

Feedbacks between moisture, cumulus convection and large-scale circulations over the tropical oceans

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...with help from Peter Blossey, Marat Khairoutdinov, and others

What makes tropical dynamics unique?

Moist convection!

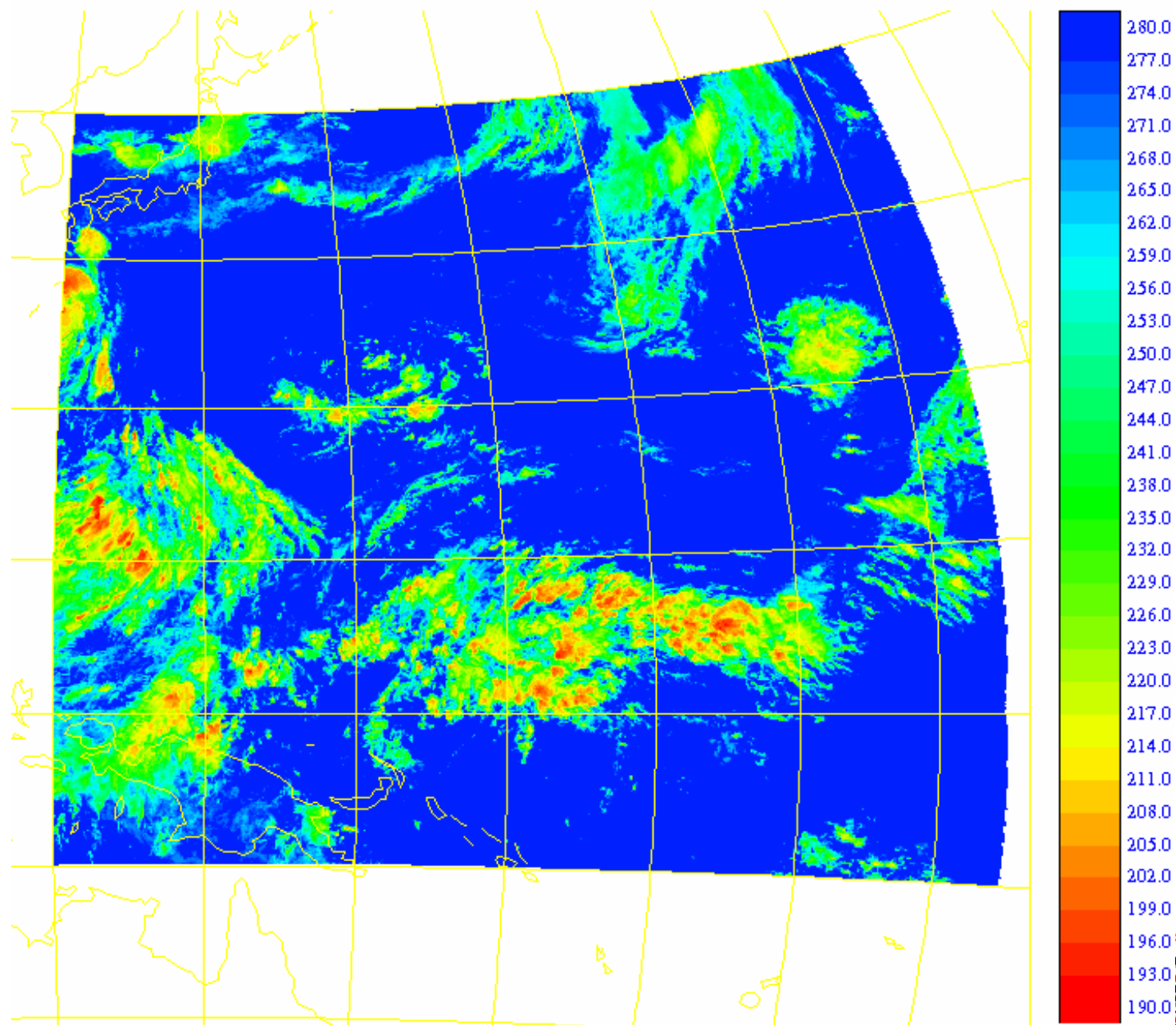
- Heat engine of large-scale circulations (rainfall) .
- Determines tropical thermal stratification.
- Tightly connected to water vapor, clouds, radiation.
- Scale interaction
- Strong 2-way link to SST and land surface properties.

This talk

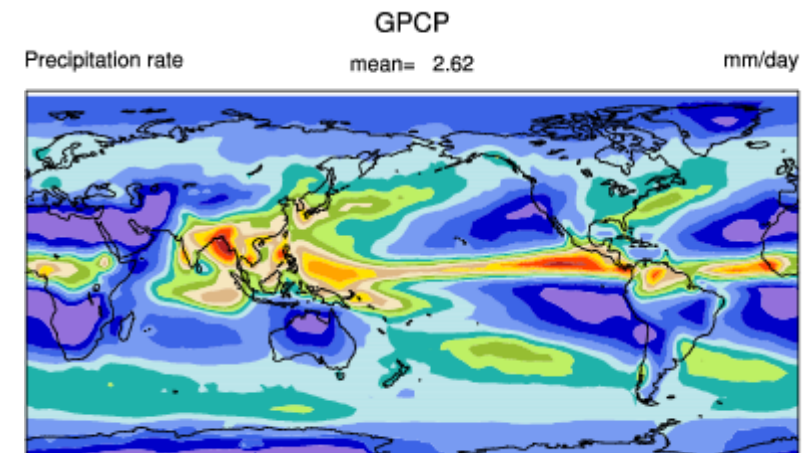
Role of feedbacks between convection and water vapor in organizing large-scale tropical circulations in a CRM.

- Convective self-aggregation over uniform SST
- Mock-Walker circulation

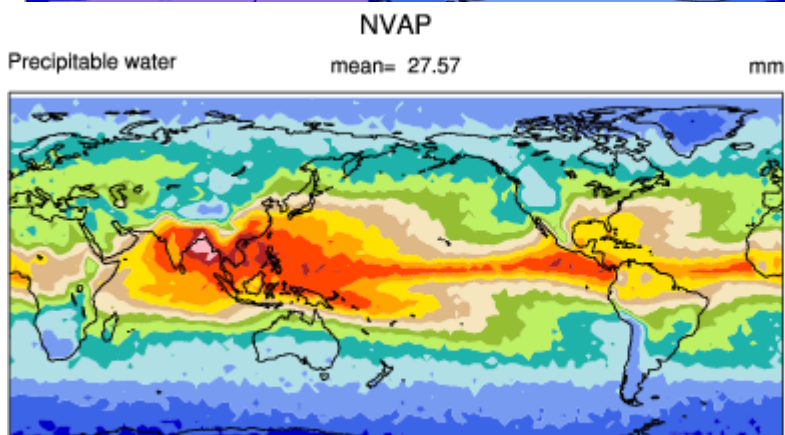
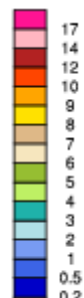
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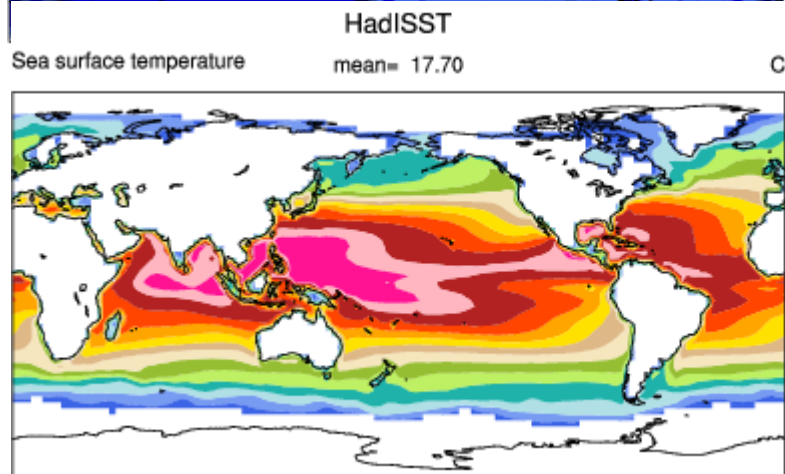
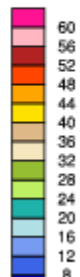
Mean rainfall-humidity correlations (JJA mean)



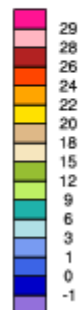
Min = 0.00 Max = 14.24



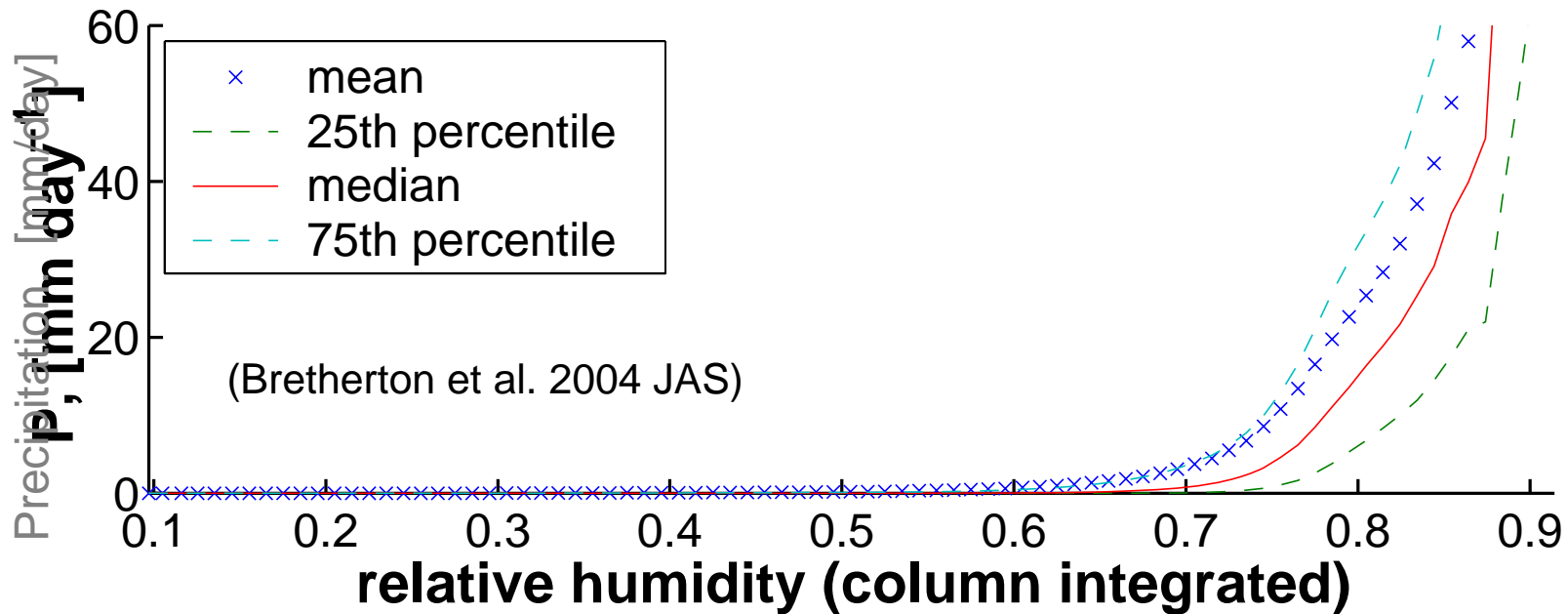
Min = 4.54 Max = 58.42



Min = 0.00 Max = 29.60



Strong SSM/I observed rainfall-humidity correlation on daily timescales as well



Radiative-Convective Equilibrium

A traditional 1D perspective on the atmospheric structure of the deep tropics and its response to climate forcings (e. g. Manabe and Strickler 1964).

- Uniform insolation.
- No ambient rotation.
- Uniform surface (e. g. constant SST or zero-flux).

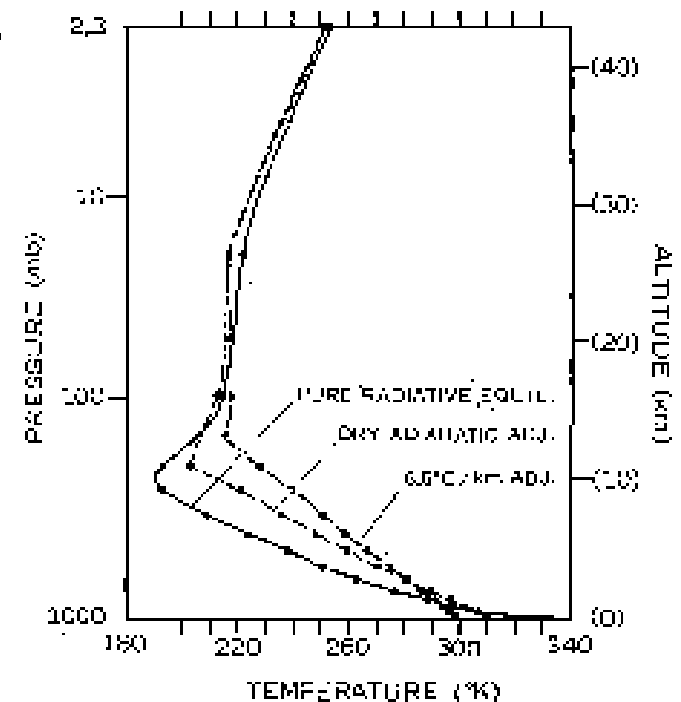
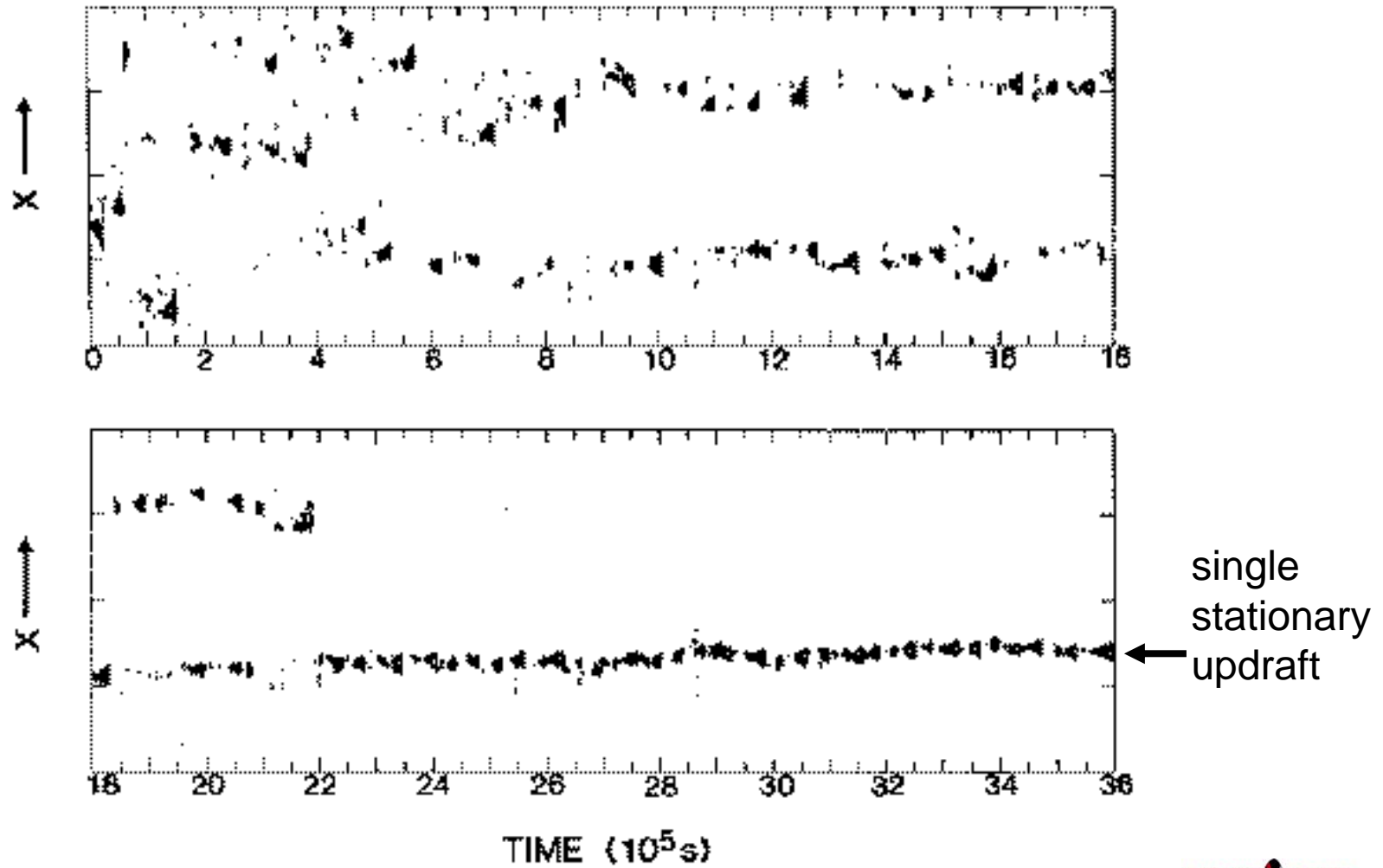


FIG. 4. The dashed, dotted, and solid lines show the thermal equilibrium with a critical lapse rate of 6.5 deg km^{-1} , a dry-adiabatic critical lapse rate (10 deg km^{-1}), and pure radiative equilibrium.

2D domain RCE simulation

(Held et al. 1993, $A = 640$ km, $\Delta x = 5$ km, zero mean wind)



(Held et al. 1993)

FIG. 4. Precipitation as a function of time and x in the case in which the mean wind is constrained to vanish.

Imposed weak $1 \text{ m s}^{-1} \text{ km}^{-1}$ mean vertical shear over lowest 5 km destroys organization by shearing out moist anomaly.

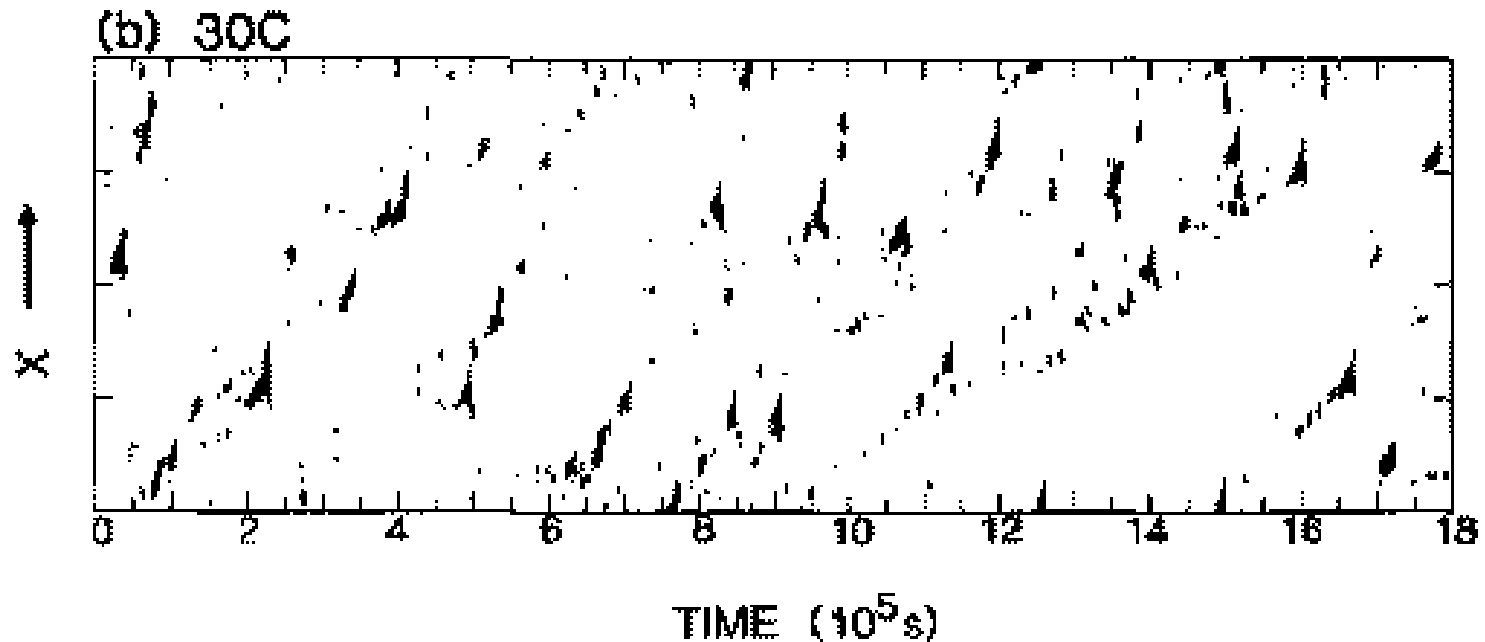
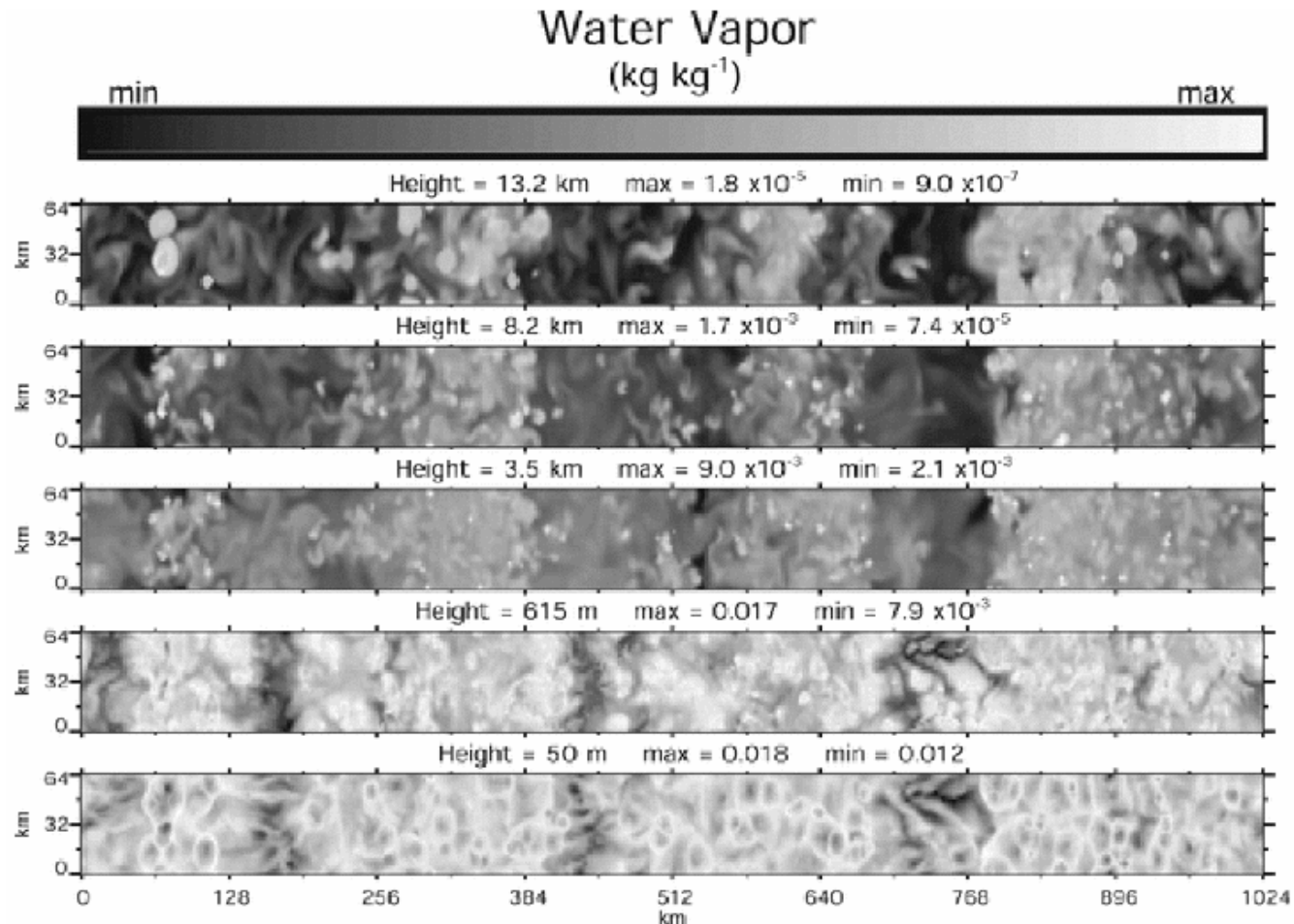


FIG. 7. Precipitation as a function of time and x in the case with a prescribed mean shear: (a) 25°C and (b) 30°C .

“We are convinced that it is the moisture field, rather than the large-scale low-level convergence pattern, that gives the ‘wet spot’ its memory”. (Held et al. 1993)

Tompkins (2001, JAS)

- 1024x64 km domain, $\Delta x = 2$ km. Specified radiation, interactive surface fluxes. Convective feedback on mean shear was enabled, but mean winds did not build up. Self-aggregation in $O(10)$ days).



(Day 15)

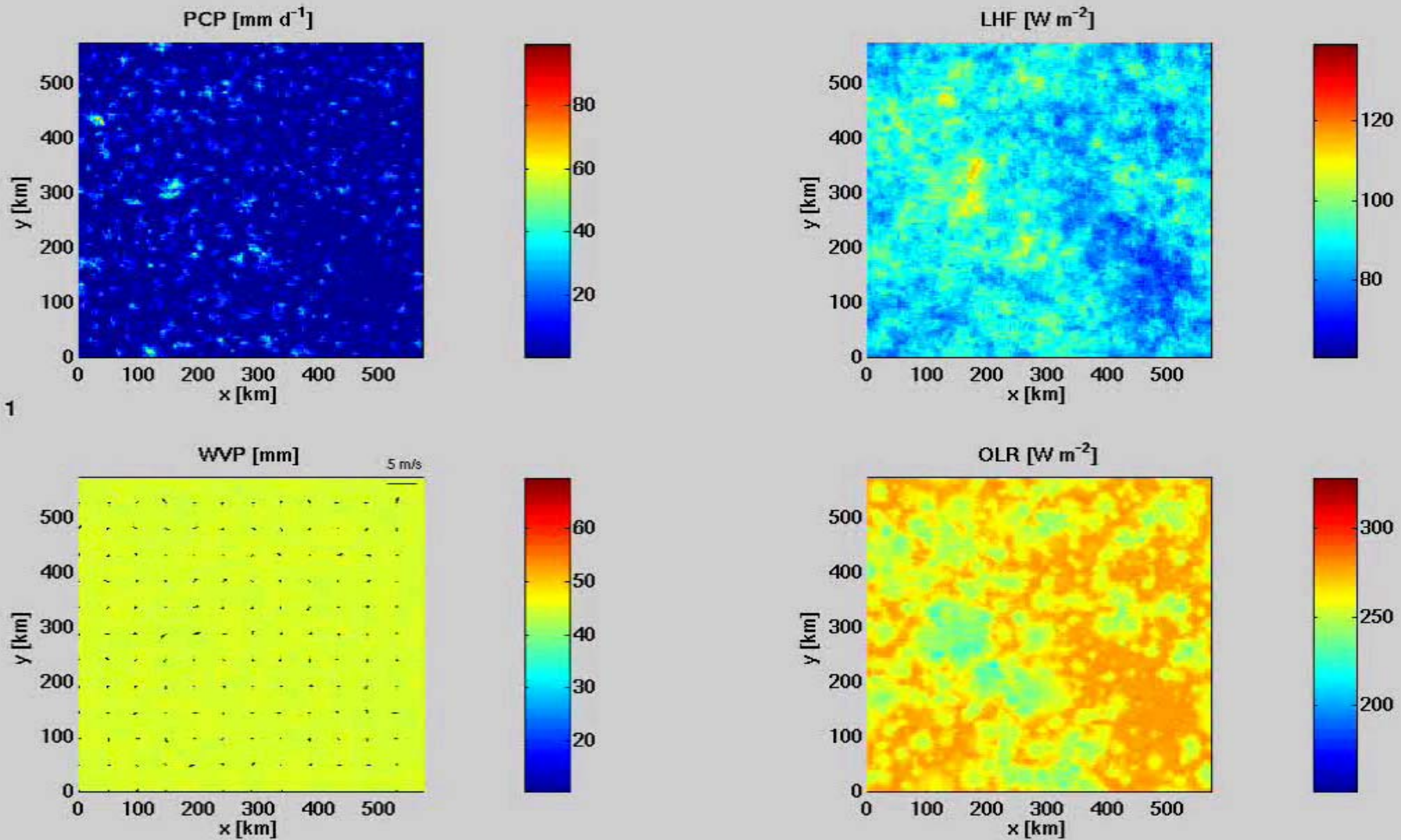
Self-aggregation over 576x576 km domain

(Bretherton et al. 2005 JAS)

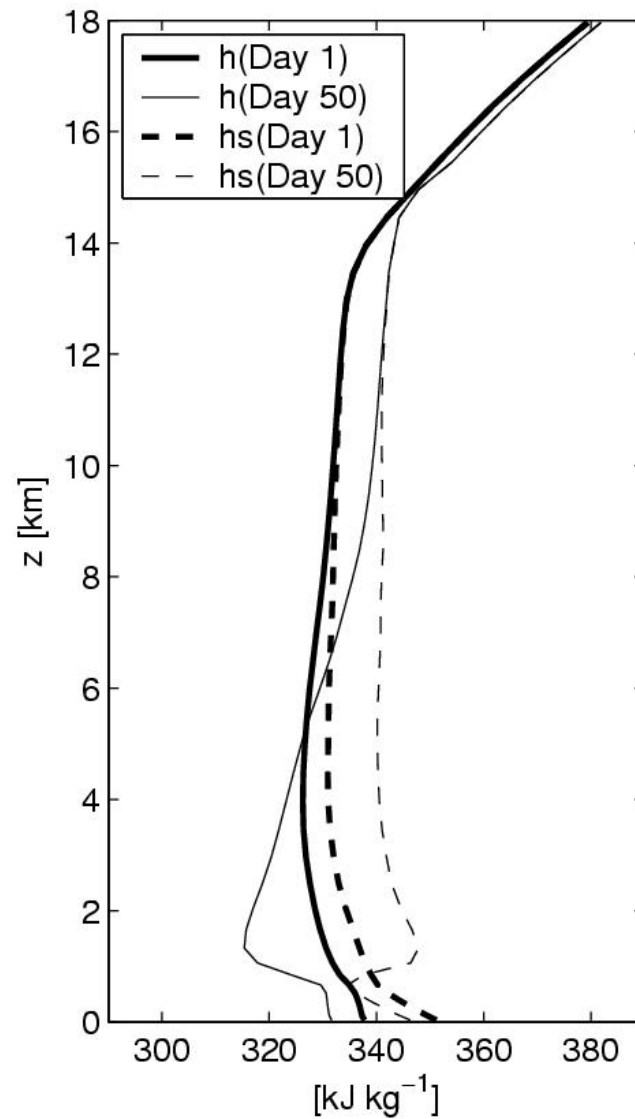
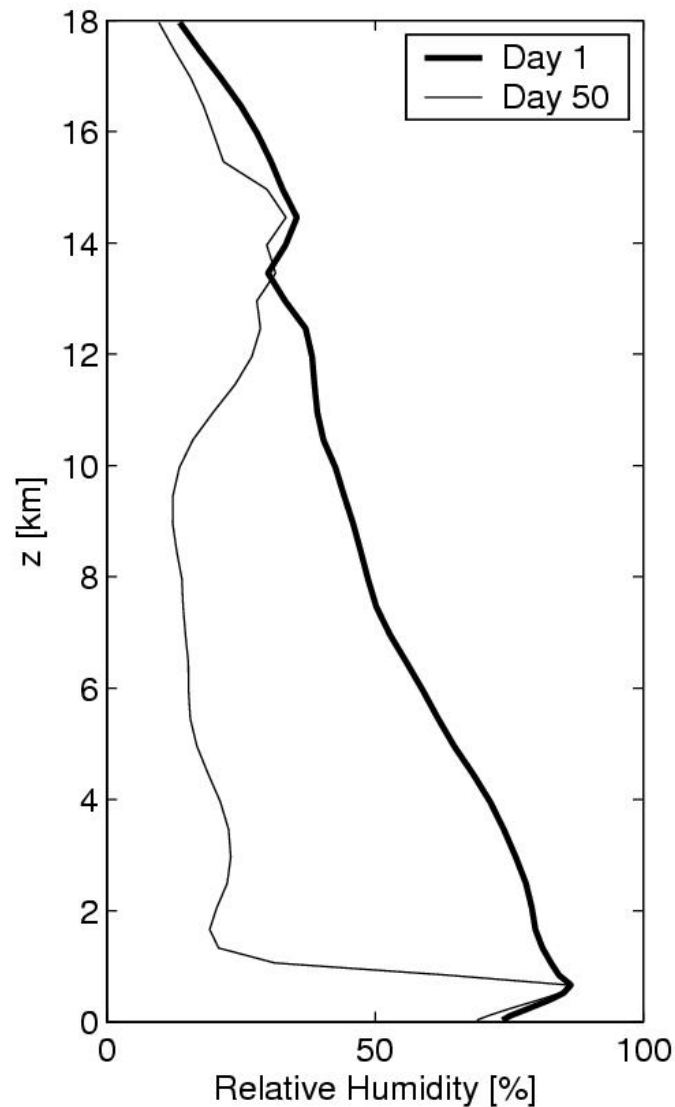
Spatially uniform RCE over constant SST appears to be unstable to ‘self-aggregation instability’ on quasi-2D domains. Also on fully 3D domain? Theoretical model?

- SAM6.1 CRM (Khairoutdinov and Randall 1993)
- Doubly periodic, $\Delta x = 3$ km, 64 vertical levels
- No initial mean wind, CMT affects mean flow.
- Interactive surface fluxes and radiation.
- First run ‘small-domain’ 96x96 km 301 K RCE simulation to steady state (popcorn convection, no aggregation).
- Tile onto the large domain, add random perturbations, integrate 100 days.

100 days of self-aggregation

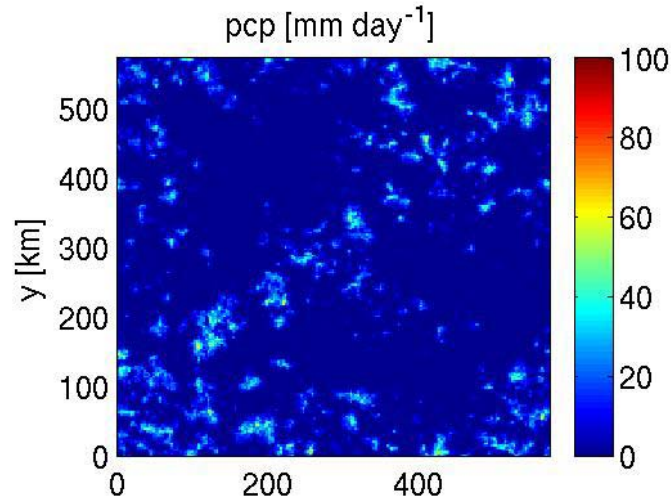


Mean sounding profoundly dries and warms

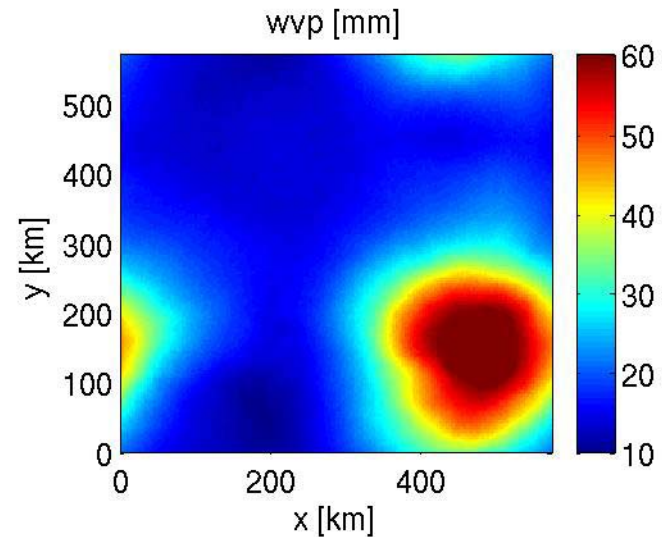
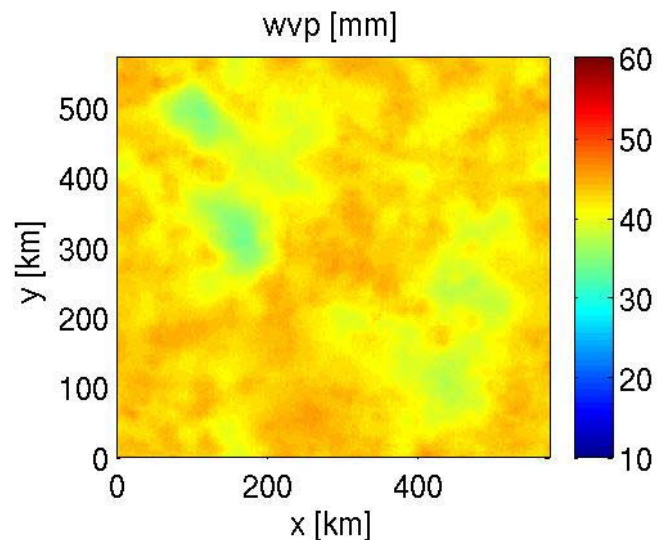
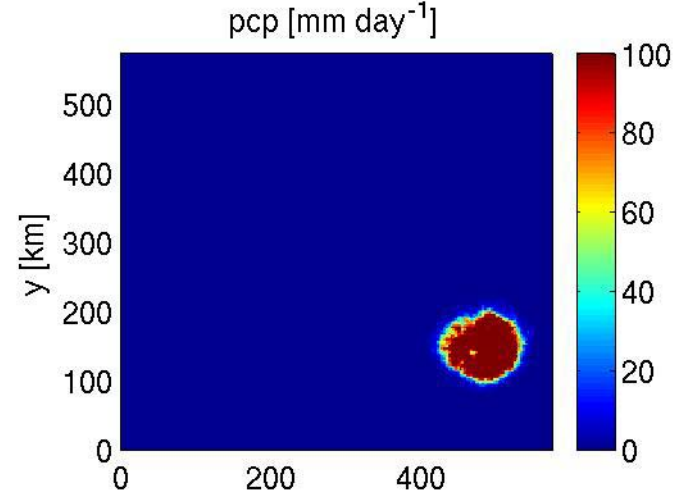


...so how does self-aggregation 'instability' happen?

Day 6 avg.
incipient self-aggregation



Day 50 avg.
One convective center



Moist static energy budget analysis of self-aggregation

- Use daily horiz. averages over 72x72 km subdomains (space-time averaging on sub-aggregation scale)
- Use subdomain tropospheric column-integrated '<>' budgets of moist static energy $h = c_p T + Lq + gz$ [- $L_f q_i$] to understand self-aggregation feedbacks.

$$\begin{aligned} d\langle s \rangle / dt &= LP + SHF - \Delta R - \langle \nabla \cdot (\mathbf{u}s) \rangle \\ + d\langle Lq \rangle / dt &= -LP + LHF - \langle \nabla \cdot (\mathbf{u}q) \rangle \end{aligned}$$

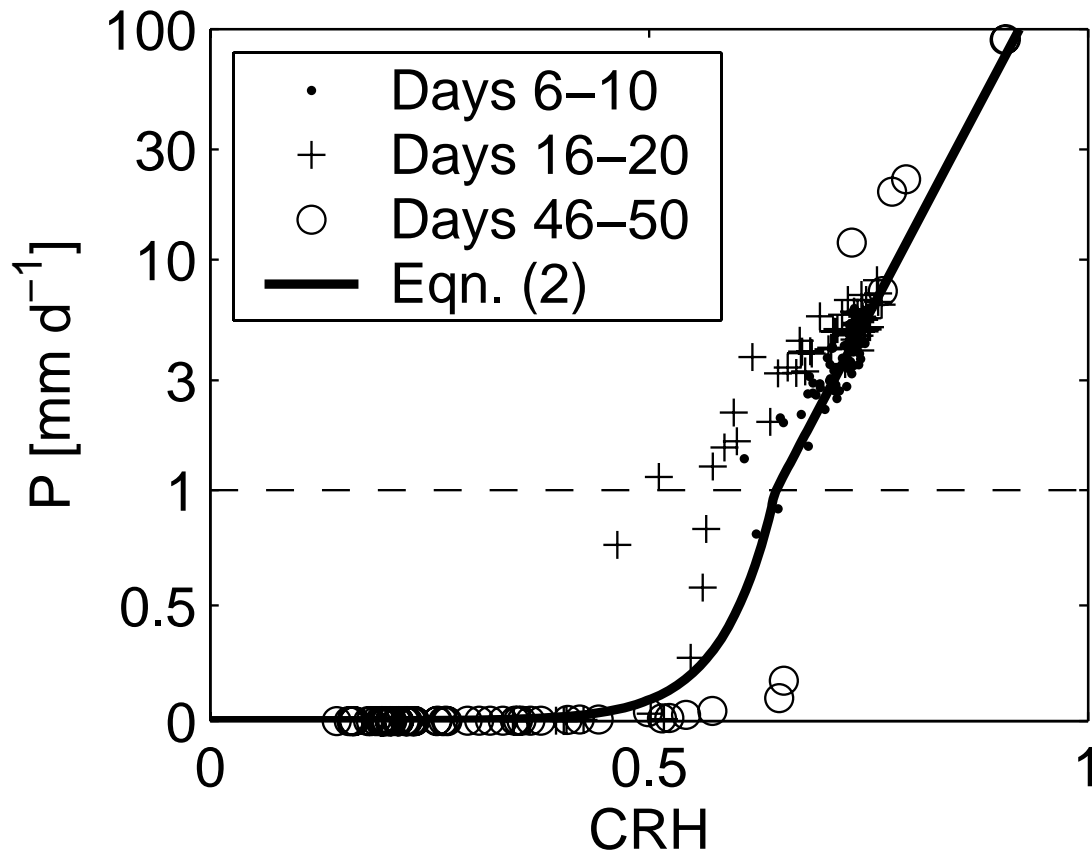
$$d\langle h \rangle / dt = THF - \Delta R - \langle \nabla \cdot (\mathbf{u}h) \rangle$$

$\langle h \rangle$ is used so we can moist convective rainfall (LP) as response to external forcing (so don't want LP on RHS).

- Horizontal T variations ($'$) small, so $\langle h \rangle' \approx \langle Lq \rangle' = LW'$, where W is water vapor path.
- Self-aggregation if $d\langle h \rangle / dt$ positively correlated to $\langle h \rangle$, so moist regions get moister and dry regions get drier.

Moister blocks precipitate more

Define 'column relative humidity' $r = W/W_{\text{sat}}$. Then...



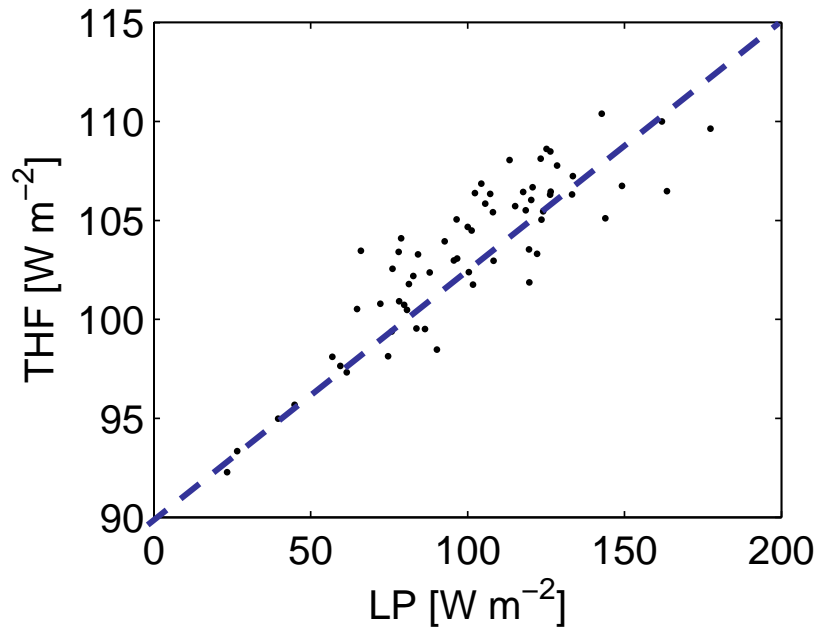
$$P \approx P_{\text{RCE}} \exp(a_m[r - r_{\text{RCE}}]),$$
$$P_{\text{RCE}} = 3.5 \text{ mm d}^{-1},$$
$$a_m = 16.6,$$
$$r_{\text{RCE}} = 0.72.$$

(Bretherton et al. 2005)

(Relationship depends slightly on evolving T profile)
...similar relationship observed over tropical oceans
on daily timescales (Bretherton et al. 2004)

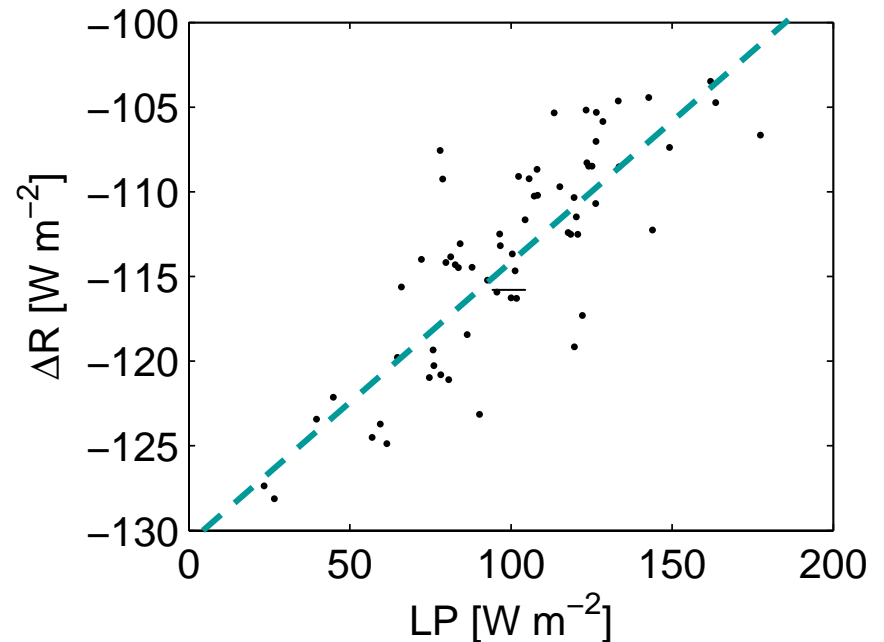
Convection influences diabatic forcing

Gustiness (cold pools)



$$d\text{THF}/d\text{LP} = c_S = 0.12$$

Anvil greenhouse

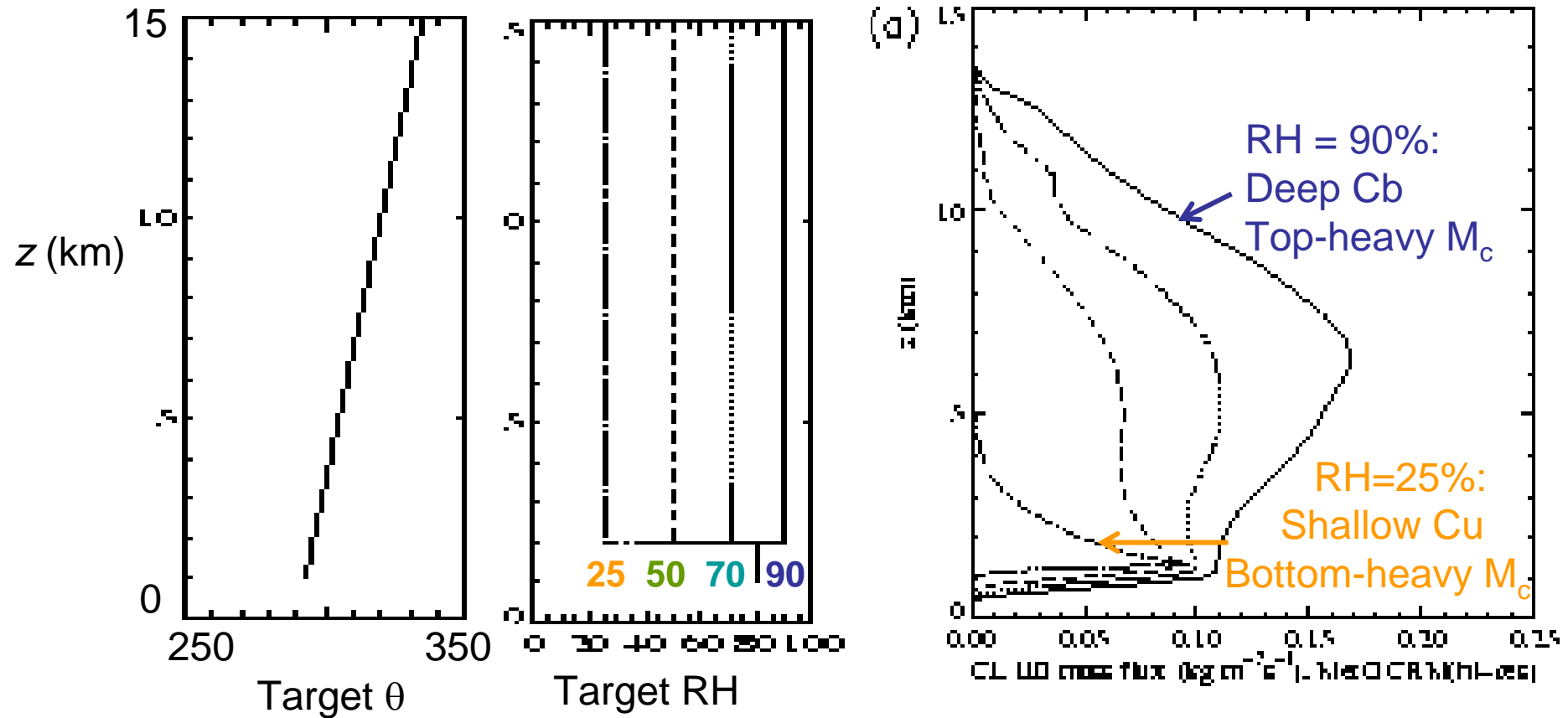


$$d\Delta R/d\text{LP} = c_R = 0.17$$

Cu depths sensitive to lower tropospheric moisture

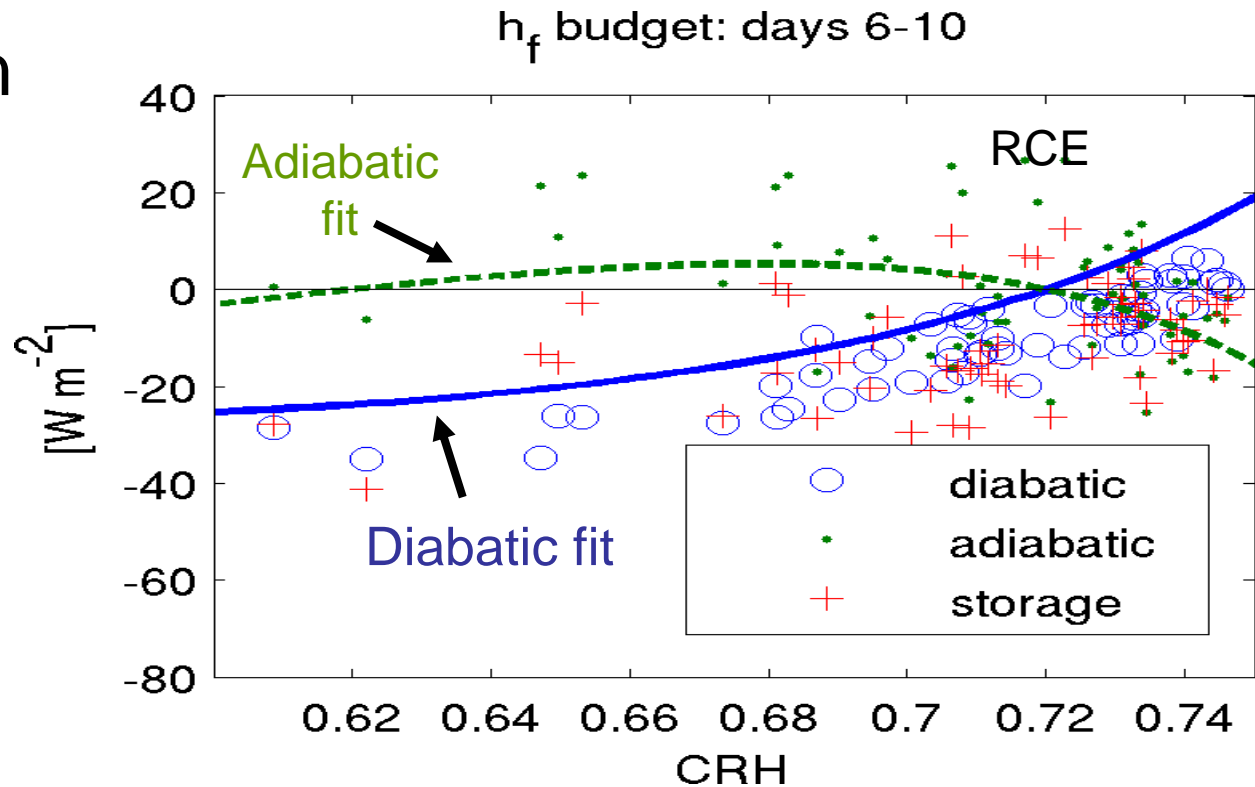
(Derbyshire et al. 2004 QJ)

UKMO CRM

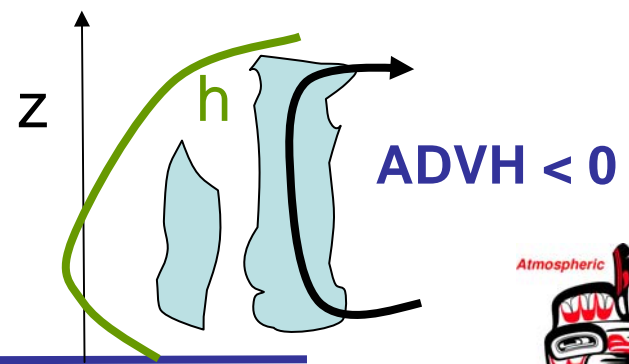
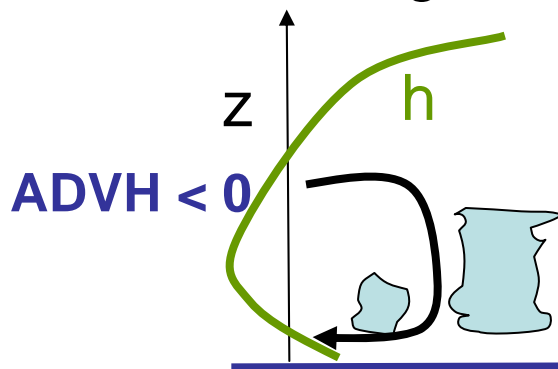


- Most cumuli entrain vigorously ($1-2 \text{ km}^{-1}$).
 - Entrainment of dry air evaporates Cu, steals their buoyancy.
- \Rightarrow Deep Cb require moist environment as well as CAPE.

Advection



$ADVH = - \langle \nabla \cdot (\mathbf{u}h) \rangle = \alpha_h L (P - P_{RCE})(r_h - r)$, $\alpha_h = 1.8$, $r_h = 0.62$
 ...is stabilizing for $r > 0.68$.



A simple MSE-based theory of self-aggregation

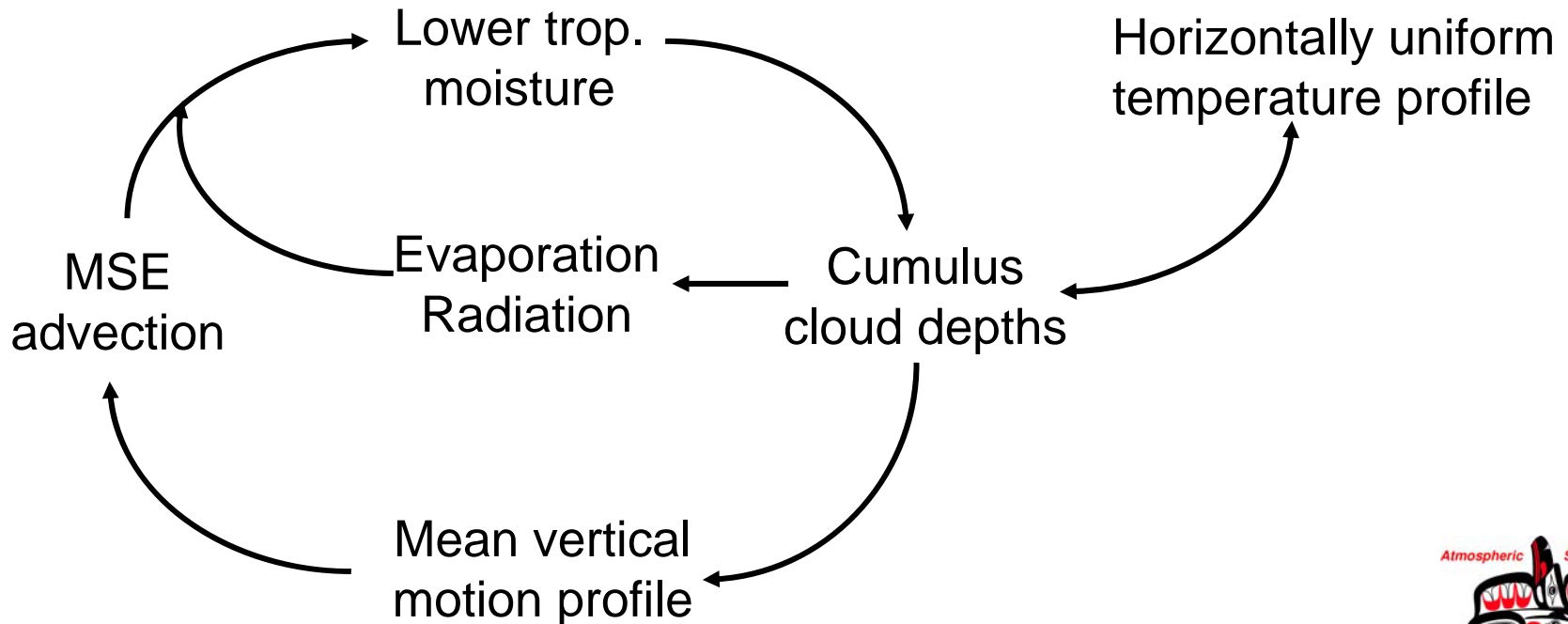
$$d\langle h \rangle / dt = \text{THF} - \Delta R - \langle \nabla \cdot (\mathbf{u}h) \rangle$$

$$\Rightarrow \text{LW}_{\text{sat}} dr/dt = (c_S + c_R) \text{LP}(r) + \text{ADVH}(r, P(r)) [+ \text{Noise}(t)]$$

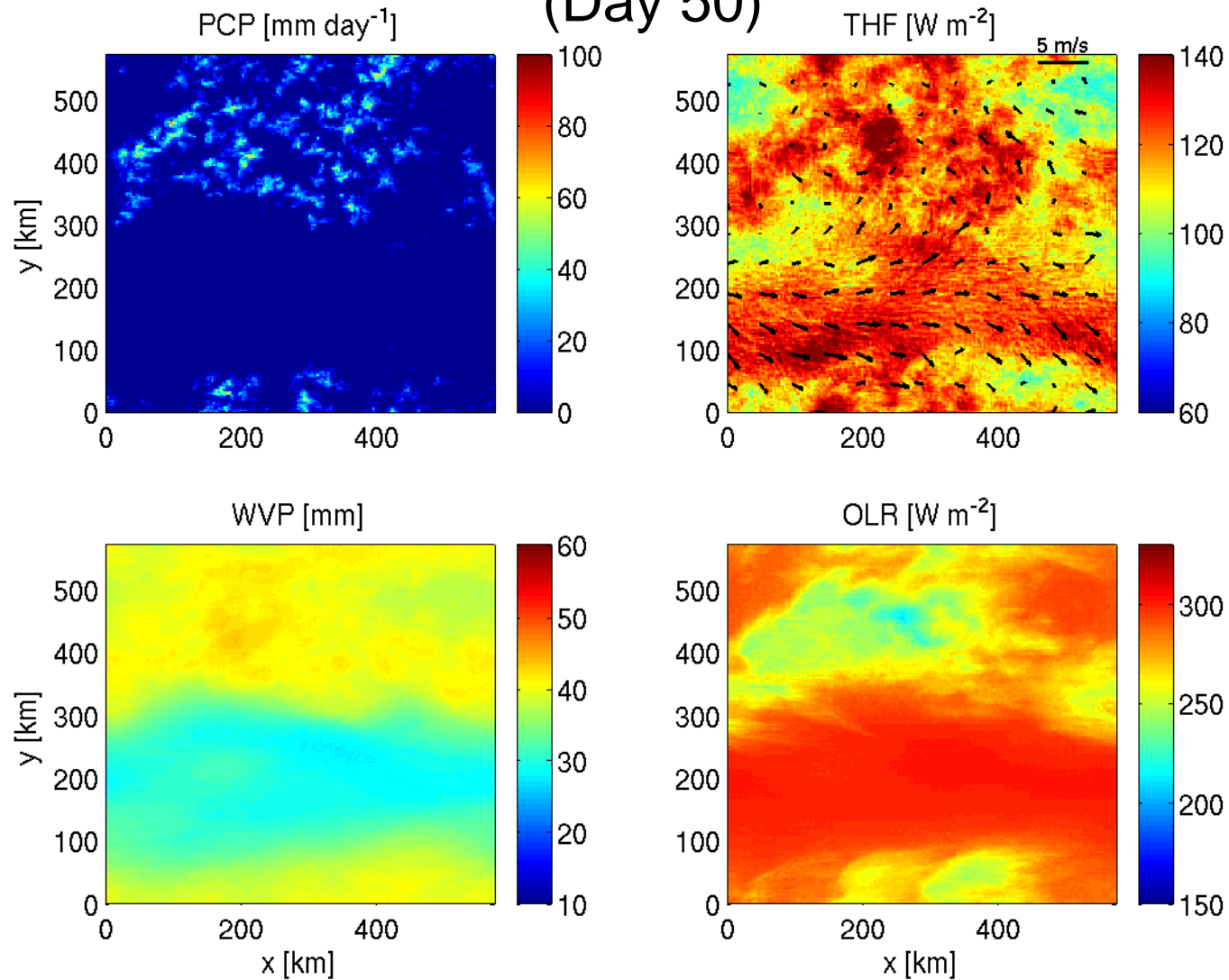
...an ODE for the column moisture r .

Instability if RHS positively correlated with r near RCE:

$$(c_S + c_R) + d\text{ADVH}/dr|_{\text{RCE}} > 0$$
$$(0.12 + 0.17) - 0.18 = 0.11 \Rightarrow \text{unstable (9d e-fold)}$$



Self-aggregation under unidirectional shear (Day 50)

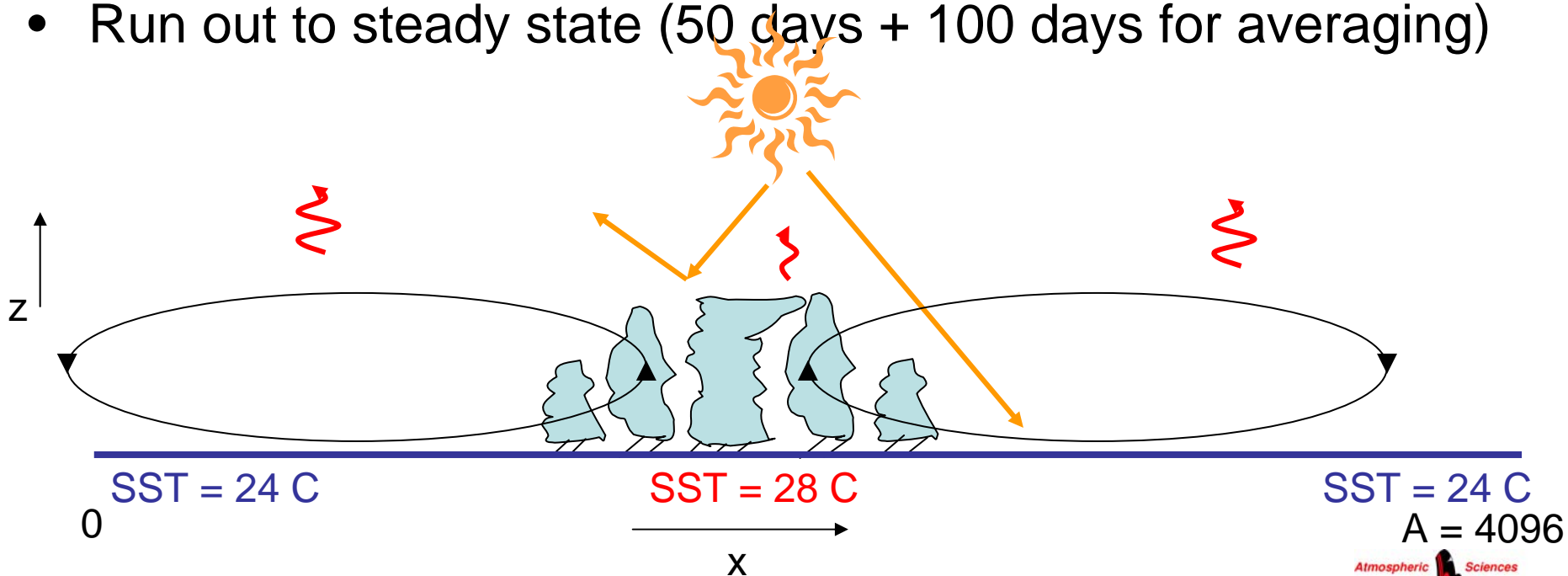


Fixed-SST Mock-Walker circulation (Grabowski et al. 2000)

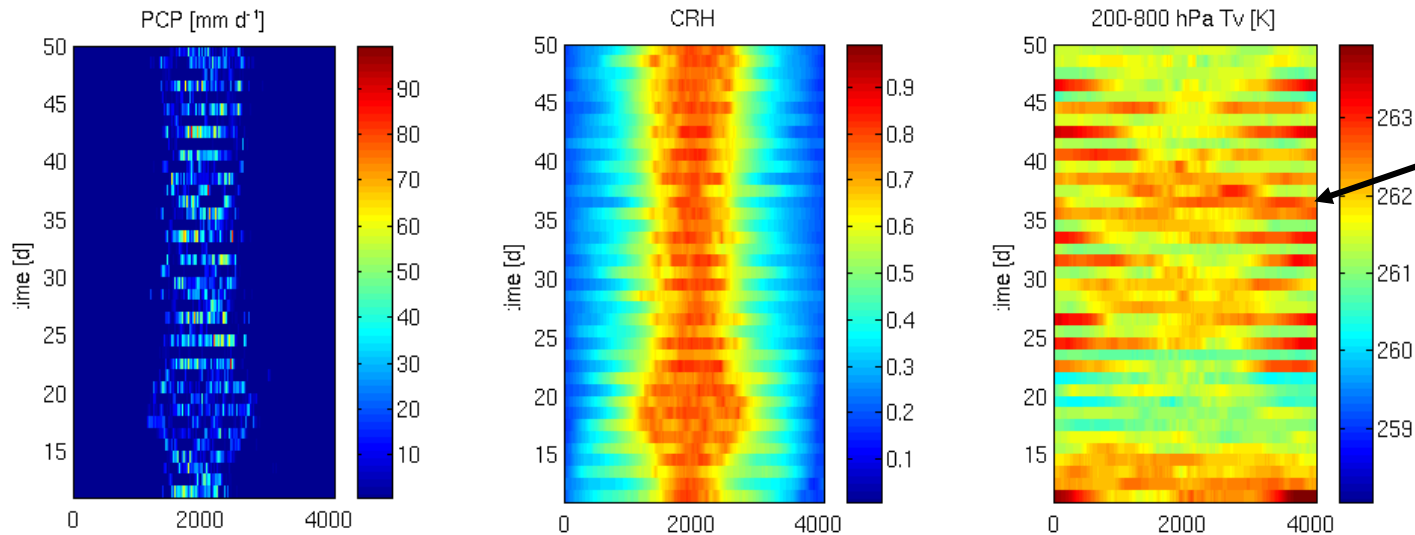
- No rotation, uniform insolation, periodic BCs
- Specified SST ($^{\circ}\text{C}$) = $26, 28 - 2 \cos(2\pi x/X)$.

Our study (Bretherton et al. 2005, submitted to TCFD)

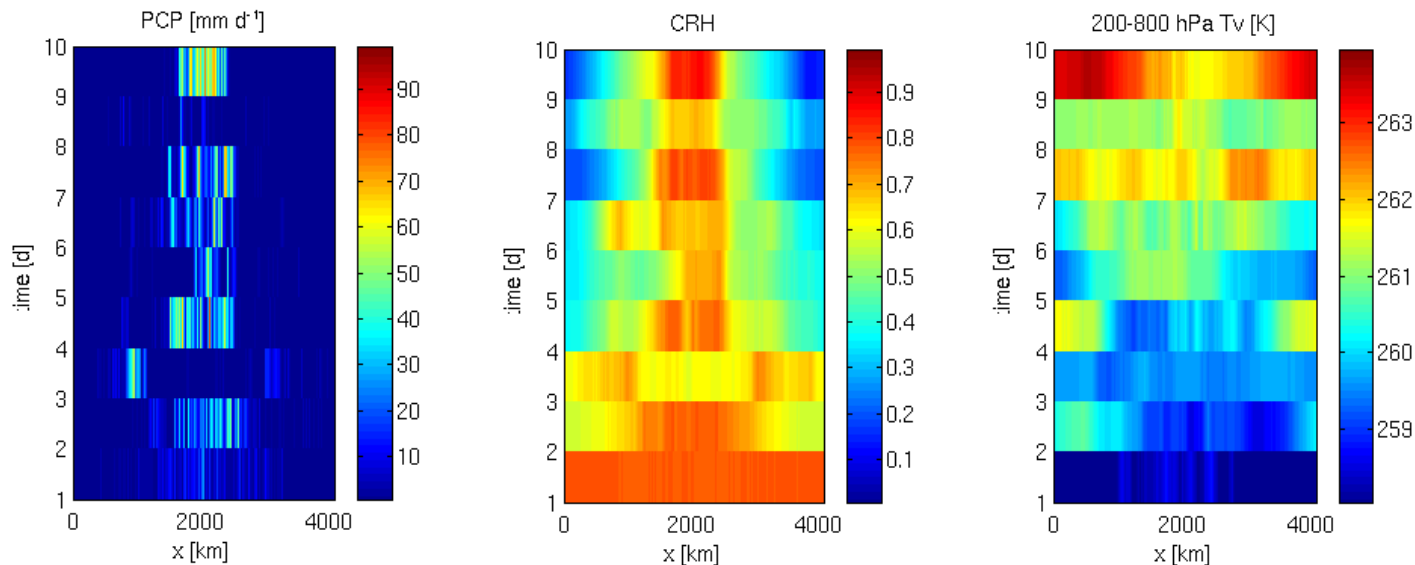
- SAM6.3 CRM (Khairoutdinov and Randall 2003)
- Bowling alley 4096 [1024] x 64 km, $\Delta x = 2$ km, 64 levels.
- Run out to steady state (50 days + 100 days for averaging)



Approach to equilibrium

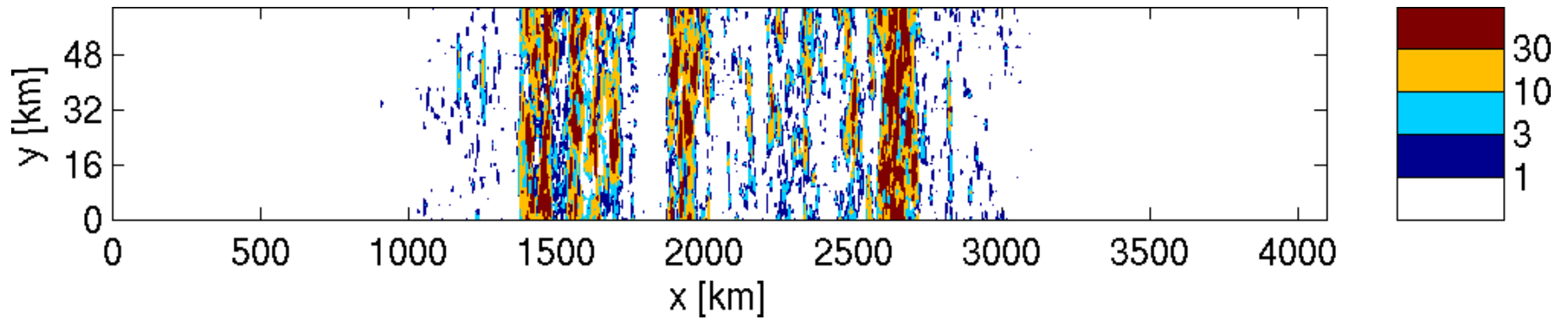


Standing
internal
waves

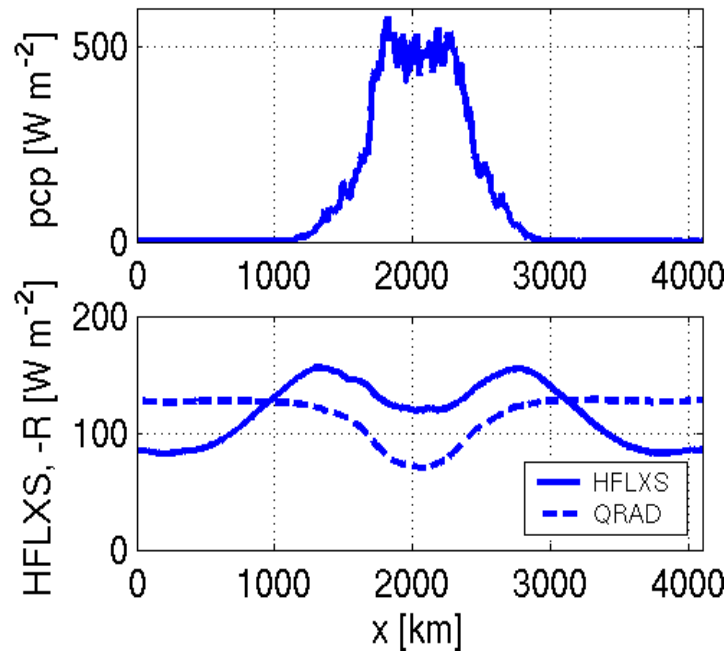


25d to thermal
equilibrium
after initial
warming

Mean rainfall for day 50

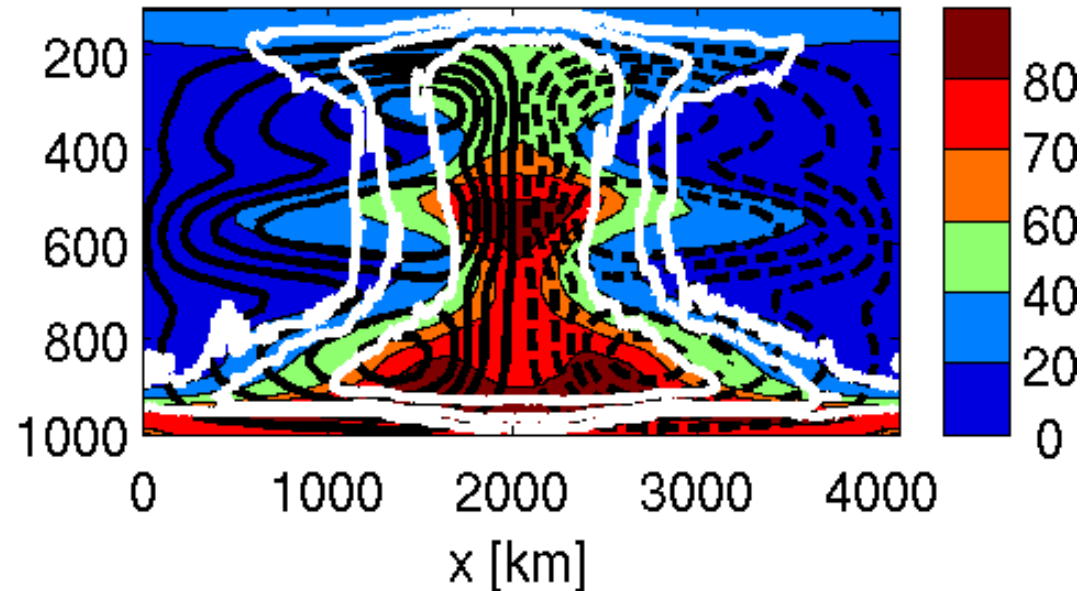


50-150 day mean Walker circulation



Thermally direct circulation

(b) CRM, relh: grey, Ψ : black, qn: white



What determines ascent
region width, rainfall?

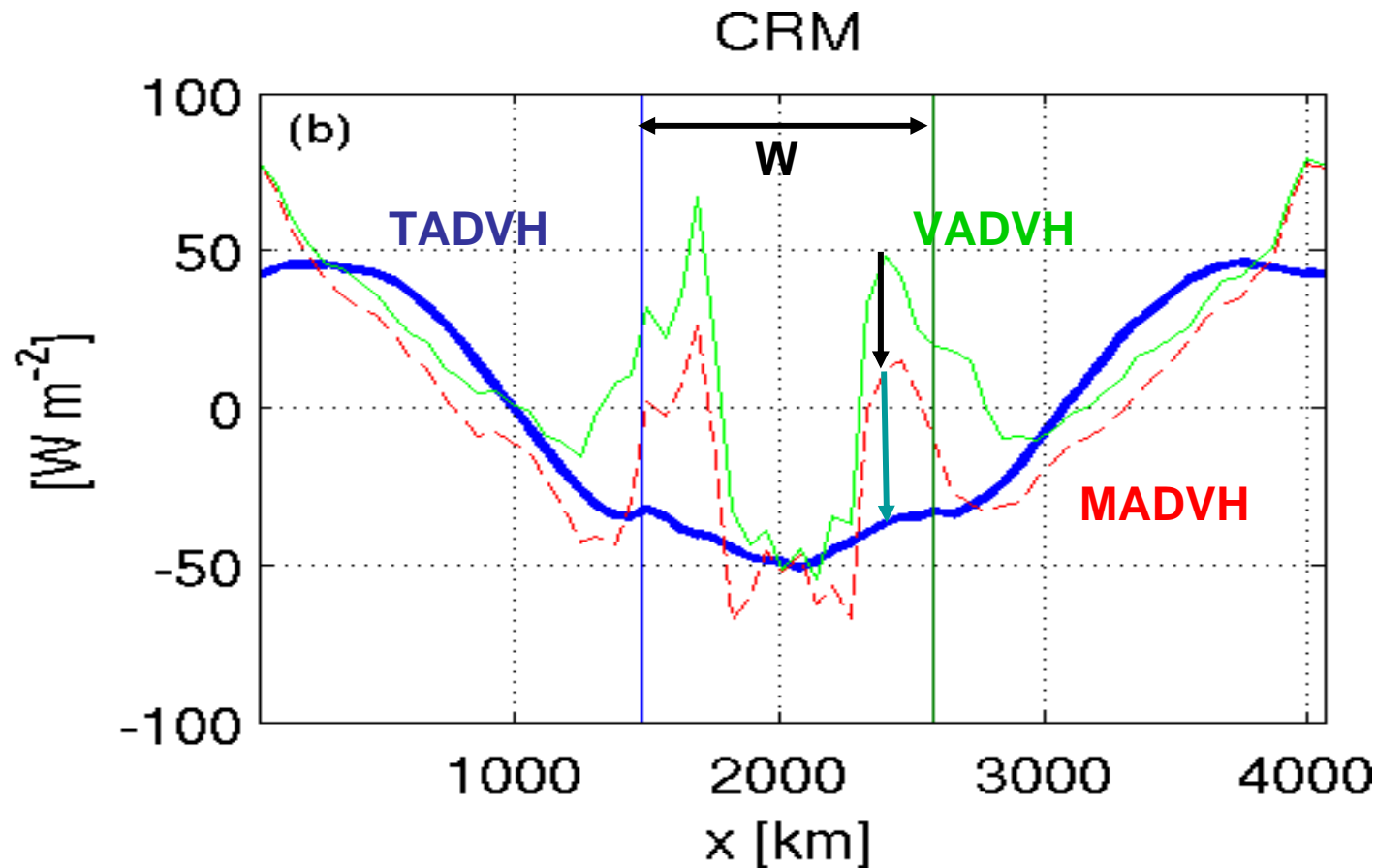
Steady-state MSE advection

$$0 = \text{THF} - \Delta R + \text{TADVH}$$

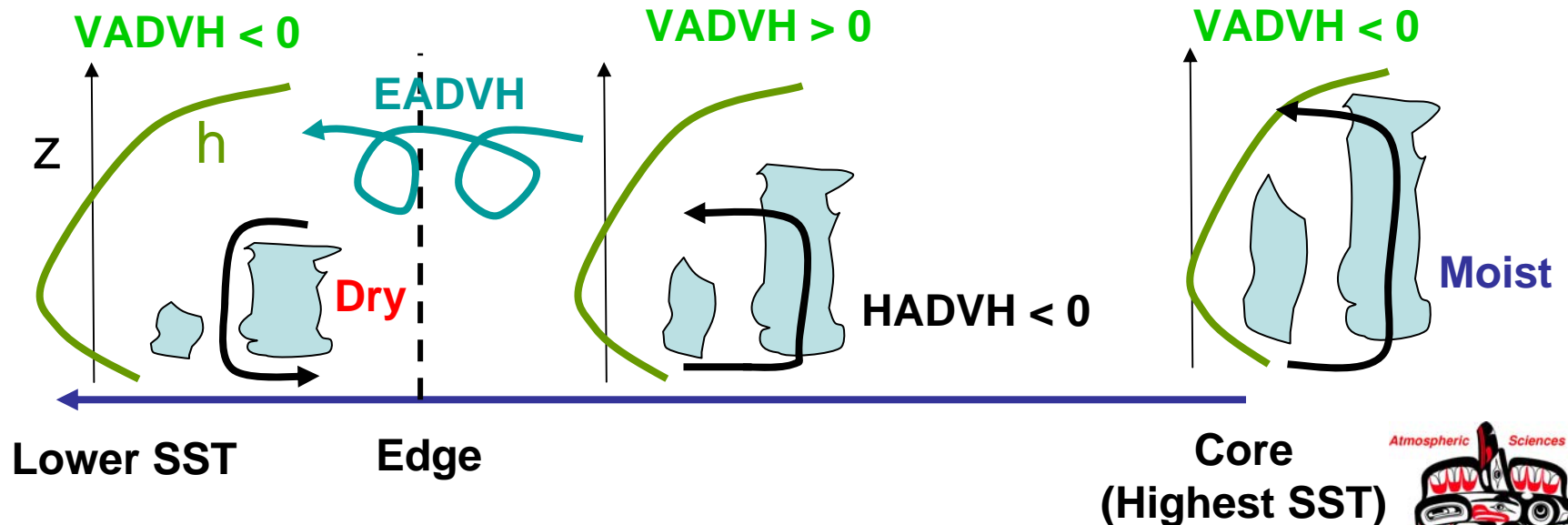
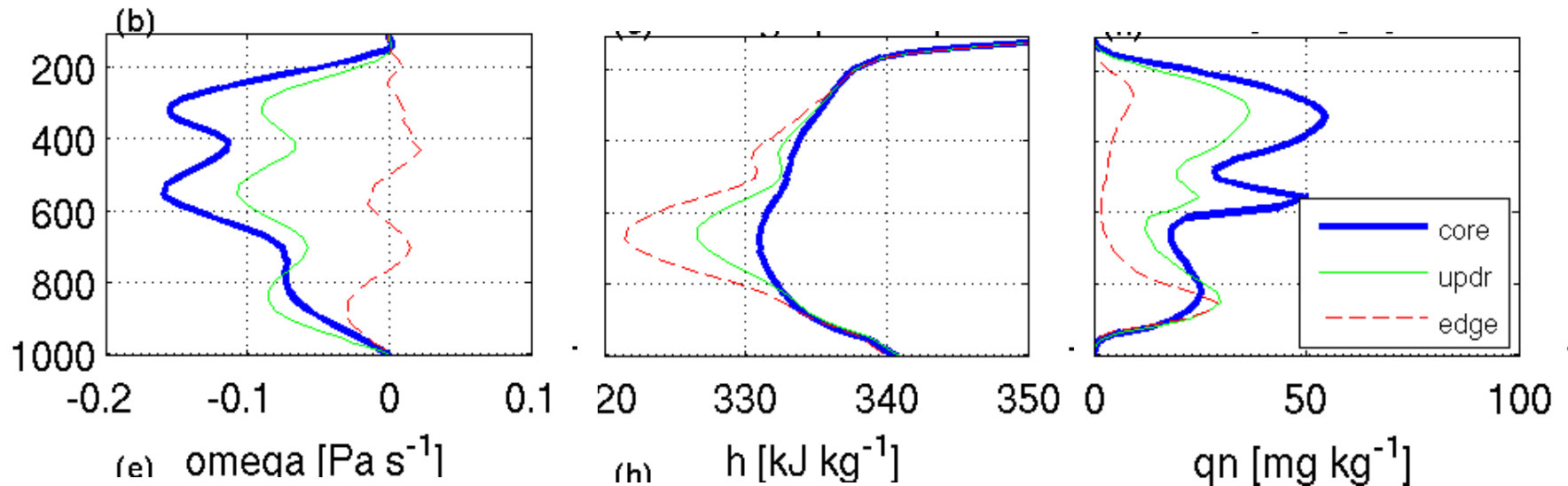
$$\text{TADVH} = \text{MADVH} + \text{EADVH}$$

$$\text{MADVH} = \langle -uh \rangle = \langle -h \nabla \cdot \mathbf{u} \rangle (\text{VADVH}) + \langle -\mathbf{u} \cdot \nabla h \rangle (\text{HADVH})$$

$$\text{EADVH} = \langle -u' h' \rangle$$



Horizontal structure of the ascent region



Ascent-region average MSE/DSE budgets

Goal: Understand ascent region ($\langle w \rangle > 0$) width W .

$$\text{MSE: } 0 = \overline{LHF} + \overline{SHF} - \overline{\Delta R} + \overline{MADVH} + \overline{EADVH}$$

$$\text{DSE: } 0 = \overline{LP} + \overline{SHF} - \overline{\Delta R} + \overline{VADVS} + \overline{HADVS} + \overline{EADVS}$$

Define ascent region moist stability ratio

$$\alpha = \underbrace{\overline{MADVH} / \overline{VADVS}}_{\alpha_M} + \underbrace{\overline{EADVH} / \overline{VADVS}}_{\alpha_E}$$

Then MSE + DSE \Rightarrow

$$\overline{LP} = \alpha^{-1} \left[\overline{LHF} + (1 - \alpha)(\overline{SHF} - \overline{\Delta R}) \right]$$

Assuming that almost all rainfall is in ascent region,

$$W \cdot \overline{LP} = A \cdot \overline{LHF} \quad (\text{rainfall} = \text{evaporation})$$

so

$$W / A \approx \alpha / D \quad D = \left[\overline{LHF} + (1 - \alpha)(\overline{SHF} - \overline{\Delta R}) \right] / \overline{LHF}$$

(diabatic forcing)

Does this MSE diagnosis work?

For our simulation

$$W/A = 0.27$$

$$\alpha_M = 0.08, \alpha_E = 0.04 \Rightarrow \text{Moist stability ratio } \alpha = 0.12$$

$$\text{Diabatic forcing } D = 0.44$$

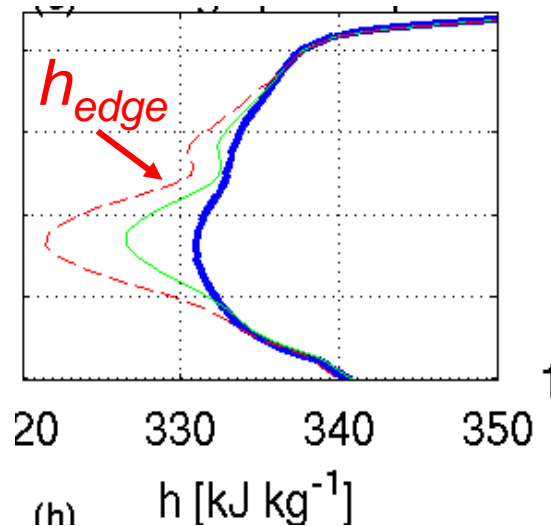
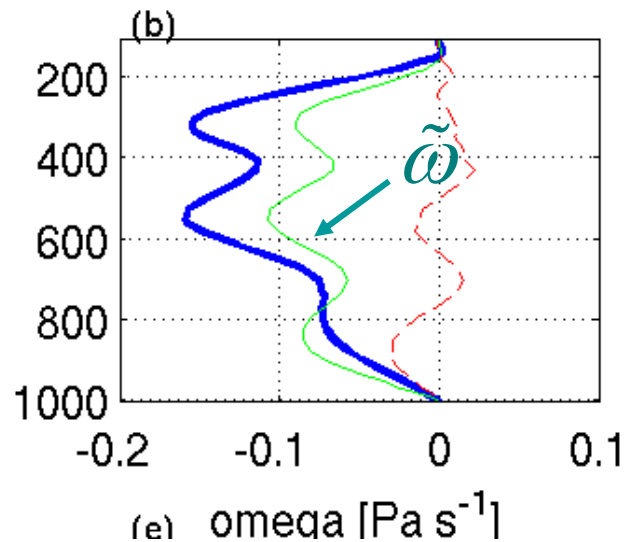
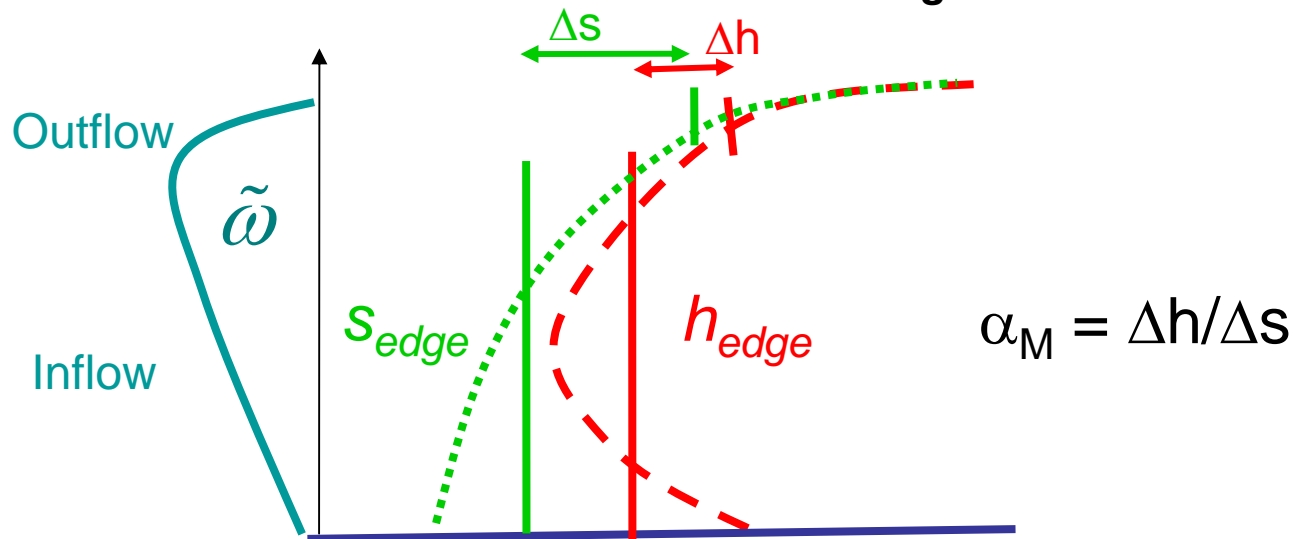
$$(W/A)_{\text{pred}} = \alpha/D = 0.27 \text{ (good)}$$

- Simulations with different A and/or SST_0 but the same ΔSST differ more in α than D, so α is key.
- Must understand α_M (α_E secondary unless A smaller).

$$\alpha_M = \frac{\overline{MADVH}}{\overline{VADV S}} = \frac{-\int_{p_T}^{p_s} \overline{\partial(uh)} / \partial x dp}{-\int_{p_T}^{p_s} \overline{s \partial u} / \partial x dp} = \frac{\int_{p_T}^{p_s} \overline{\omega \partial h_{edge}} / \partial p \cdot dp}{\int_{p_T}^{p_s} \overline{\omega \partial \tilde{s}} / \partial p \cdot dp}$$

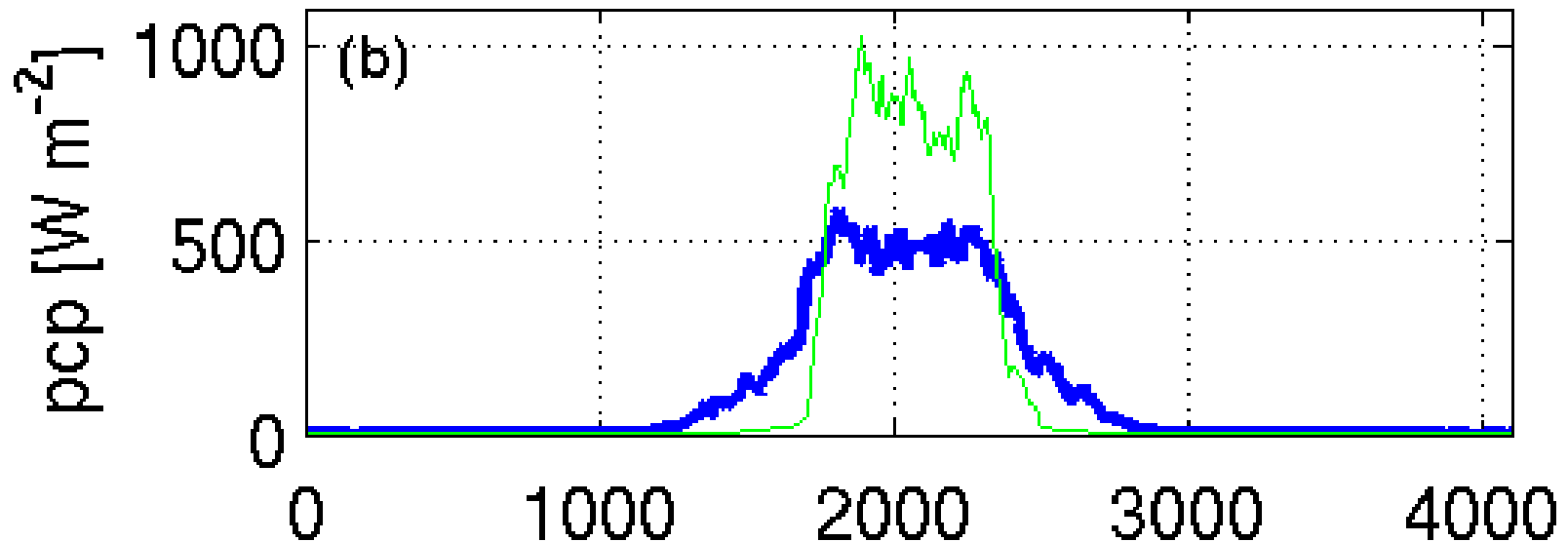
Understanding α_M

- Larger α_M if either ω top-heavy or **h_{edge} bottom-heavy**



ω -wiggles
contribute
significantly
to α .

SST+2 case vs. control



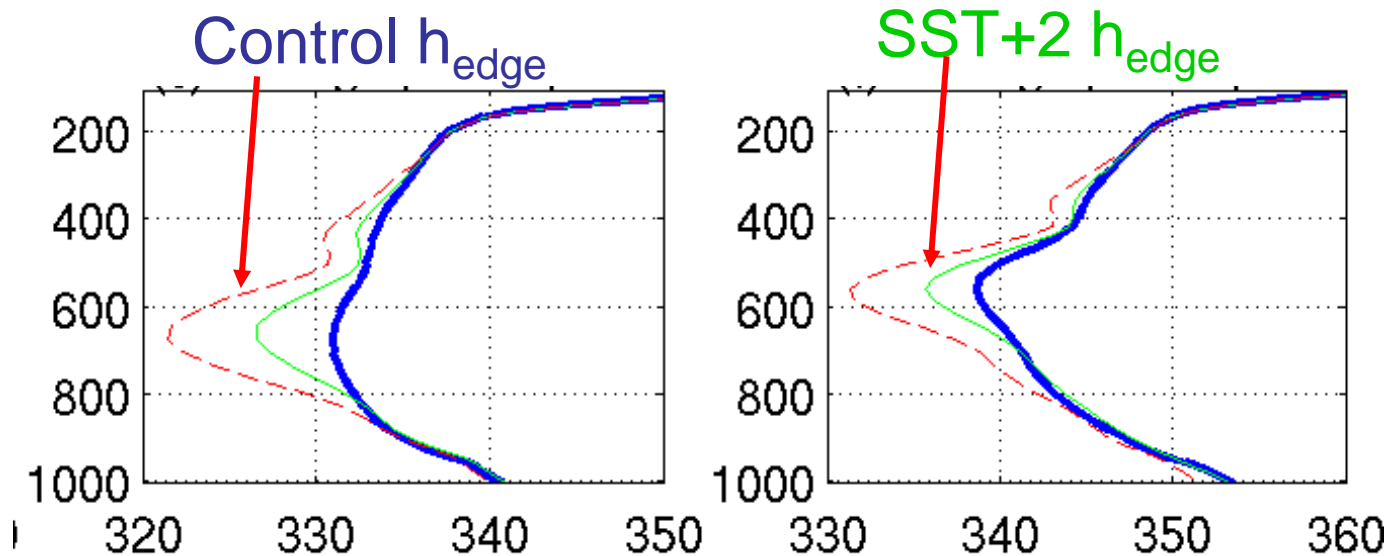
- Ascent-region width narrows, rainfall increases.
- Explainable with MSE reasoning?

$$W/A = \alpha/D, \quad \alpha_M = 0.01, \alpha_E = 0.04, D = 0.30, W/A = 0.17$$
$$(\alpha_M = 0.08, \alpha_E = 0.04, D = 0.44, W/A = 0.27)$$

- Decreased width associated with smaller α_M

Why does SST+2 have lower moist stability?

- Decreased moist stability α_M reflects less bottom-heavy h_{edge}



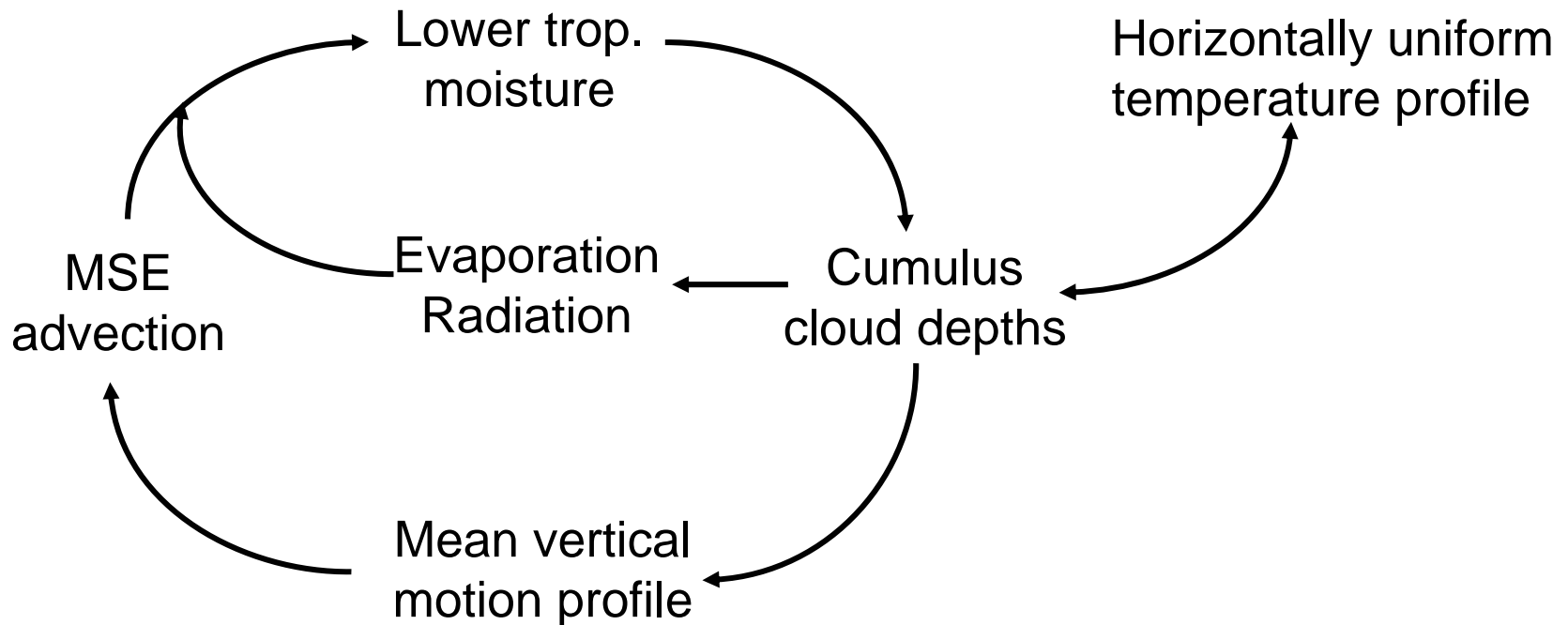
Two speculative reasons:

- More radiative cooling in SST+2 destabilizes h profile
- Higher freezing level moves up h minimum.

This type of reasoning can help us understand the response of tropical ITCZ regions to climate change.

Conclusions

- Over warm oceans, moisture-convection feedbacks fundamental to transient convection and mean rainfall.



- Column moist static energy budgets are a fruitful approach to understanding these feedbacks.