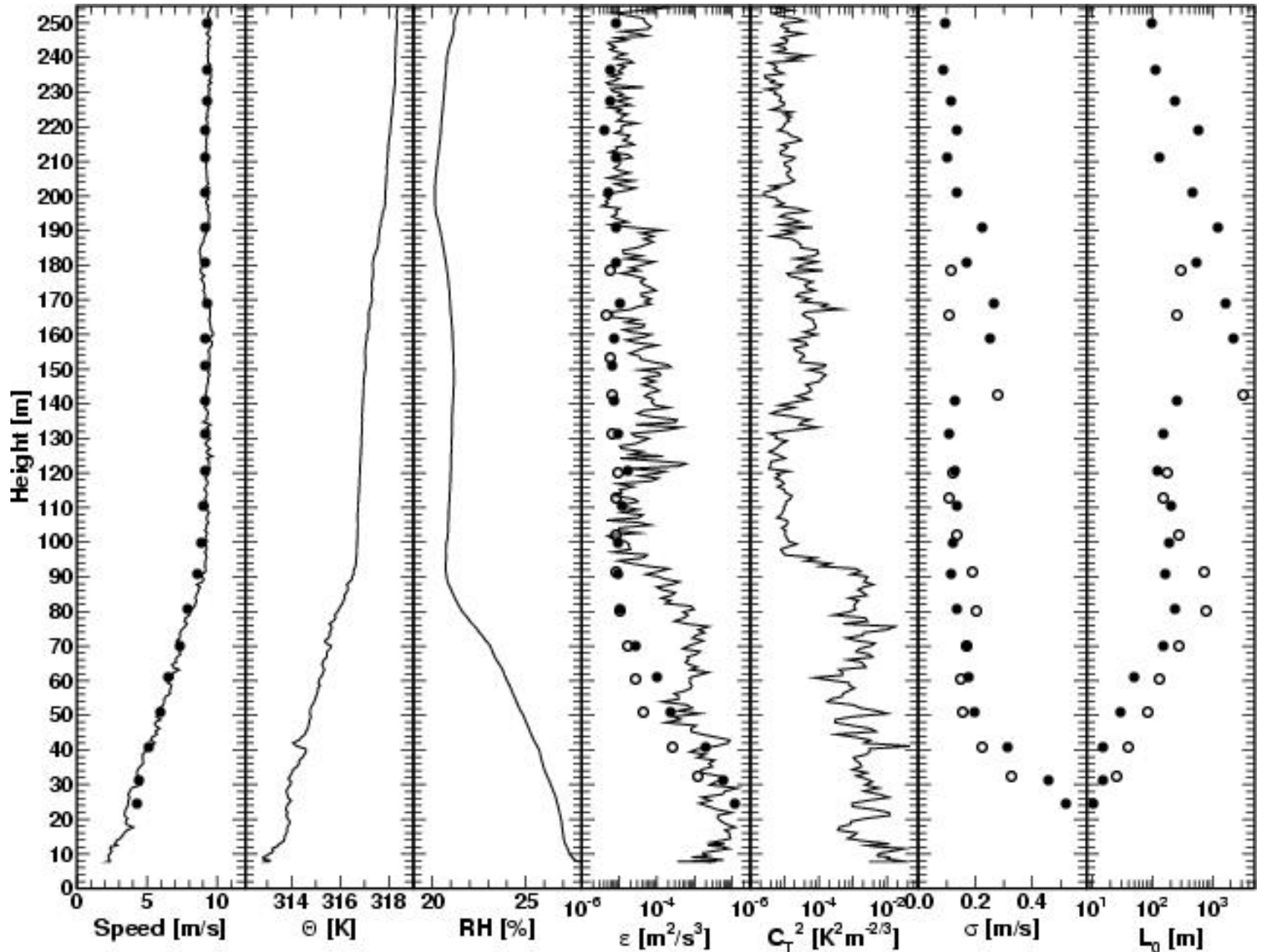
- Along-stream temperature $T(t)$
- Spectrum $S_T(f)$
- Taylor's frozen hypothesis
- Temperature structure constant C_T^2



LIDAR, SODAR and TLS (Blimp)



Lidar and TLS Profiles



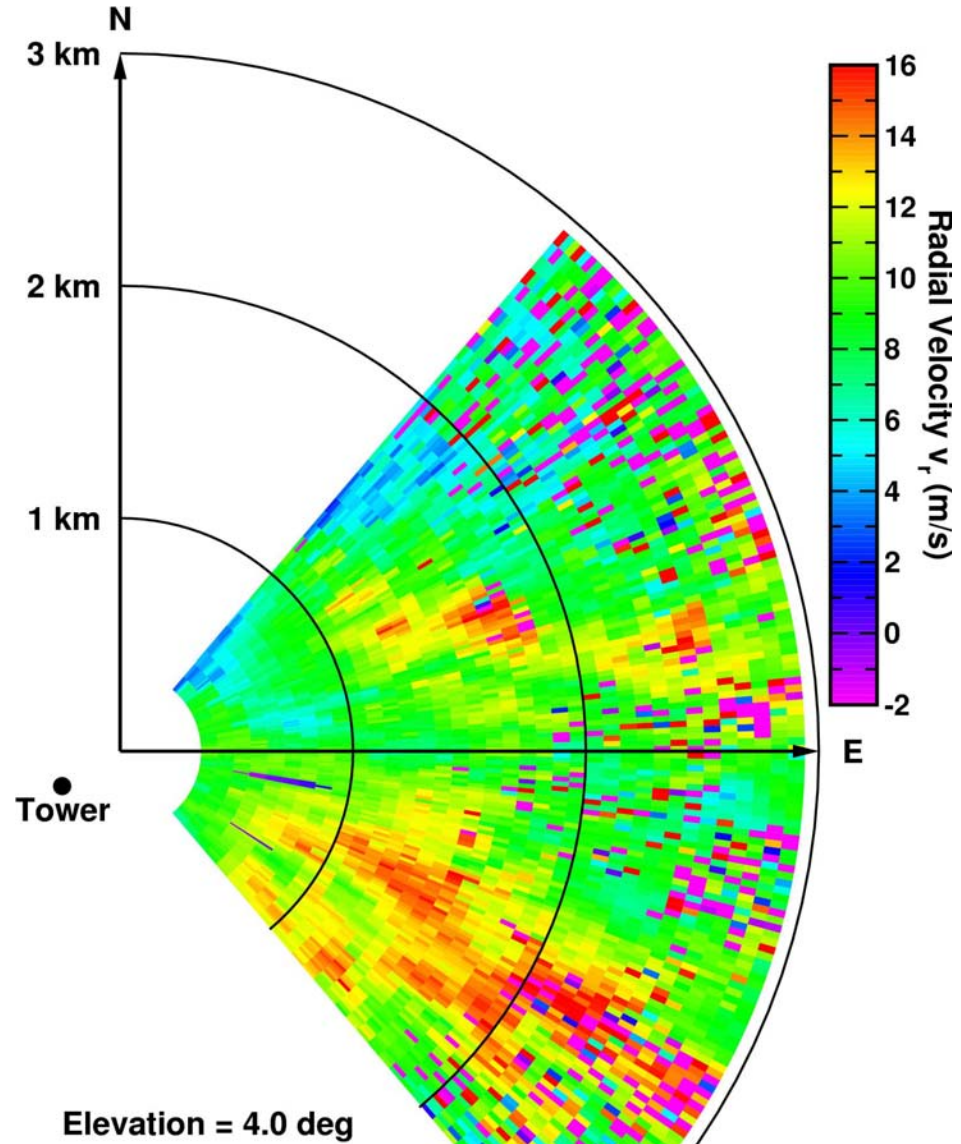
Wind Energy Applications

- Towers are expensive and limited in height coverage
- CW Doppler lidar can measure winds near an individual turbine
- Scanning Doppler lidar can monitor large area upstream of a wind farm
- Autonomous lidar (CTI)
 - Airports
 - Homeland security DC



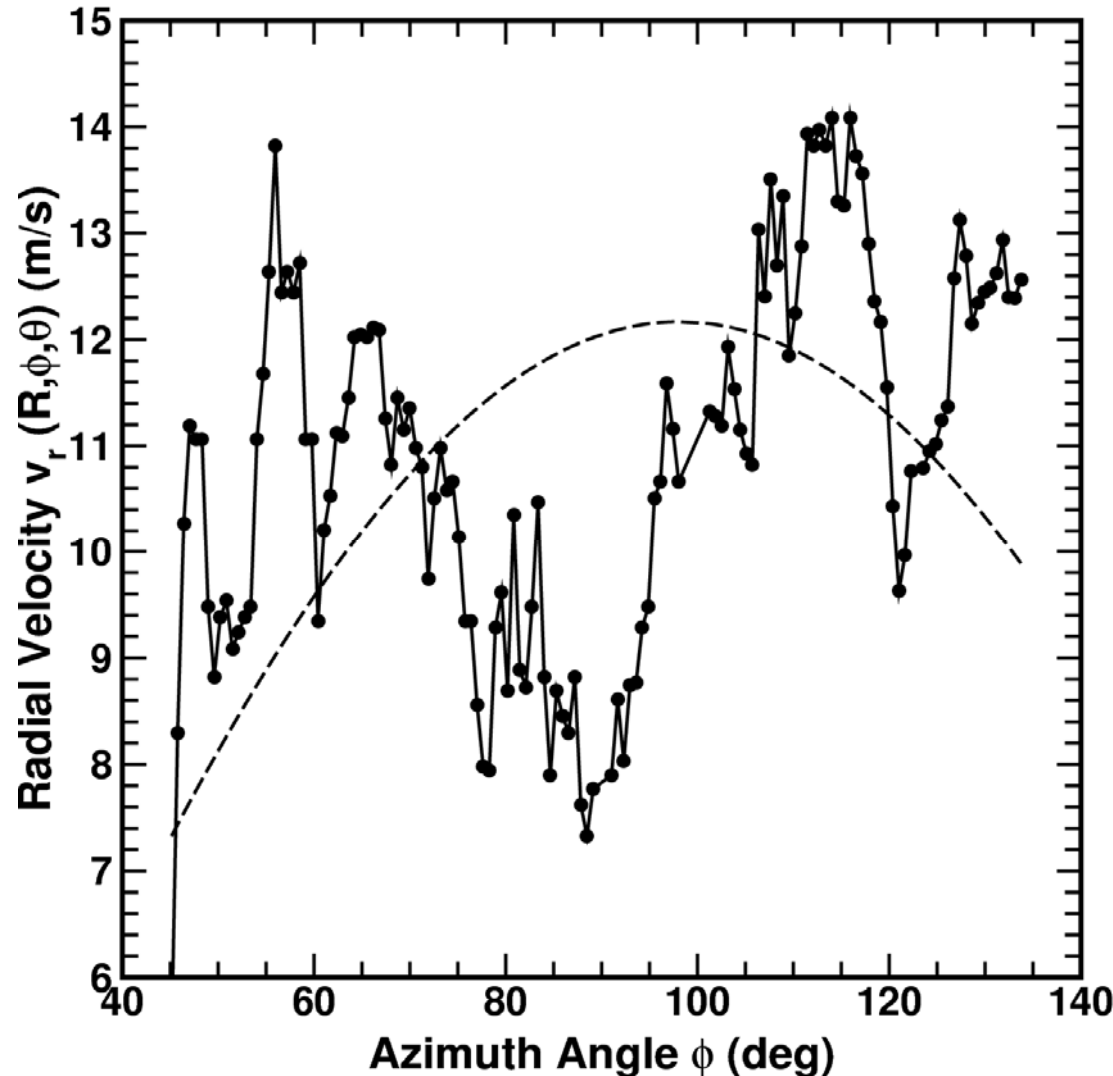
Doppler Lidar at NREL

- Radial velocity map
- Large eddies
- Large velocity variations
- Multiple elevation angles provide 3D sampling



High Turbulence

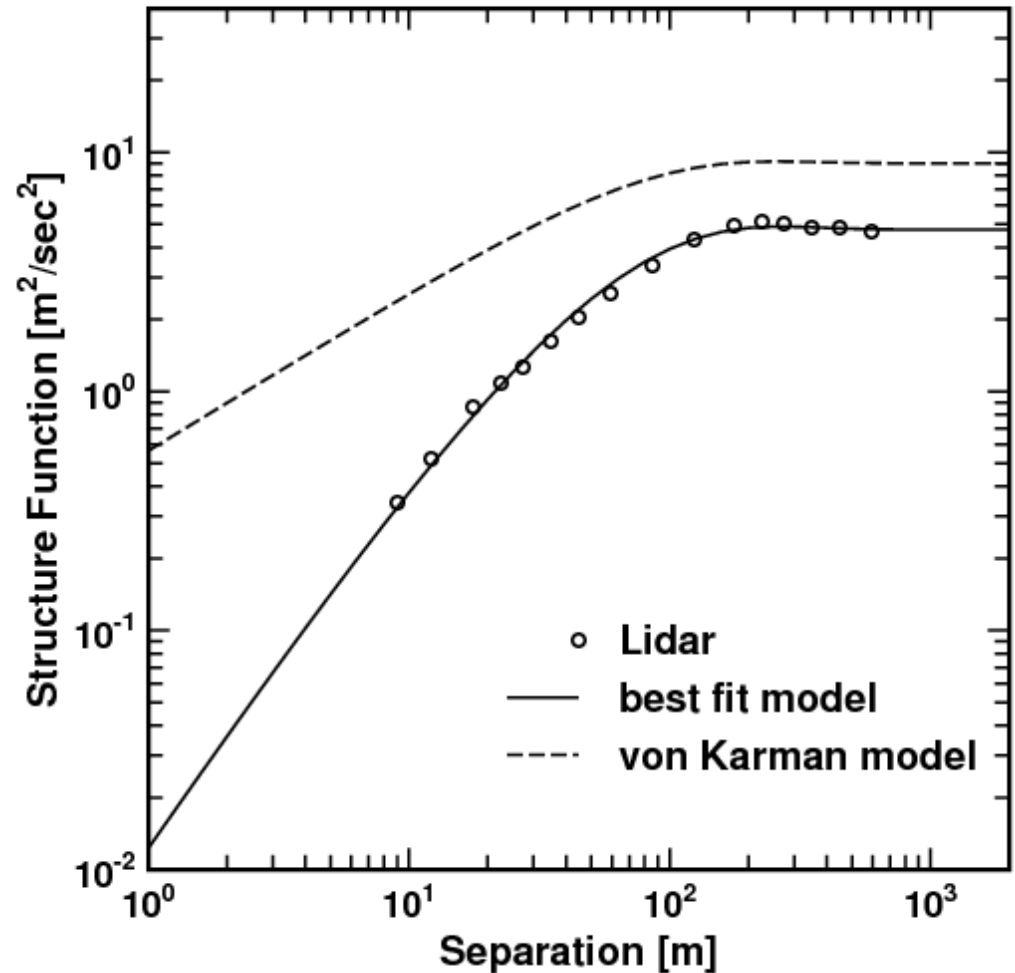
- Large fluctuations about the best fit wind speed
- 3D average required for accurate statistics



Azimuth Structure Functions

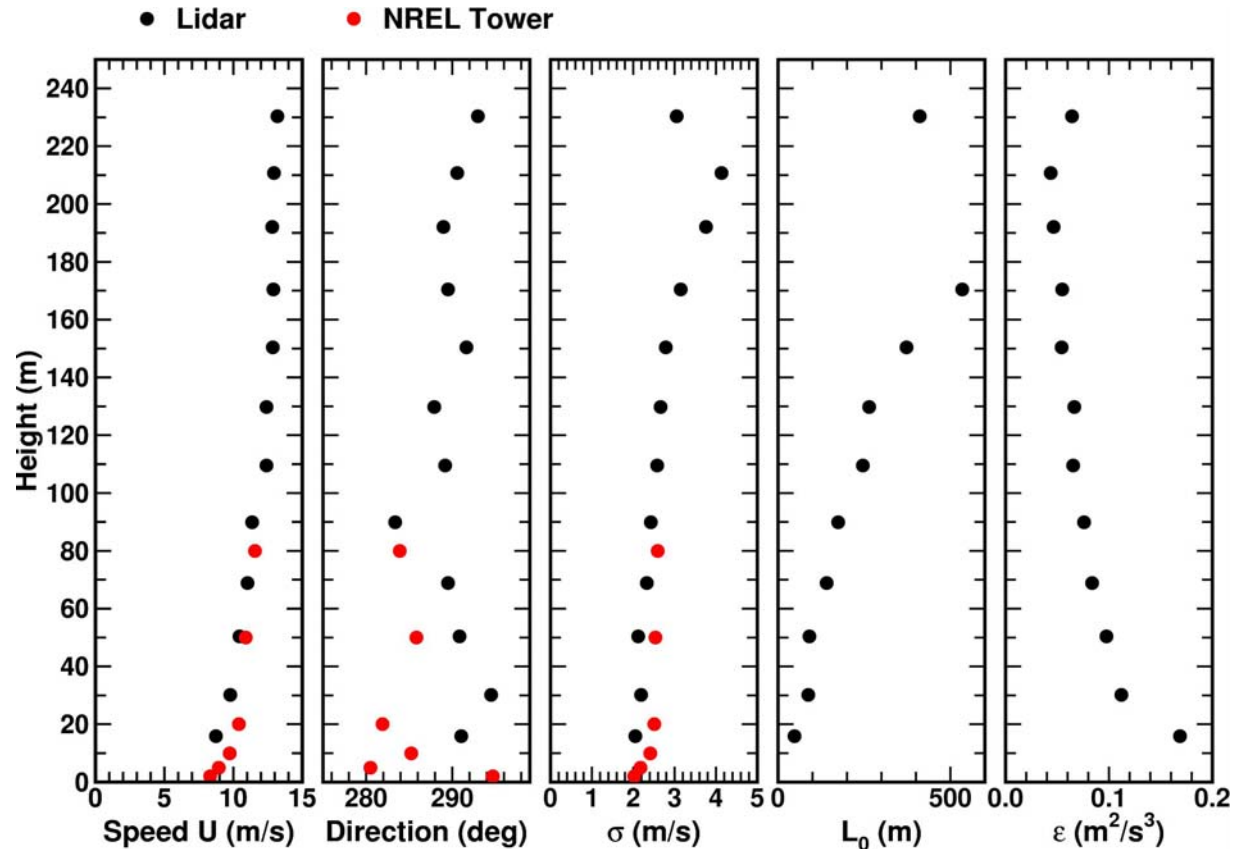
H= 50.35 m WS=10.4302 m/s dir=290.82° index=3
 $\varepsilon=0.97485\text{E-}01 \text{ m}^2/\text{s}^3$ $L_0=91.39 \text{ m}$ $\sigma=2.121 \text{ m/s}$

- **Best-fit model provides robust turbulence statistics**
- **Profiles produced from 3D volume scan by processing data in altitude bins**



Atmospheric Profiles

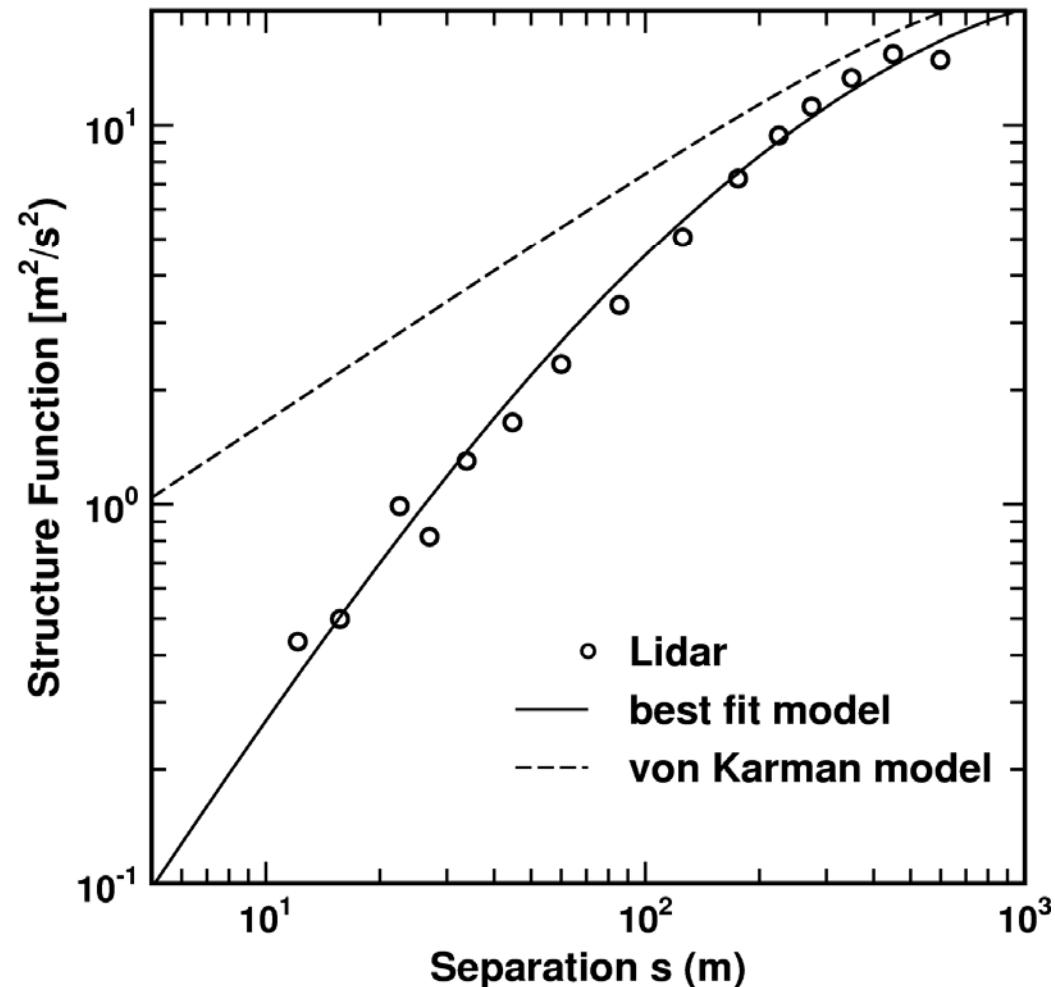
- **Accurate profiles produced**
- **Most complete description of wind and turbulence available**
- **Ideal for site resource assessment**



Large Turbulent Length Scale

- **Difficult to separate turbulence and larger scale processes**
- **Similar to troposphere and Boreas Data**
- **Violates Cartesian approximation of analysis**
- **What is optimal methodology?**

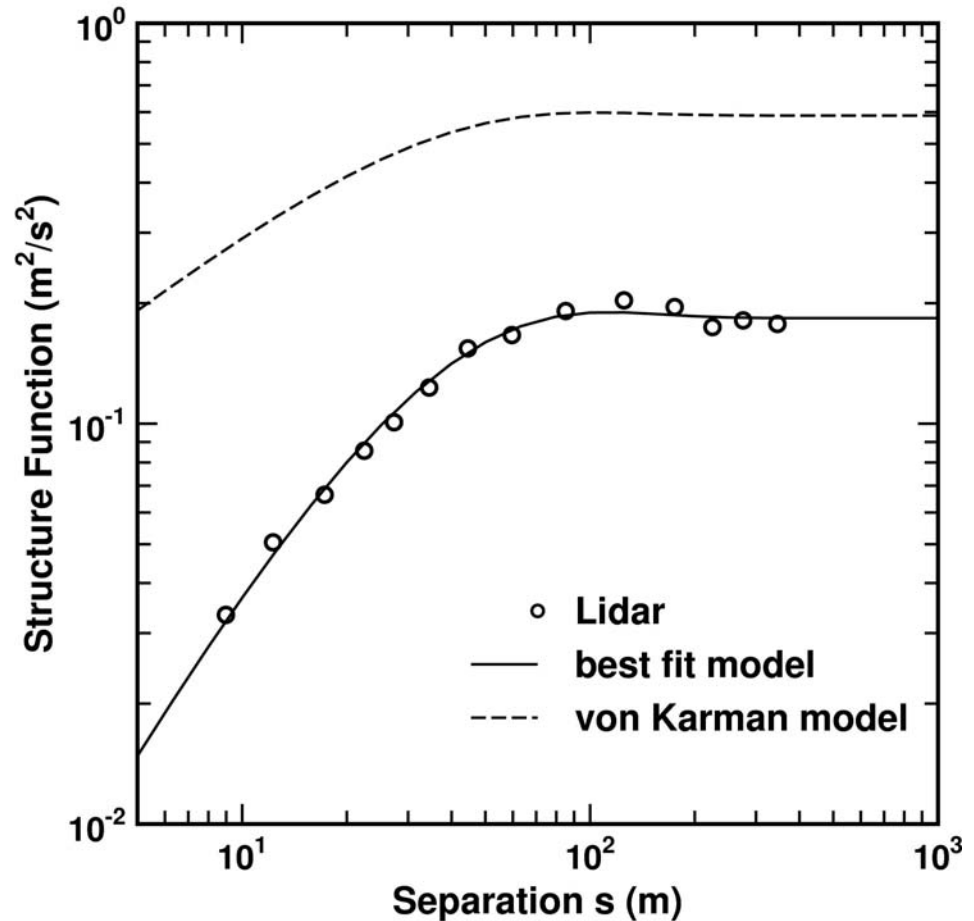
H= 192.00 m WS=12.8012 m/s dir=289.01° index=10
 $\varepsilon=0.48701\text{E-}01 \text{ m}^2/\text{s}^3$ $L_0=870.68 \text{ m}$ $\sigma=3.568 \text{ m/s}$



Small Turbulent Length Scale

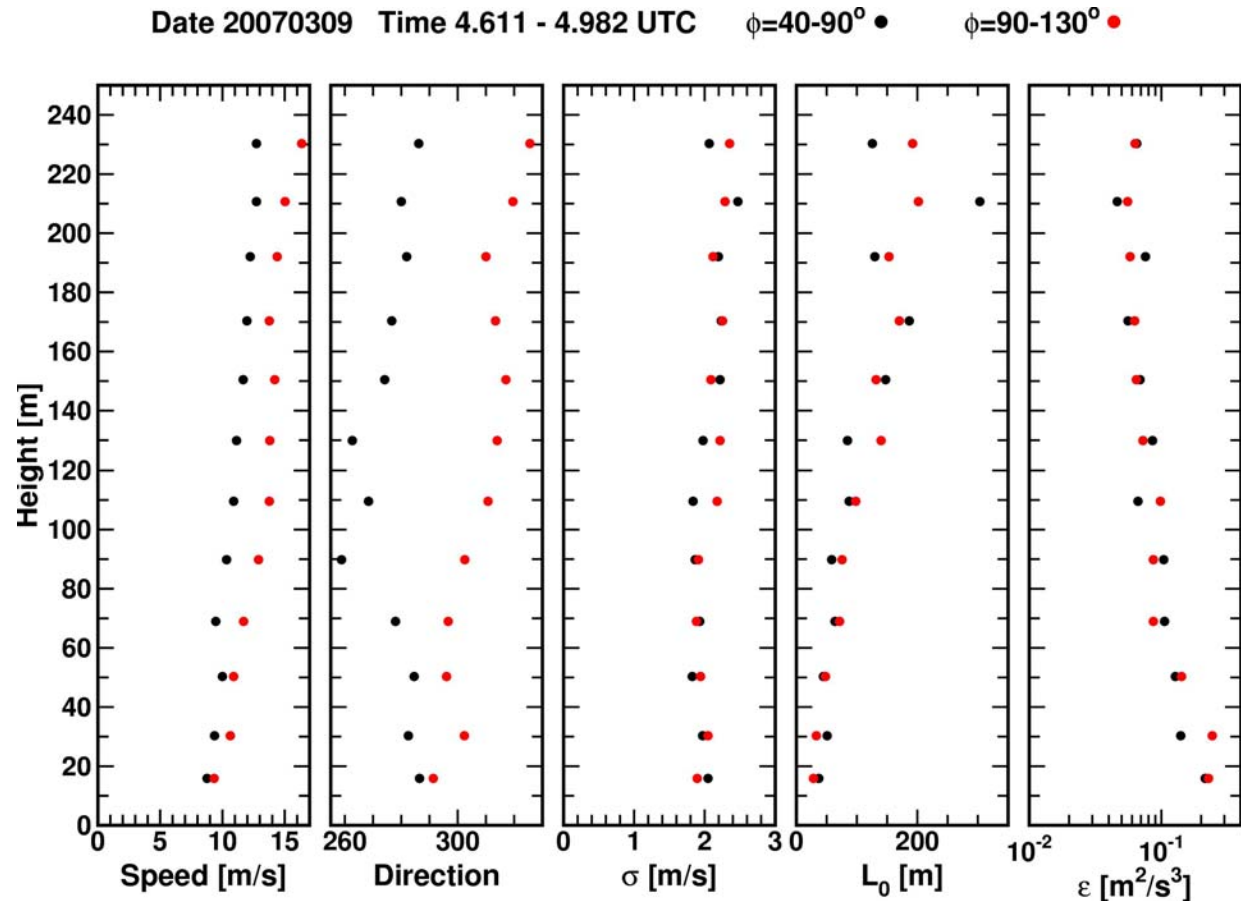
- Large corrections for spatial filtering
- Requires shorter lidar pulse and more accurate corrections
- Critical for lower altitudes

H= 30.24 m WS=4.6027 m/s dir=196.41° index=2
 $\varepsilon=0.40670E-02 \text{ m}^2/\text{s}^3$ $L_0=36.61 \text{ m}$ $\sigma=0.542 \text{ m/s}$



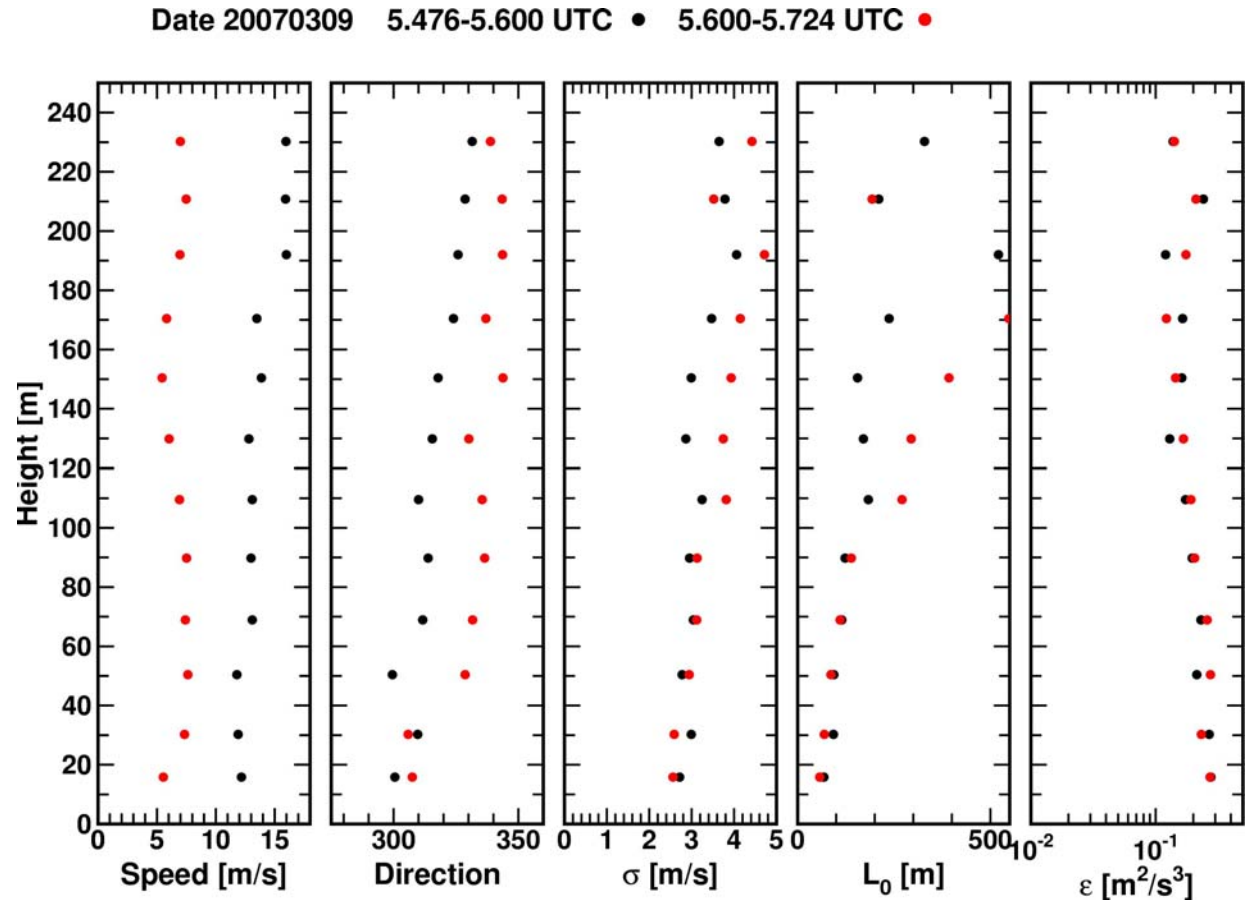
Profiles from Two Angular Sectors

- Differences in wind speed and direction
- Turbulence profiles similar
- Implications for site resource assessment



Rapid Evolution in 7 Minutes

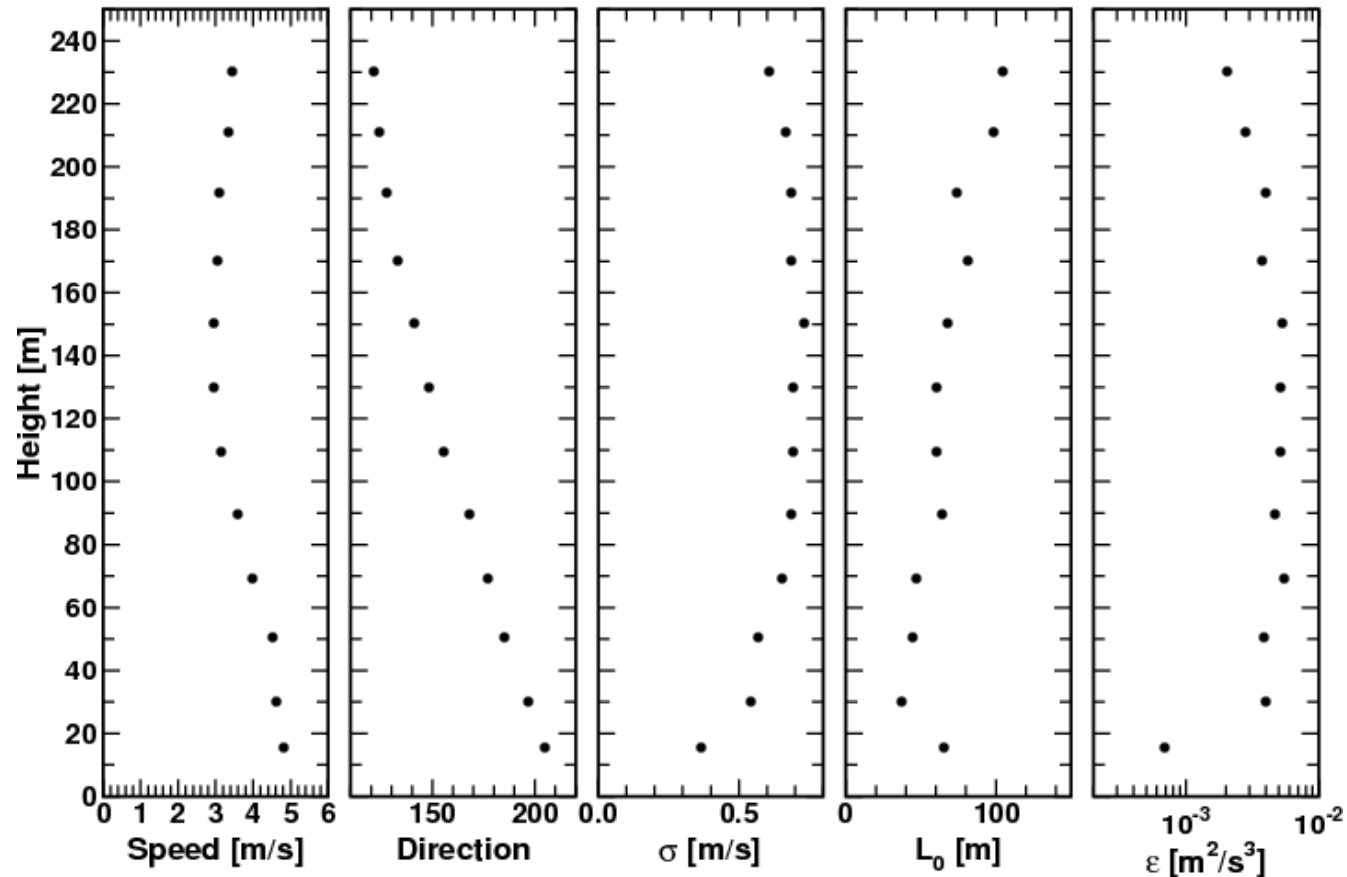
- Rapid change in wind speed
- Turbulence levels are not reduced with lower winds
- 3D scanning required for short time averages



Directional Shear

Date 20070310 Start Time UTC 6.621 End Time UTC 6.744

- Large shear in wind direction
- Typically at night with light winds
- More data required for wind energy applications



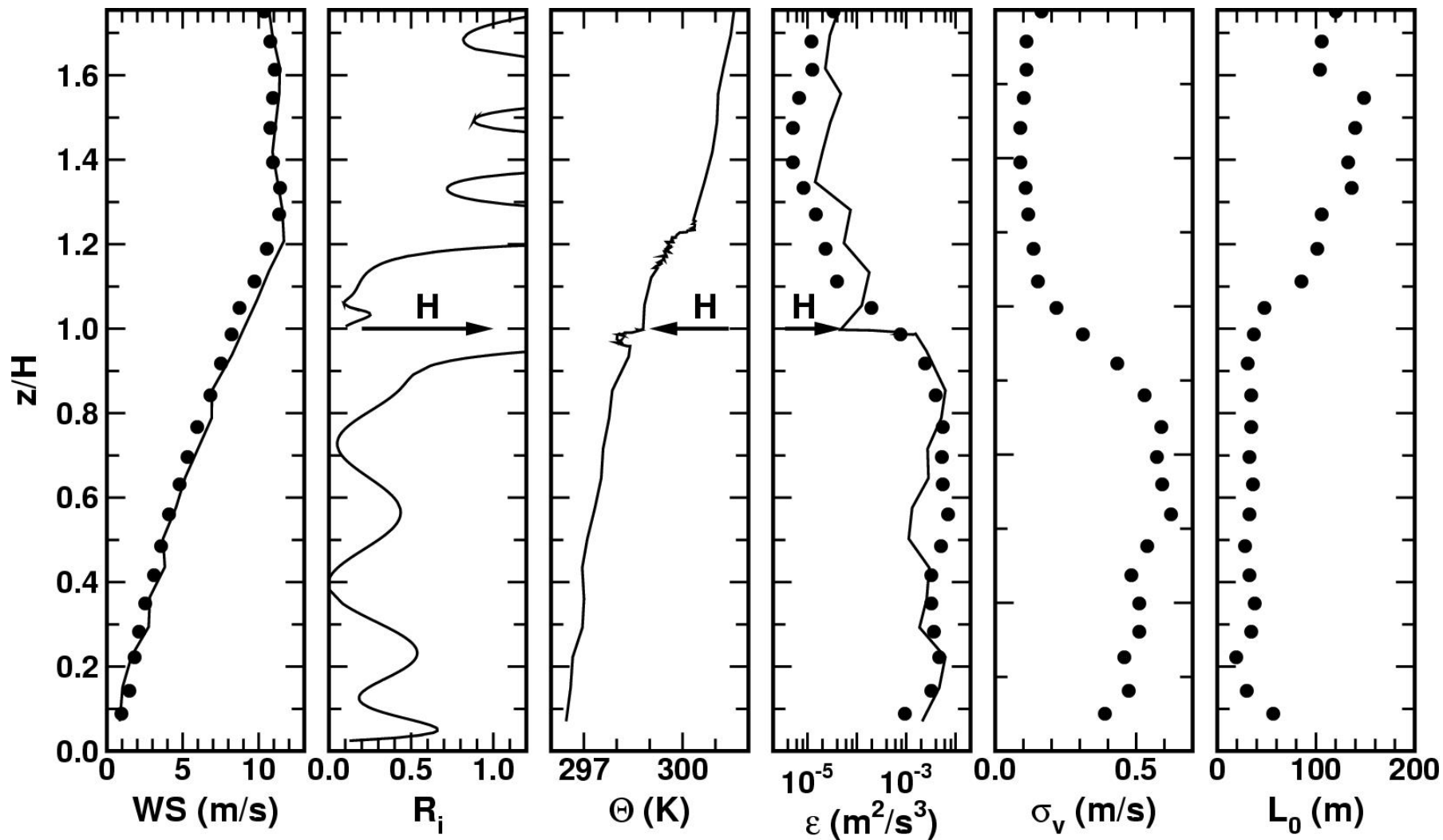
Future Work

- **Optimize Lidar design, signal processing, and scanning patterns**
- **Determine universal description of turbulence for better turbulence estimates (anisotropy?)**
- **Extend spatial filter correction to two dimensions for faster scanning and larger maximum range**
- **Improve algorithms for large length scale L_0 (relax Cartesian approximation)**
- **More data required, especially for wind energy research**

Lafayette Campaign

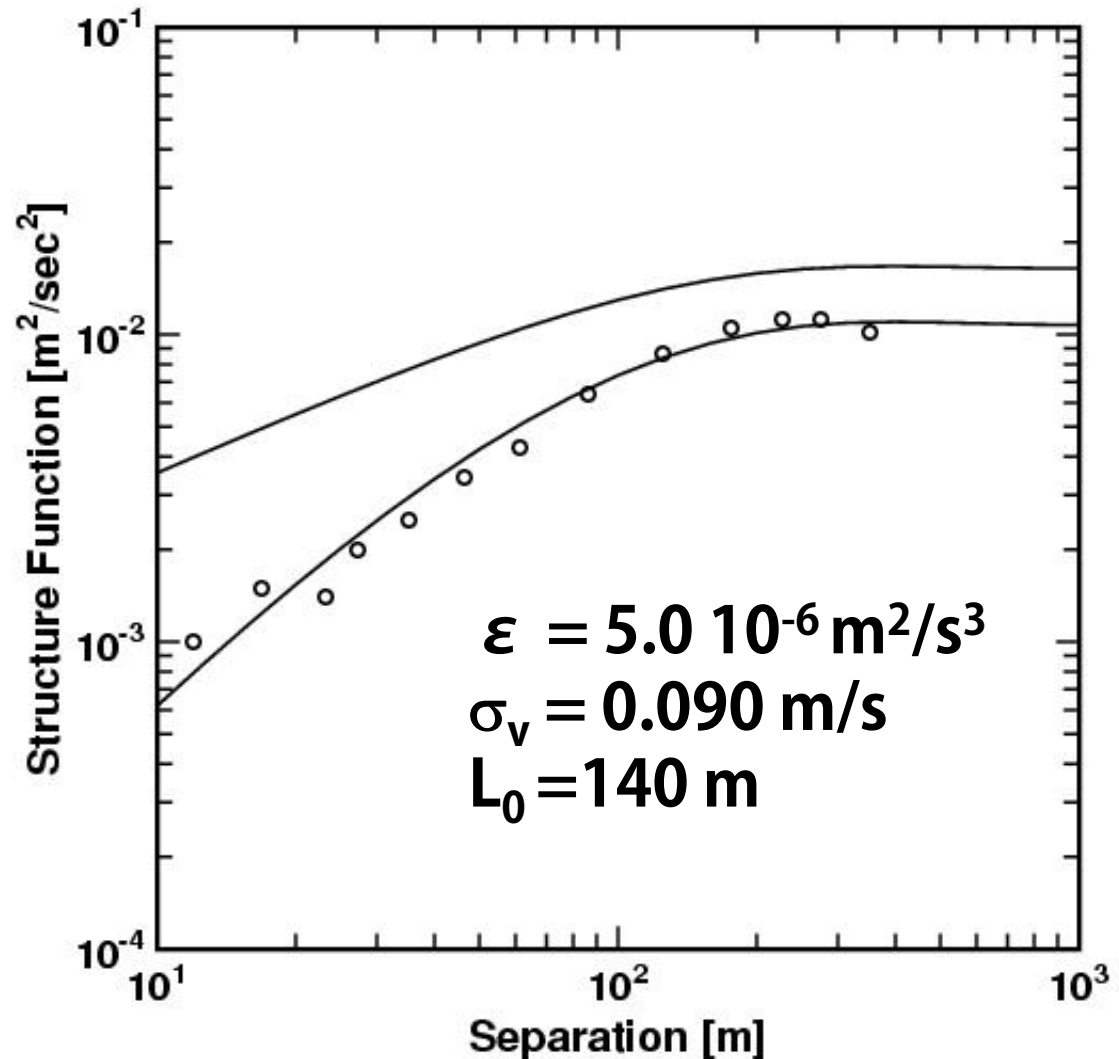


LIDAR and TLS (Blimp)

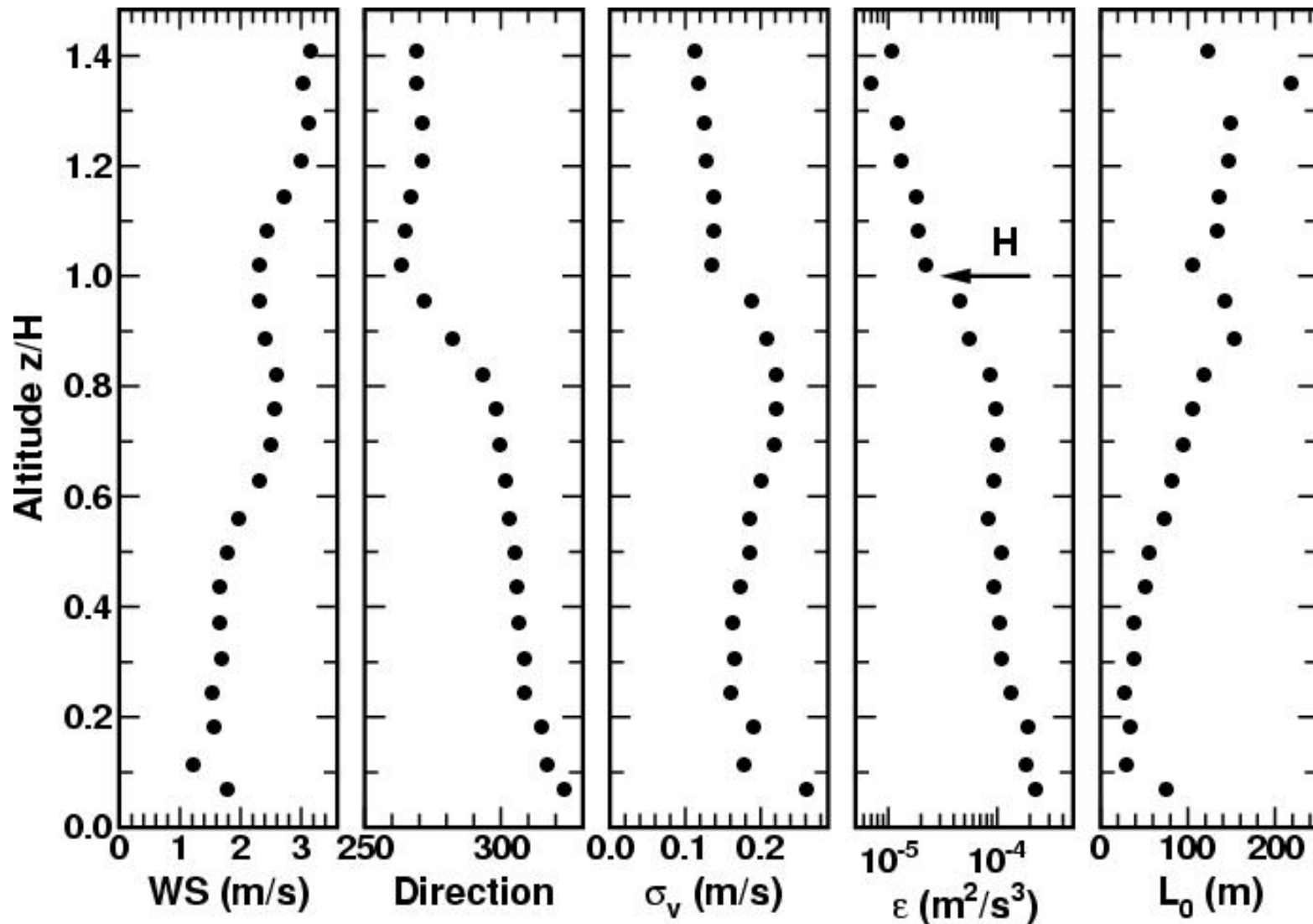


Low Turbulence Data

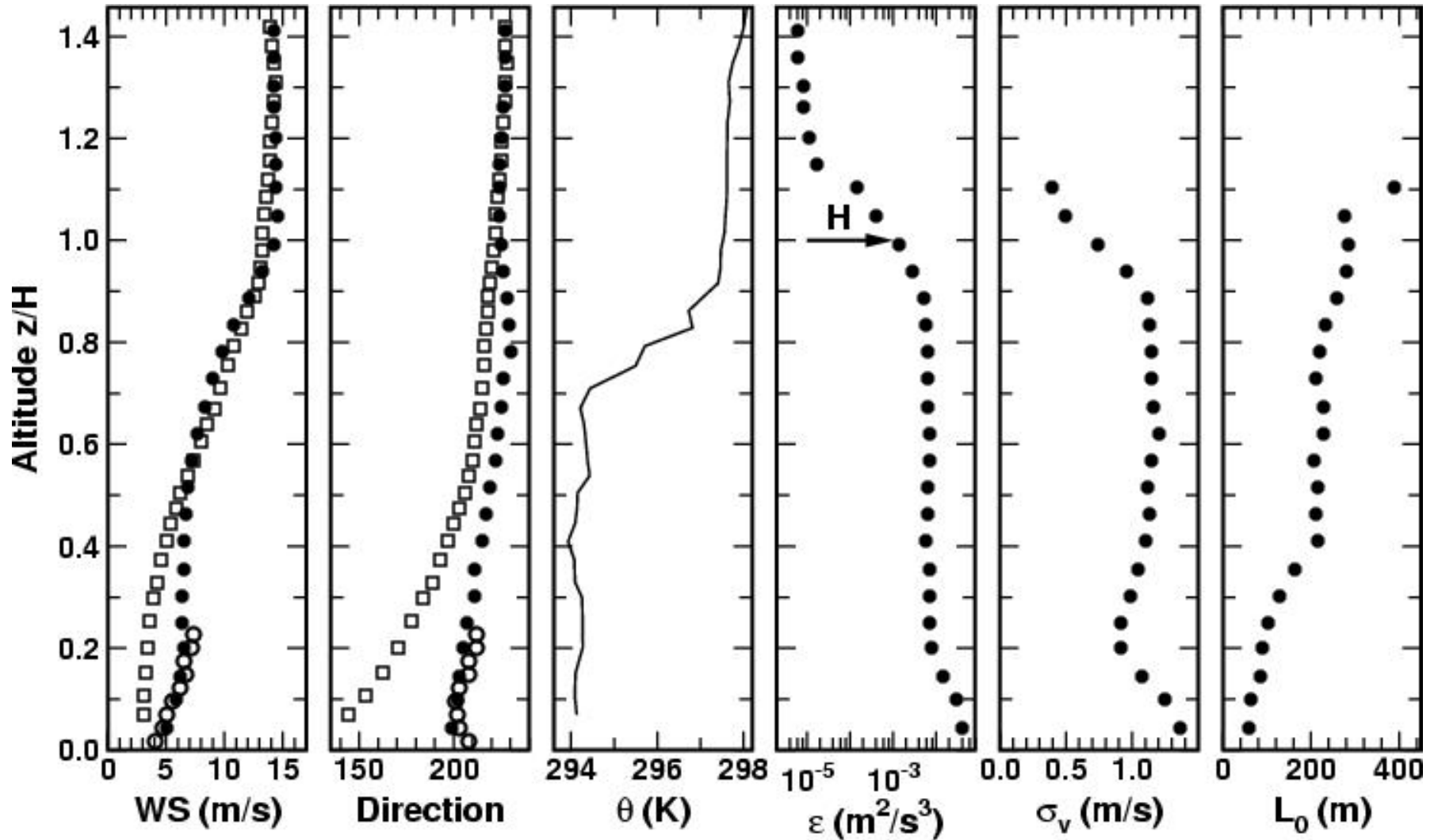
- Accurate corrections for pulse filtering required
- Correct turbulence model for spatial statistics



Low Turbulence Conditions



Convection

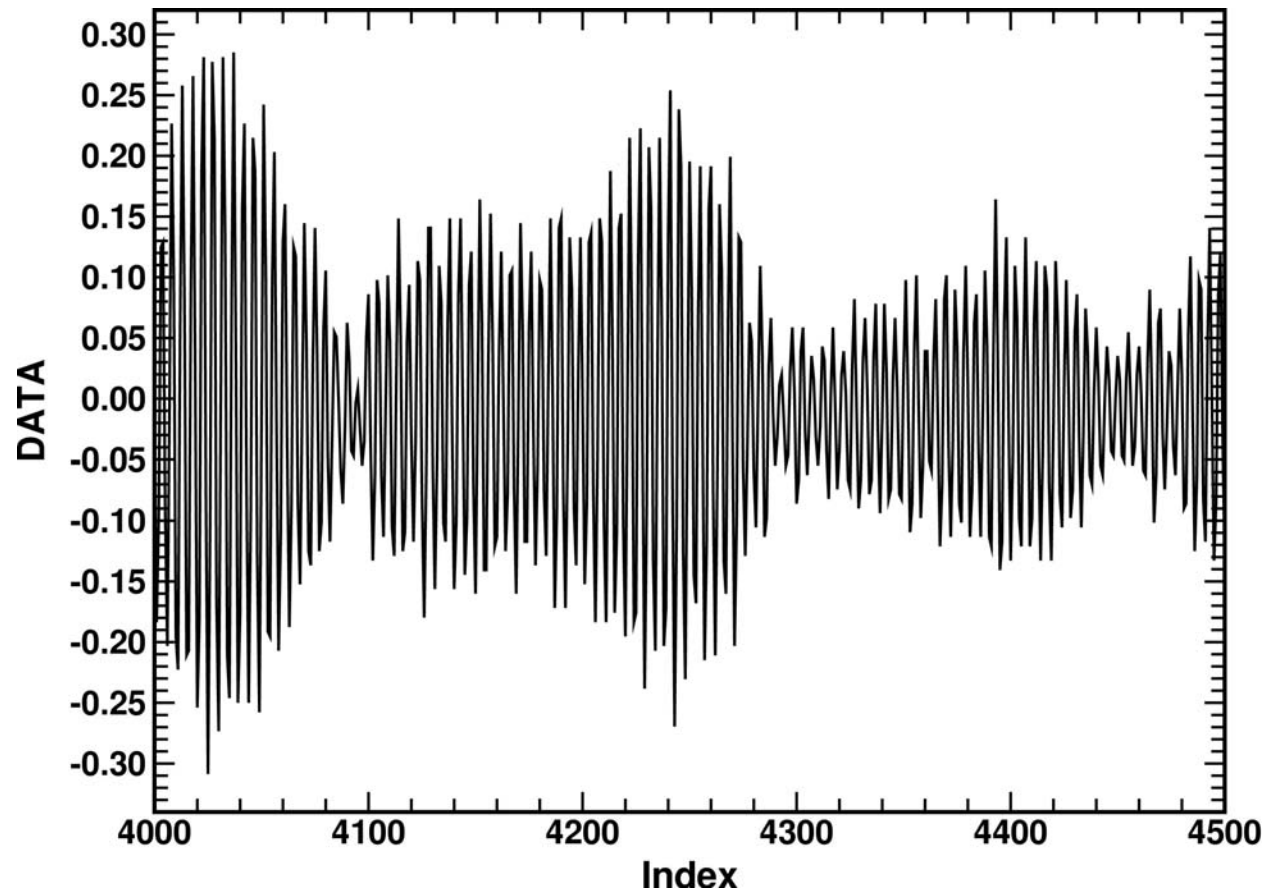


Coherent Doppler Lidar Properties

- **Direct measurement of Doppler shift from aerosol particles**
- **Doppler shift 1 MHz for 1 m/s (2 μm)**
- **Accurate radial velocity estimates with little bias**
- **Most sensitive detection method**
- **Immune to background light**
- **Eye safe operation**

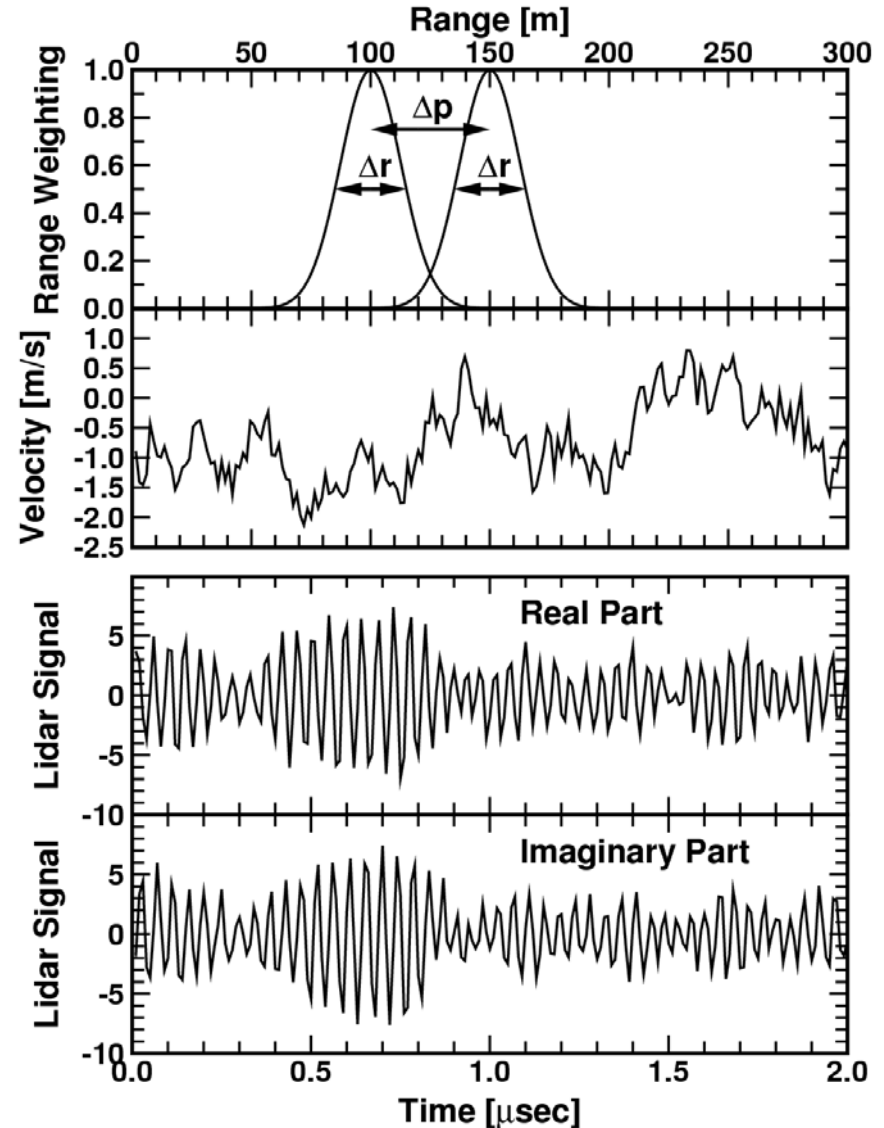
Atmospheric LIDAR Data

- Lidar signal is a narrow band Gaussian random process
- Simple statistical description for constant velocity and aerosol backscatter



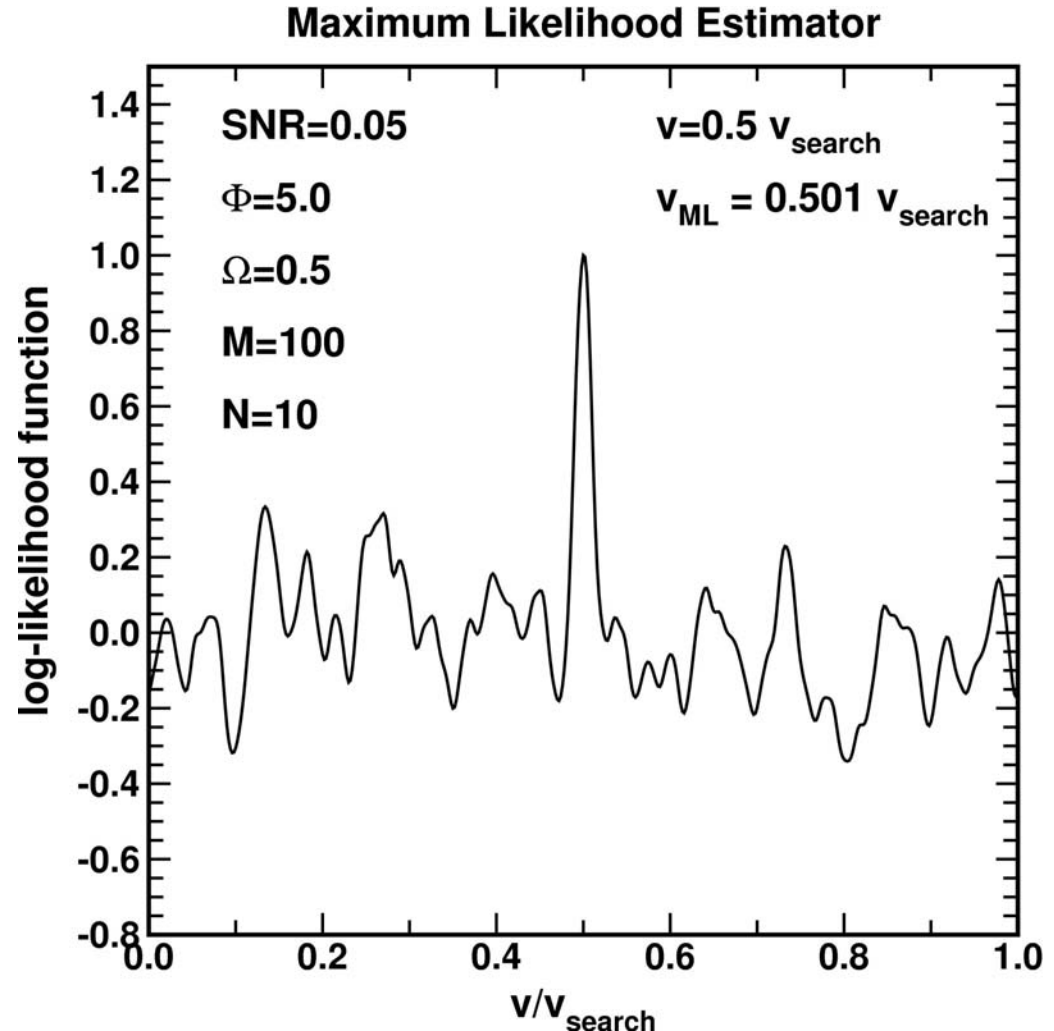
Atmospheric LIDAR Data

- Lidar signal
- Random velocity
- Pulse weighting
- Range gate defined by processing interval



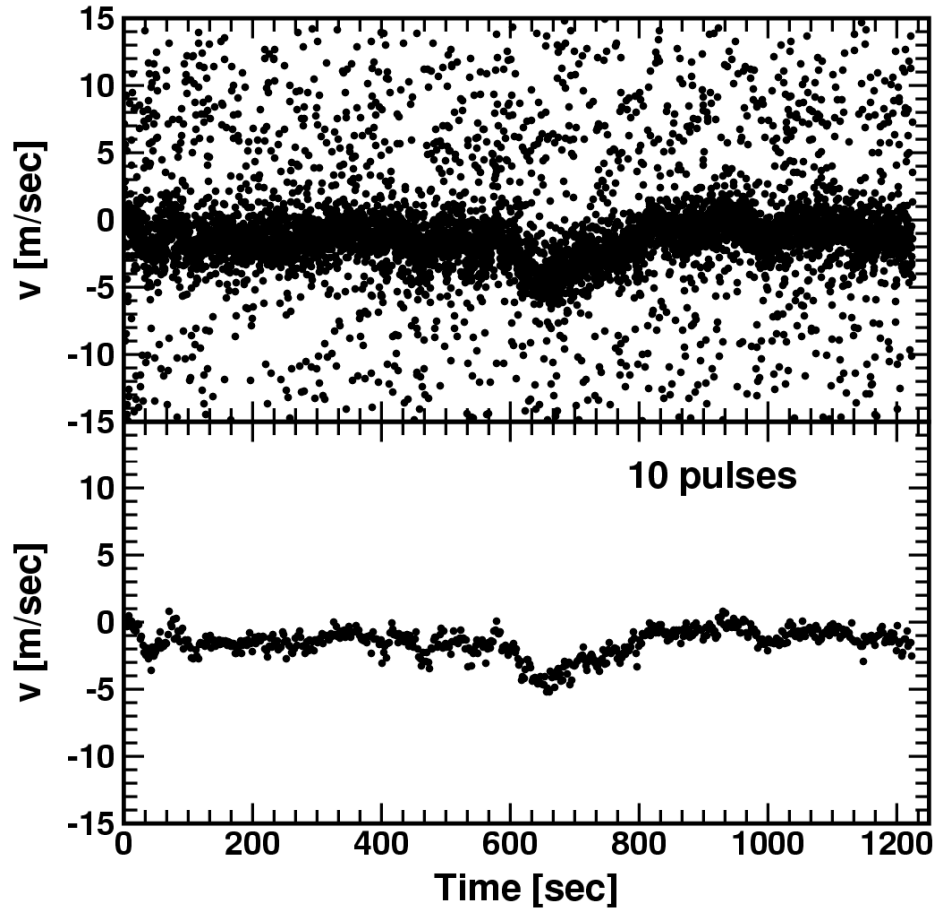
Estimation of Velocity

- Data from multiple pulses
N improves performance
- Spectral based estimators
- Maximum Likelihood has best performance



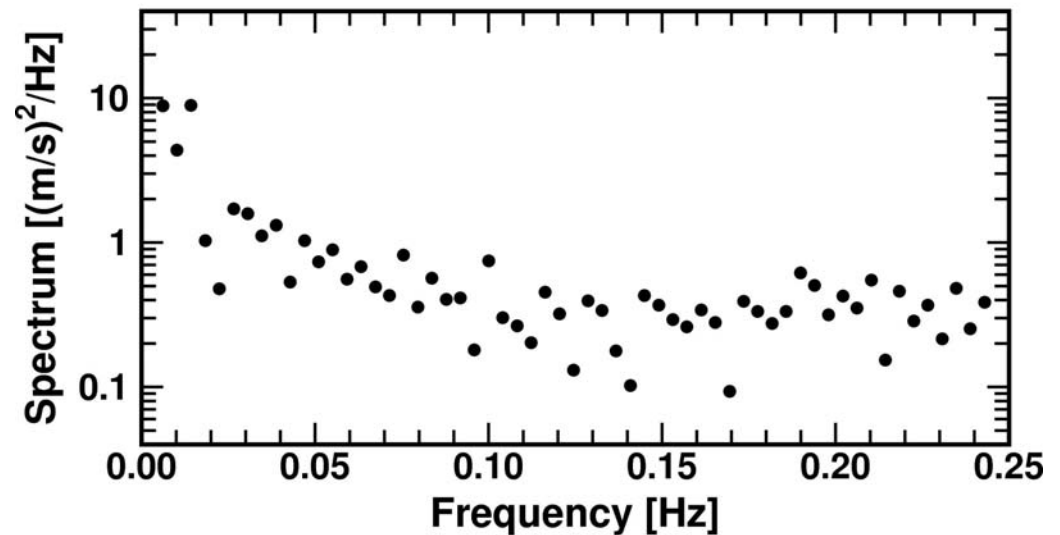
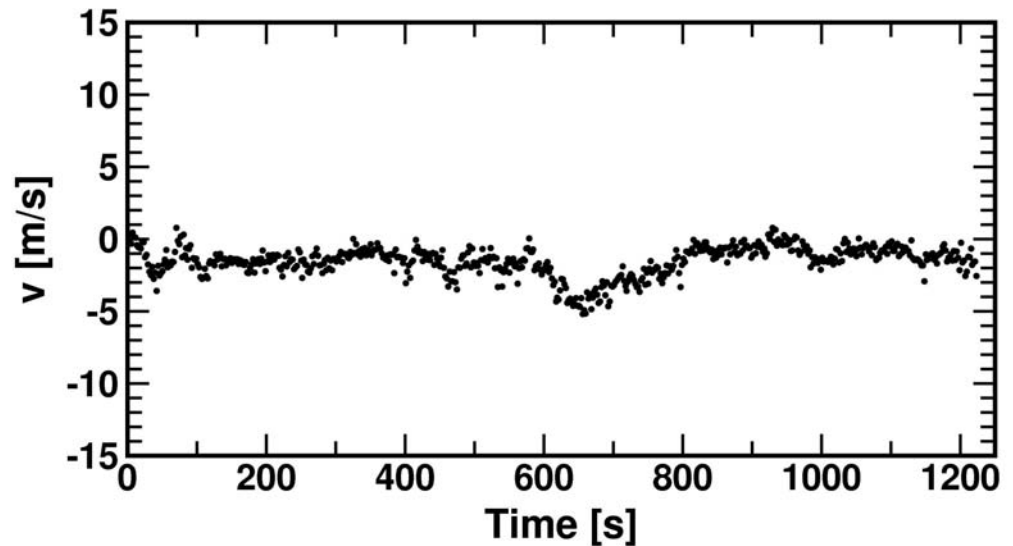
Multiple Pulse Estimates

- **Single pulse data has random outliers**
- **Pulse accumulation removes outliers**
- **Temporal resolution reduced**



Estimates of Random Error-cont.

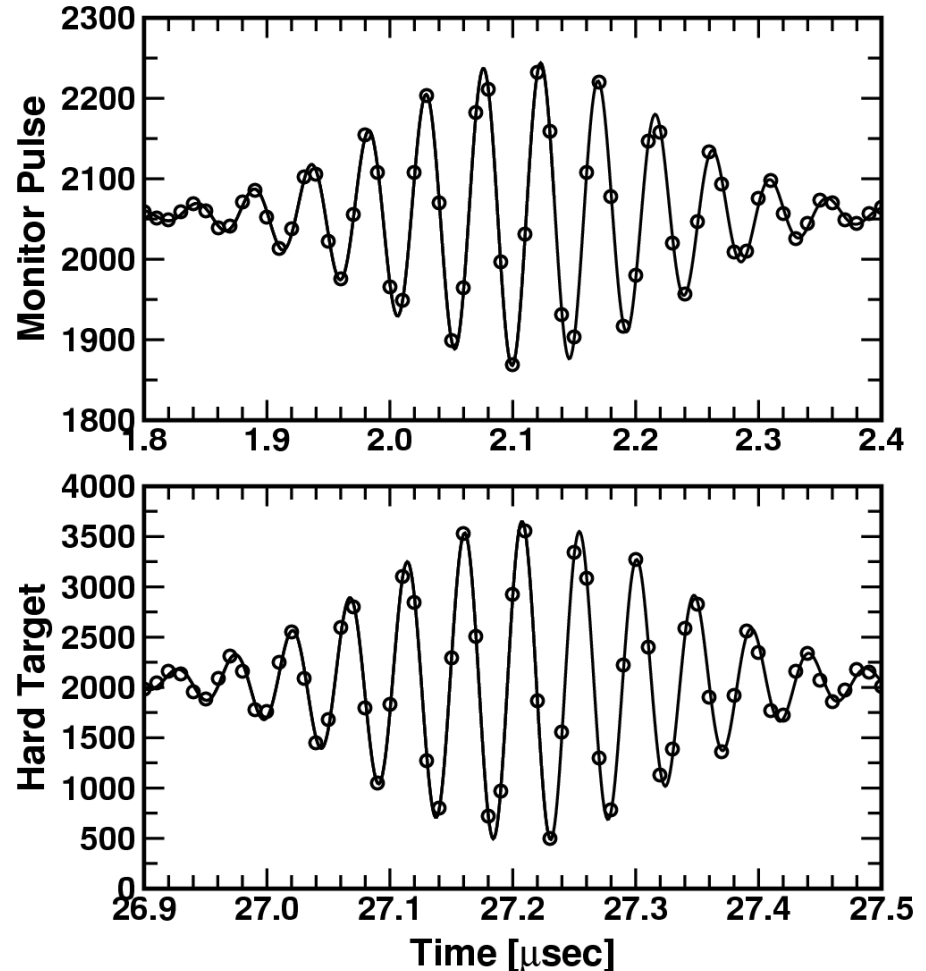
- Multiple pulse data has a smaller region for the noise floor
- The atmospheric signal must have low frequency content



Hard Target Data

- **Velocity bias determined from hard target data**
- **Bias is typically less than 2 cm/s**

2 μ m Lidar Data from Coherent Technologies, Inc.



Verification of Accuracy

- **Velocity random error depends on signal energy**
- **Accuracy is very good**
- **Agrees with theoretical predictions if turbulence is included**

